## PROBLEM 1 - 10 points

Two charges are placed on the $x$-axis. The charge at $x=-3 d$ has a charge of $-2 Q$, while the charge at +3 d has a charge of $+Q$.

[2 points] (a) The net electric potential due to the two charges is zero at at least one location on the x -axis near the two charges. In which region(s) is there such a point on the x -axis, where the net electric potential is zero a finite distance from the charges? Select all that apply.
[ ] to the left of the -2 Q charge
[ ] between the charges
[ ] to the right of the +Q charge
[5 points] (b) Determine the location of one such point on the x-axis near the charges where the net electric potential is zero.
[3 points] (c) Are there any points near the charges, but not on the $\mathbf{x}$-axis, where the net electric potential due to the point charges is zero? Explain.

## PROBLEM 2-15 points

Three configurations of point charges are shown. Each charge is located a distance d from the origin. In each case the origin is located at the intersection of the axes. The electric potential from a single charge is defined to be zero an infinite distance from the charge, and the electric potential associated with two charges is also defined to be zero when the charges are infinitely far apart.

[4 points] (a) In configuration $A$, imagine that the $+Q$ and $-Q$ charges are placed at the locations shown, and then the +7 Q charge is brought into the picture and placed at its location. Does bringing in the +7 Q charge cause the potential energy of configuration A to increase, decrease, or stay the same? Briefly explain.
[4 points] (b) In configuration $\mathbf{B}$, what is the electric potential at the origin because of the four charges? You can express this in terms of $\mathrm{k}, \mathrm{Q}$, and d .
[3 points] (c) Rank the three configurations based on the electric potential at the origin due to the charges, from largest to smallest.
[ ] $\mathrm{A}>\mathrm{B}>\mathrm{C}$
[ ] A $>C>B$
[ ] $A=B>C$
[ ] $\mathrm{B}>\mathrm{A}>\mathrm{C}$
[ ] B $>\mathrm{C}>\mathrm{A}$
[ ] $\mathrm{C}>\mathrm{A}>\mathrm{B}$
[ ] C $>B>A$
[ ] $\mathrm{C}>\mathrm{A}=\mathrm{B}$
[4 points] (d) In one, and only one, of the configurations the total potential energy is negative. Which configuration is this?
[ ] A
[ ]B
[ ] C

Briefly explain your answer:

A parallel-plate capacitor, with air between the plates (dielectric constant $=1$ ) is charged by being connected to a battery that has a voltage of $V_{0}$. Then, a series of steps is carried out, as shown below. For each step, fill in the table with the potential difference across the capacitor, in terms of $V_{0}$; the capacitance, in terms of the initial capacitance, $C_{0}$; the charge stored in the capacitor, in terms of the initial charge $Q_{0}$; the magnitude of the uniform electric field in the capacitor, in terms of the initial value $E_{0}$; and the stored electric energy, in terms of the initial energy $U_{0}$. The values after step 1 are shown, as an example.

Step 1: After the wires connecting the battery to the capacitor are removed, the distance between the capacitor plates is doubled.

Step 2: After completing step 1, a dielectric, with a dielectric constant of 3, is placed in the capacitor, completely filling the space between the plates.

Step 3: After completing step 2, the battery is re-connected to the capacitor.
Step 4: After completing step 3, the dielectric is removed from the capacitor.

|  | Potential <br> difference | Capacitance | Charge | Field | Energy |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Initially | $V_{0}$ | $C_{0}$ | $Q_{0}$ | $E_{0}$ | $U_{0}$ |
| 1. Wires <br> removed, then <br> distance is <br> doubled | $2 V_{0}$ | $\frac{C_{0}}{2}$ | $Q_{0}$ | $E_{0}$ | $2 U_{0}$ |
| 2. Dielectric <br> inserted |  |  |  |  |  |
| 3. Battery re- <br> connected |  |  |  |  |  |
| 4. Dielectric <br> removed |  |  |  |  |  |

Show work here.

