

Momentum and Collisions

How do things look from a different reference frame; and how do we analyze a collision?

Useful equations

$$m^2 = E^2 - p^2 \qquad \gamma = \frac{1}{\sqrt{1-v^2}}, \text{ where } v \text{ is expressed as a fraction of } c.$$

$$E = m\gamma \qquad E = E_{rest} + K, \text{ where } E_{rest} = m$$

$$\bar{p}_x = m\bar{v}_x\gamma \qquad v = \frac{p}{E}$$

An object of mass 8 units is traveling with a velocity of 0.6c in the positive x-direction, according to you.

According to you:

What is the object's energy, E?

What is the object's kinetic energy, K?

What is the object's momentum, \bar{p} ?

In Karen's frame of reference the object has a velocity of 0.9c in the positive x-direction.

According to Karen:

What is the object's energy, E?

What is the object's kinetic energy, K?

What is the object's momentum, \bar{p} ?

Now let's analyze a collision.

In your reference frame an object with a mass of 3 mass units is traveling in the positive x-direction at a speed of $0.8c$. It collides with a second object that has a mass of 8 units and that is traveling in the negative x-direction at a speed of $0.6c$.

Sketch the momenergy vectors for the first object, the second object, and the system of two objects, before the collision.

The total energy in this system is: _____

The total momentum in this system is: _____

The total momenergy in this system is: _____

The objects stick together after the collision.

What is the velocity of the object after the collision?

What is the mass of the combined object after the collision?