

# New Scaling in an Old Earthquake Model

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C. A. Serino and W. Klein

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# Empirical Scaling

$$N_{GR} (M_0 > m) = A m^{-b}$$

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- Gutenberg & Richter observe the now-famous **relation** [Gutenberg and Richter, *Ann. Geophys.* **9**, 1 (1956)]:

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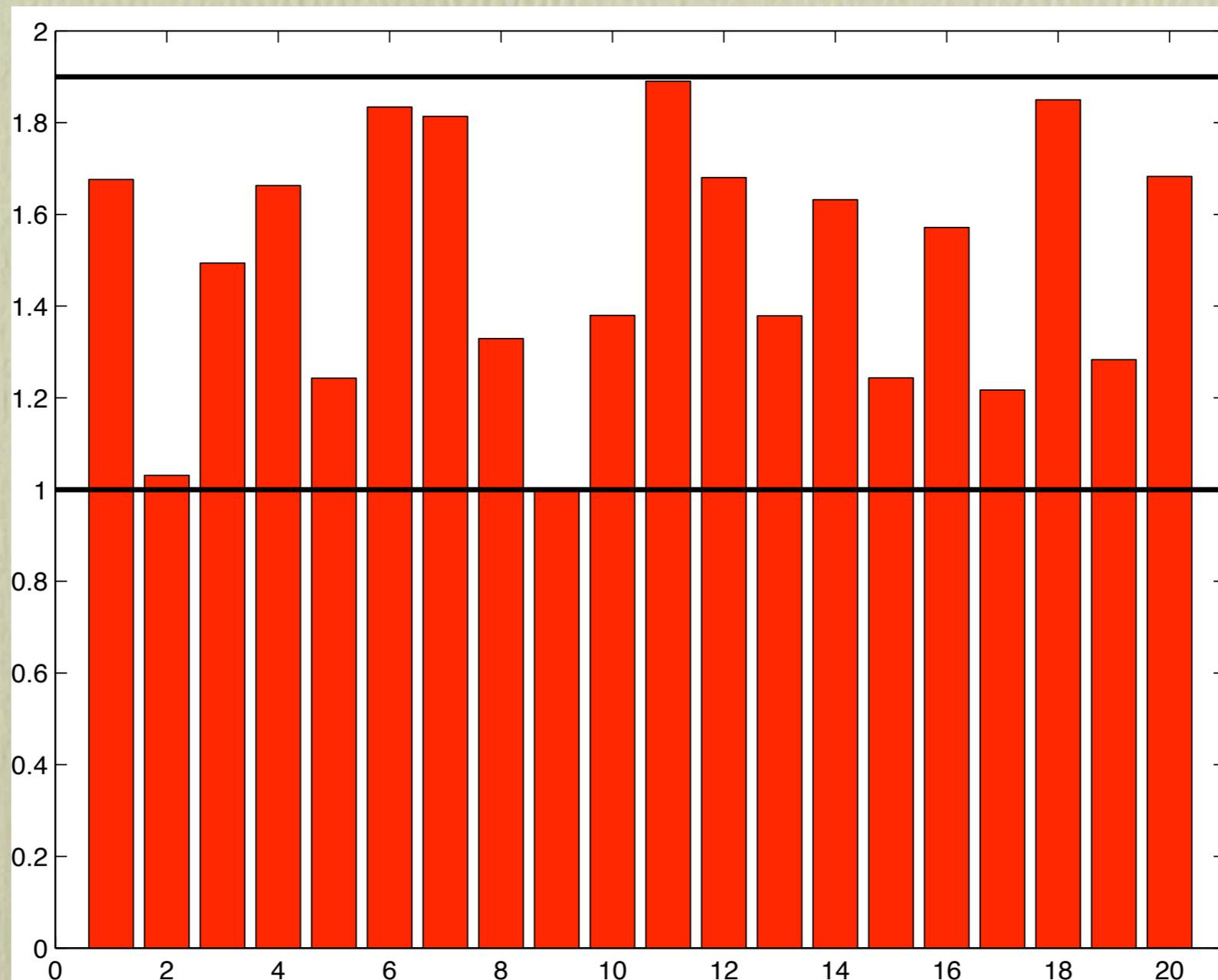
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- Scaling occurs over *fault systems*, not single faults and  $b$  is determined from a *cumulative* distribution.
- Typical b-values lie in  $0.8 \leq b \leq 1.2$  but can vary outside this region [Frohlich and Davis, *J. Geophys. Res.* **98**, 631-644 (1993)].

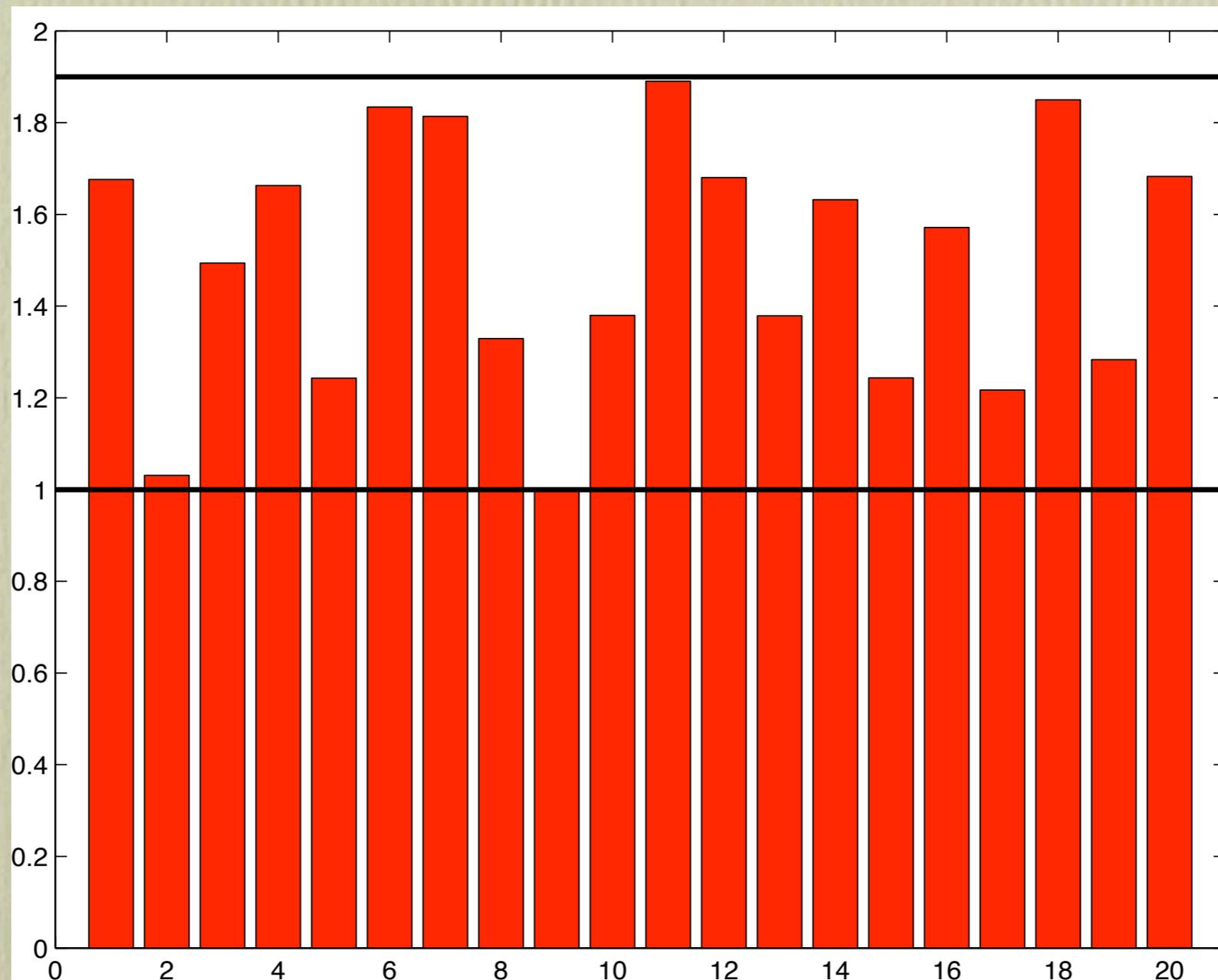
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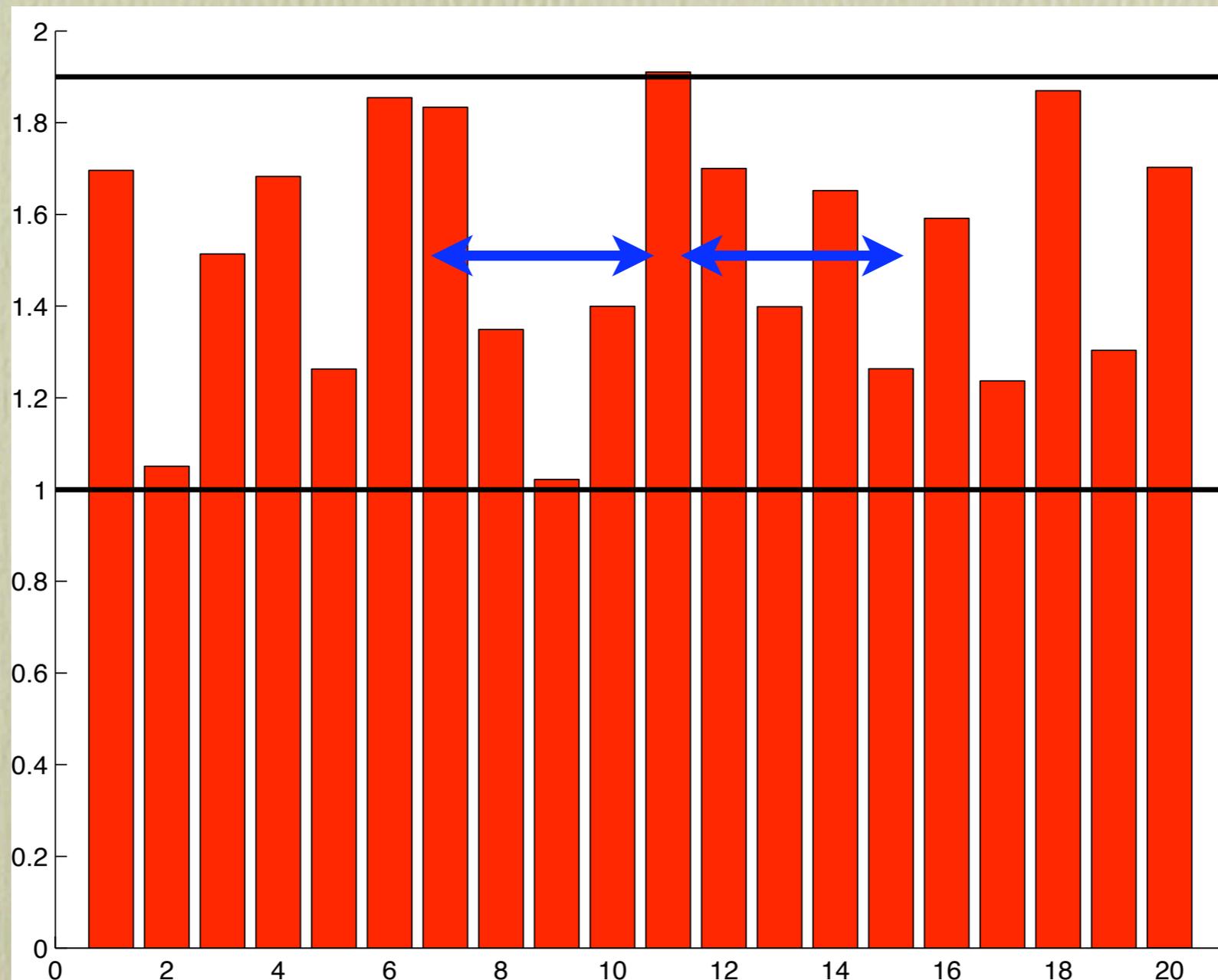
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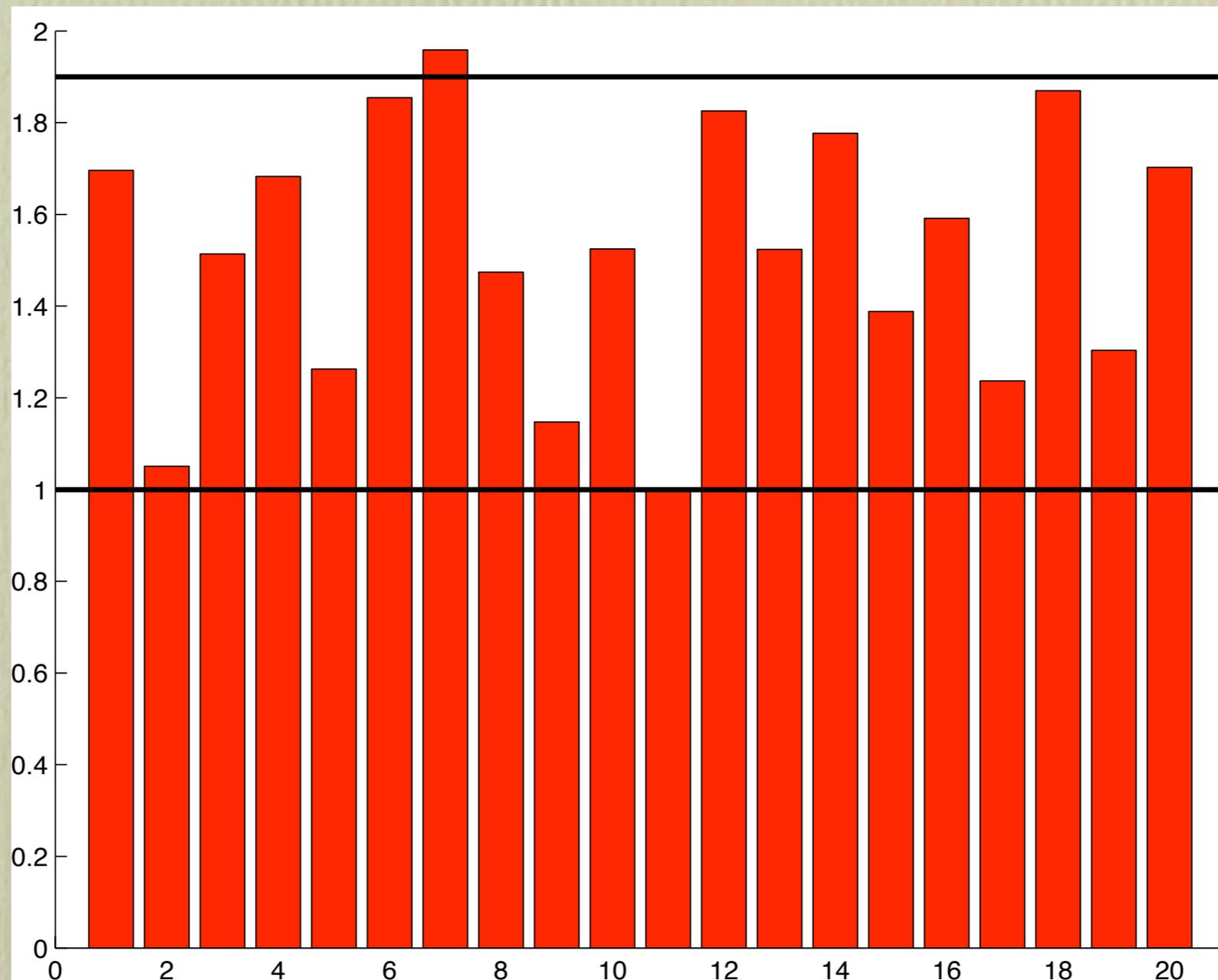
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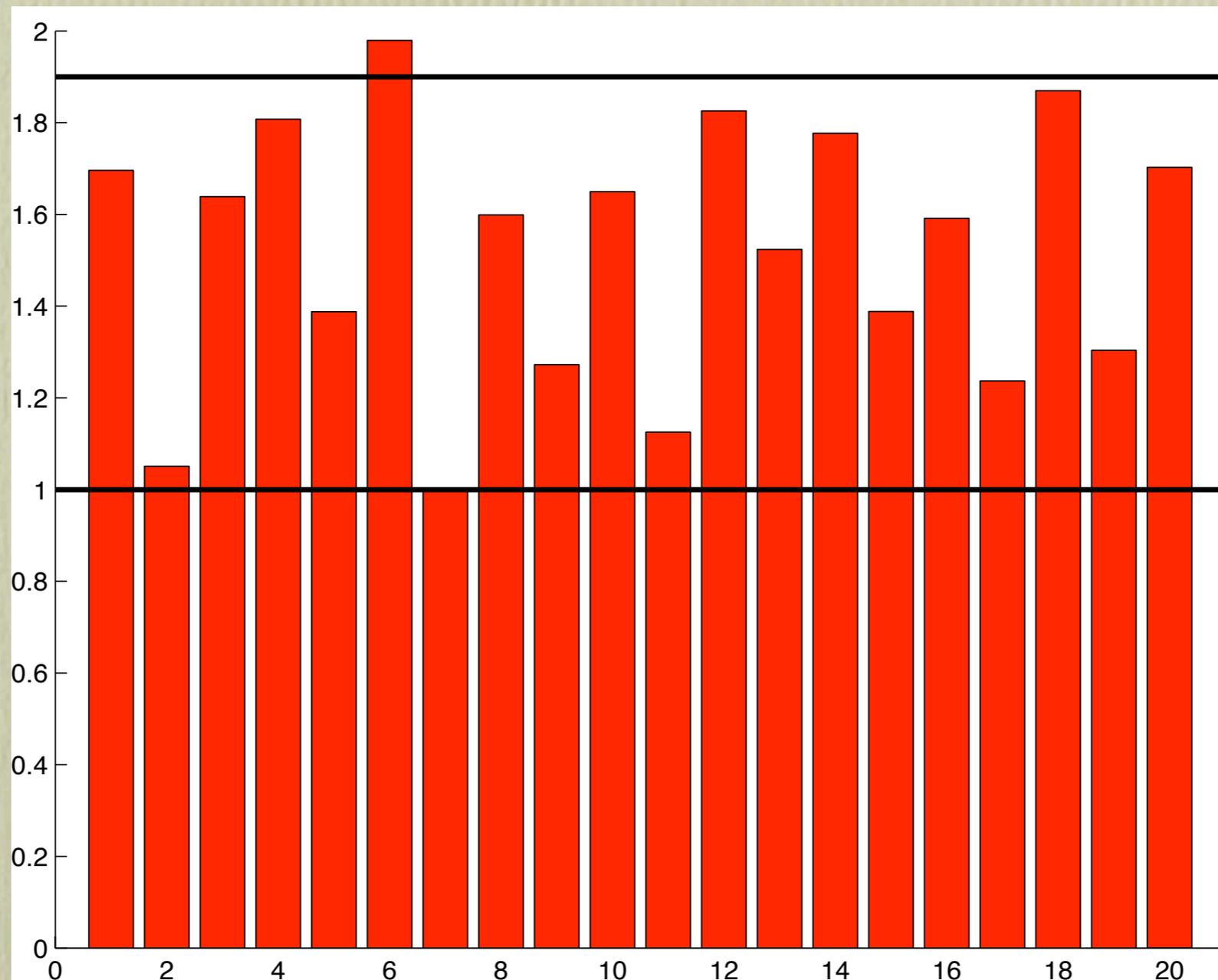
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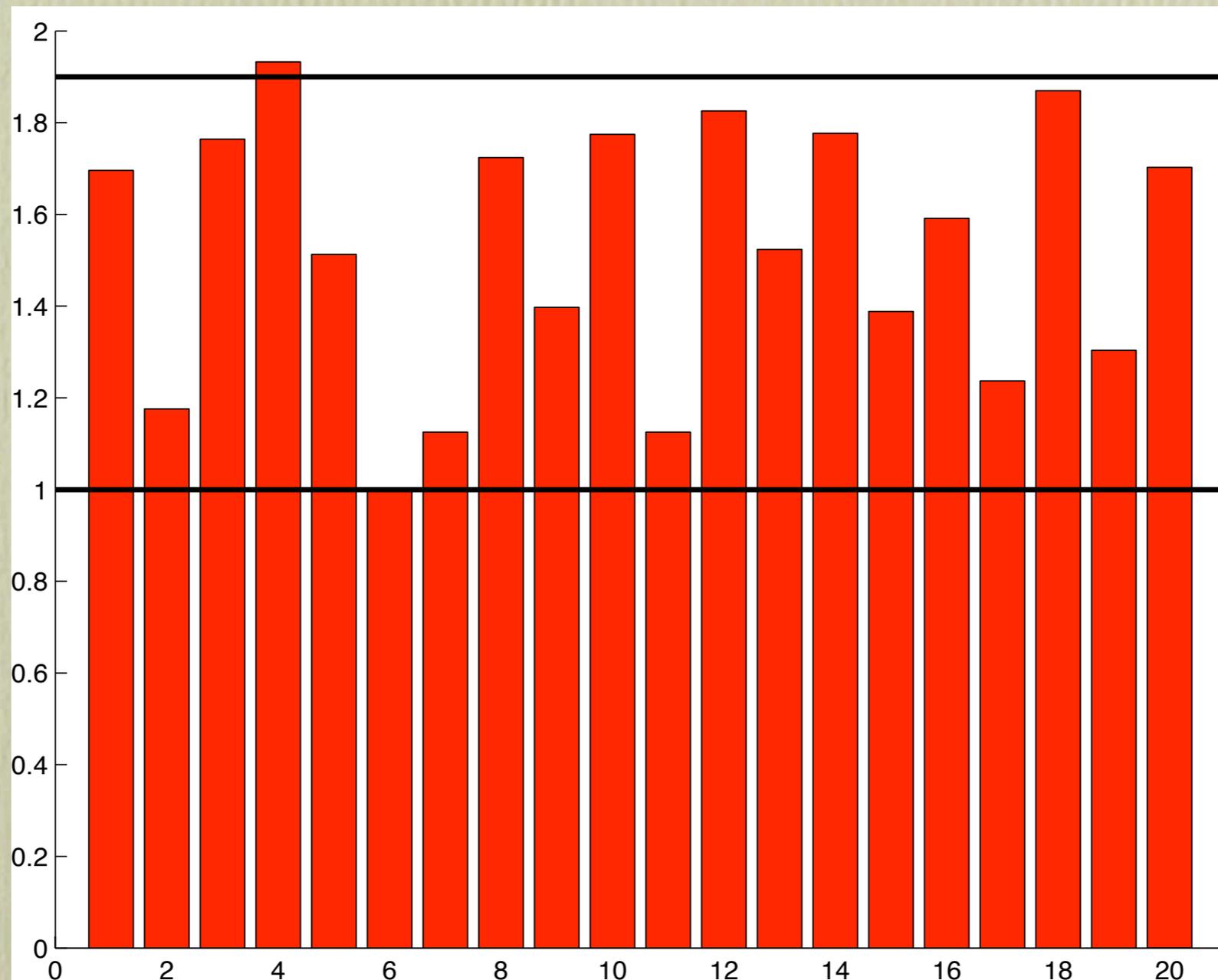
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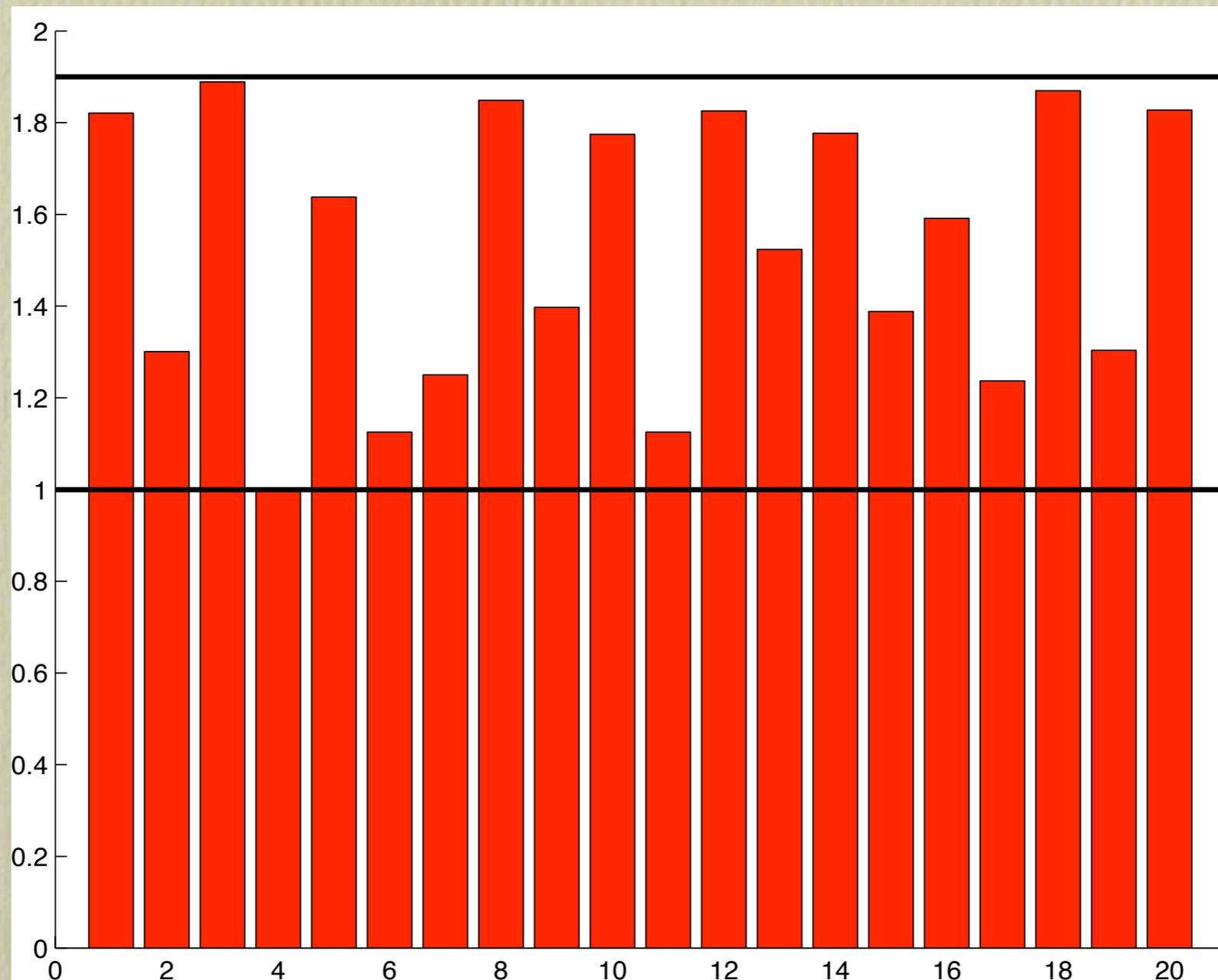
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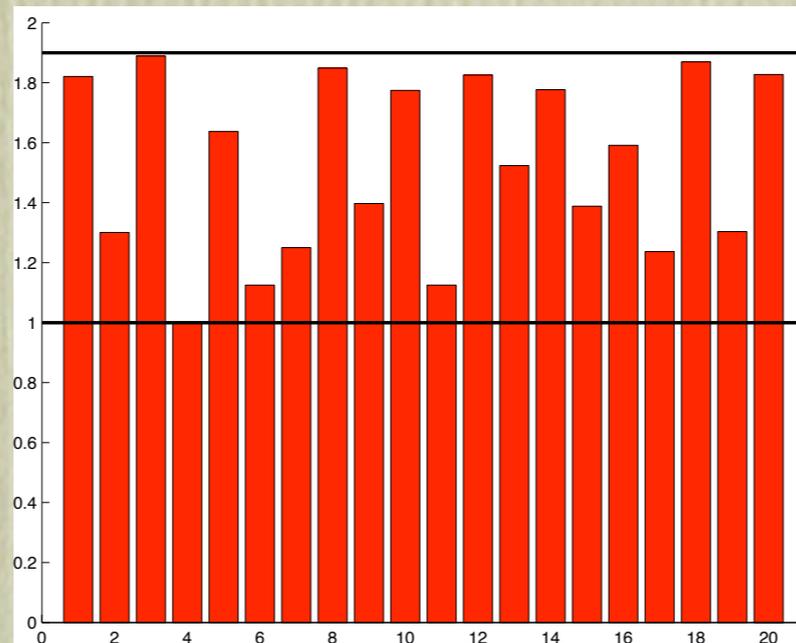
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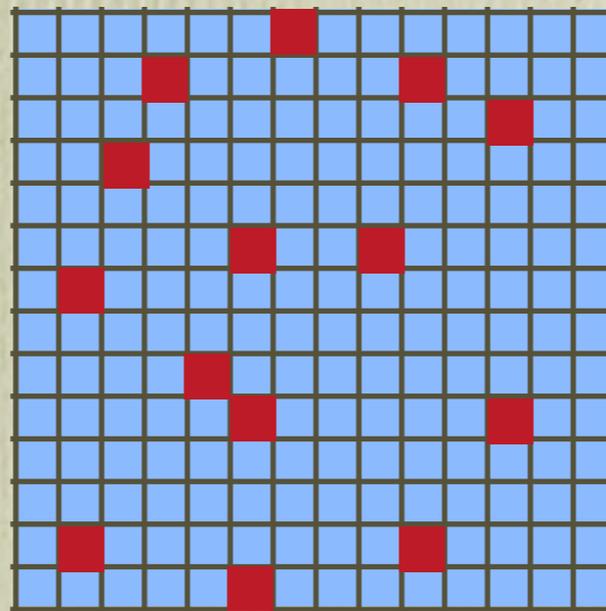
- These dynamics yield “cluster scaling”  
 $N(s) \propto s^{-\tau}$  with  $\tau = 3/2$  where  $b = \tau - 1$ .

# Introduce Damage

- We can “freeze in” a certain fraction of damaged sites,  $1 - \phi$ , that cannot receive stress from their neighbors.

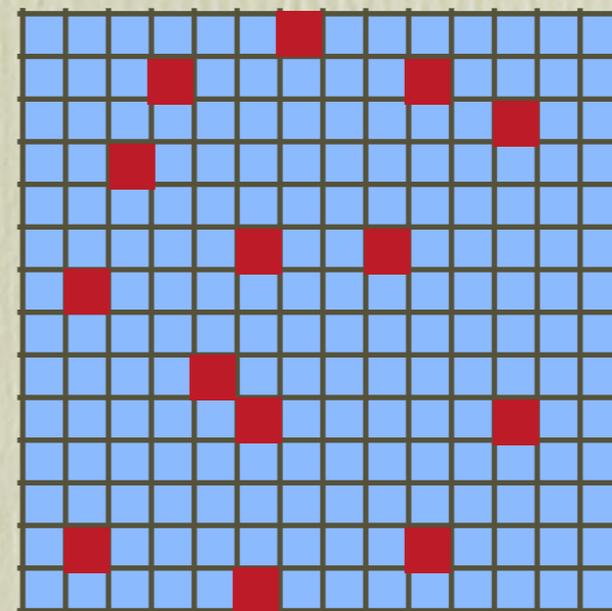
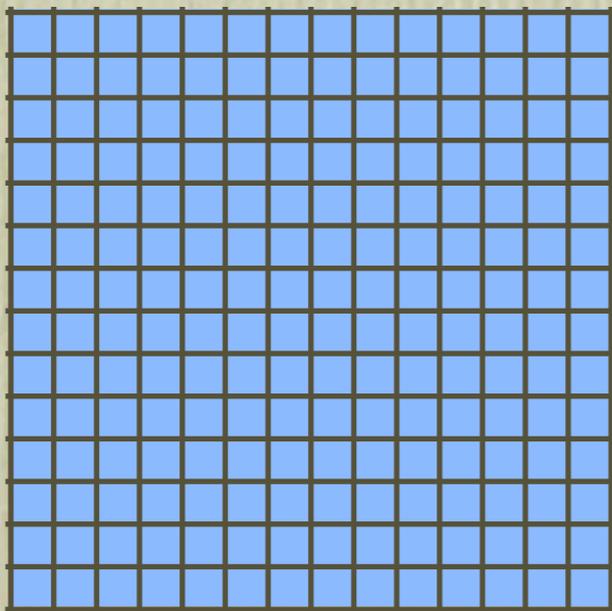
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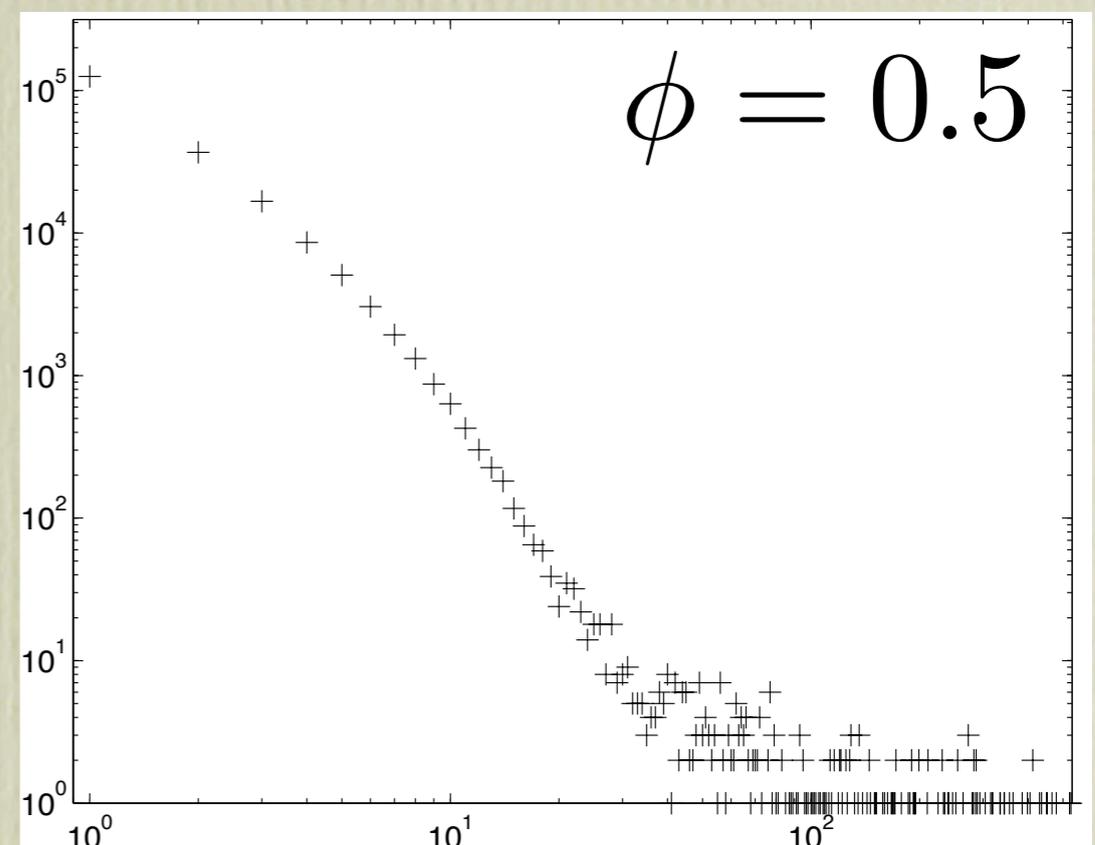
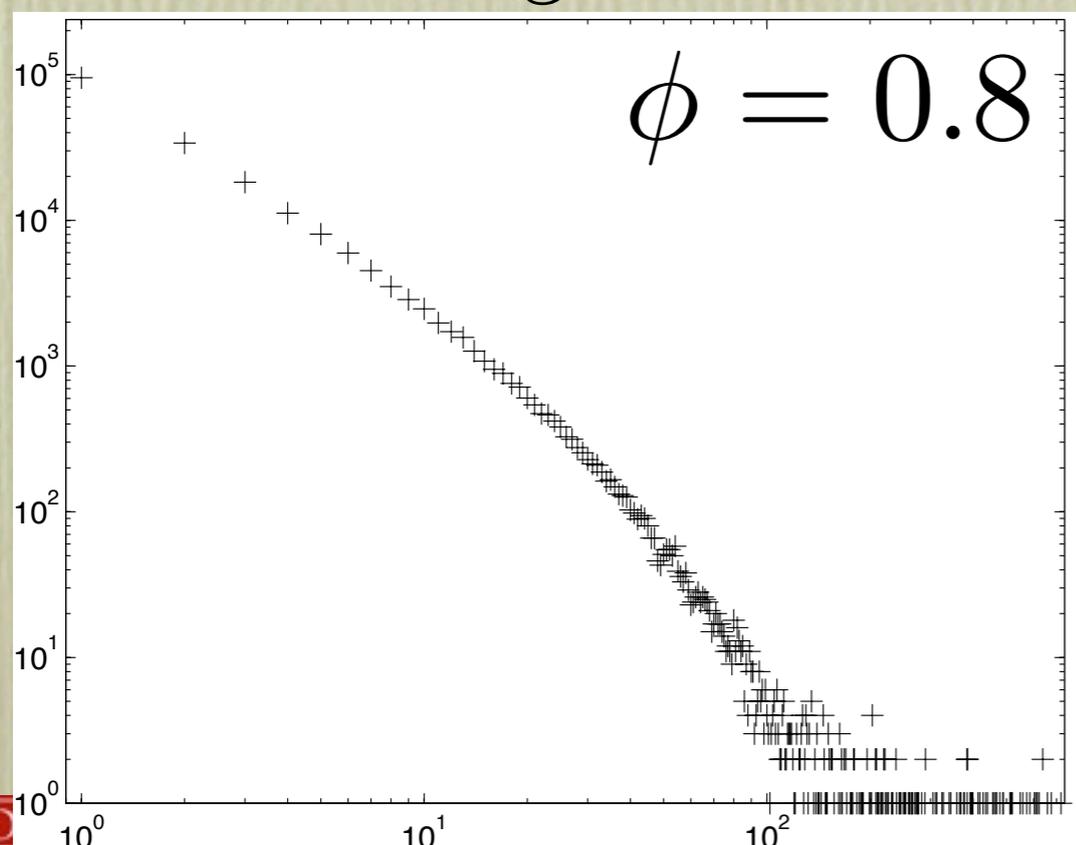
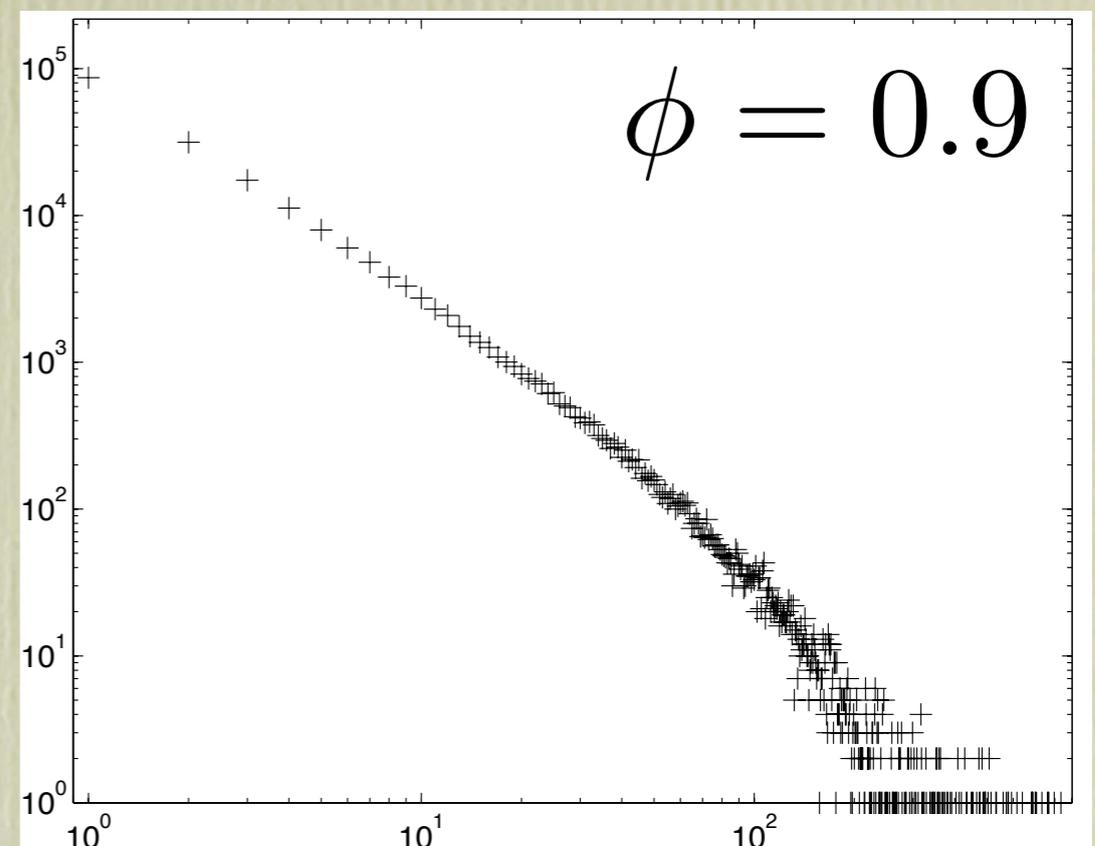
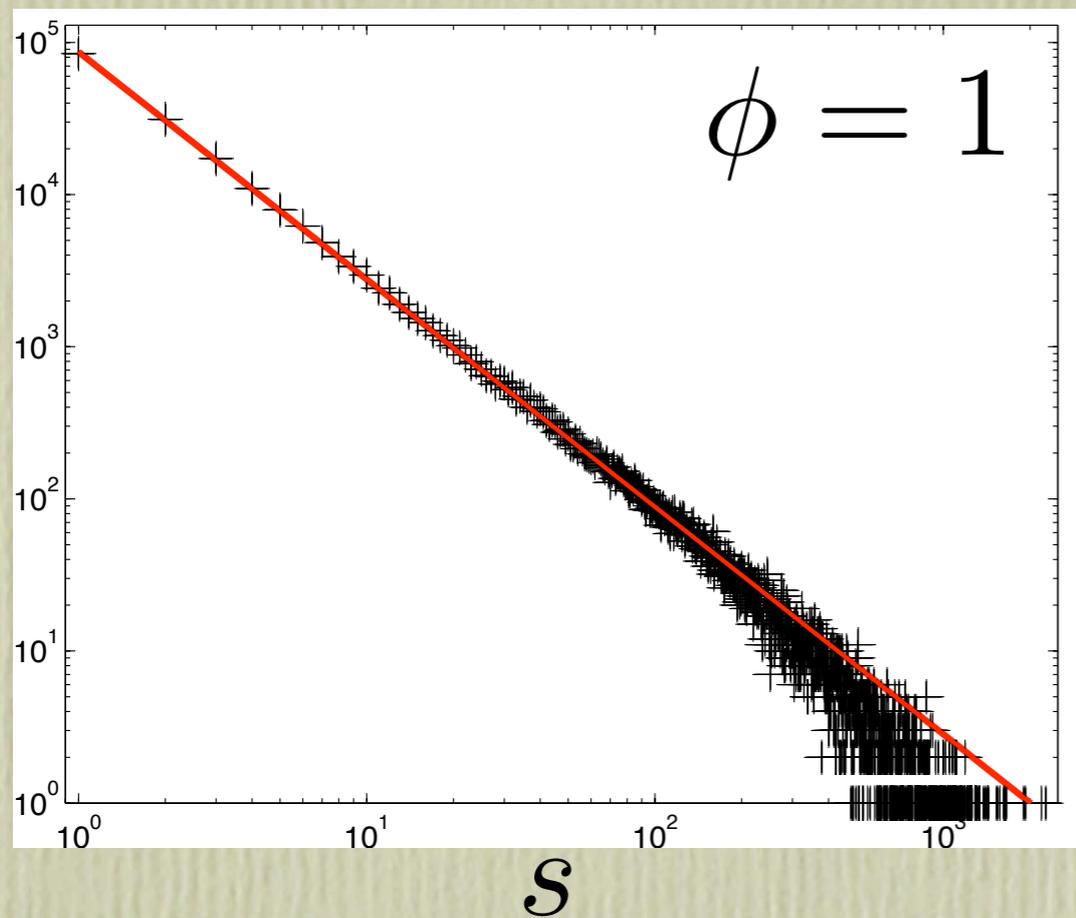
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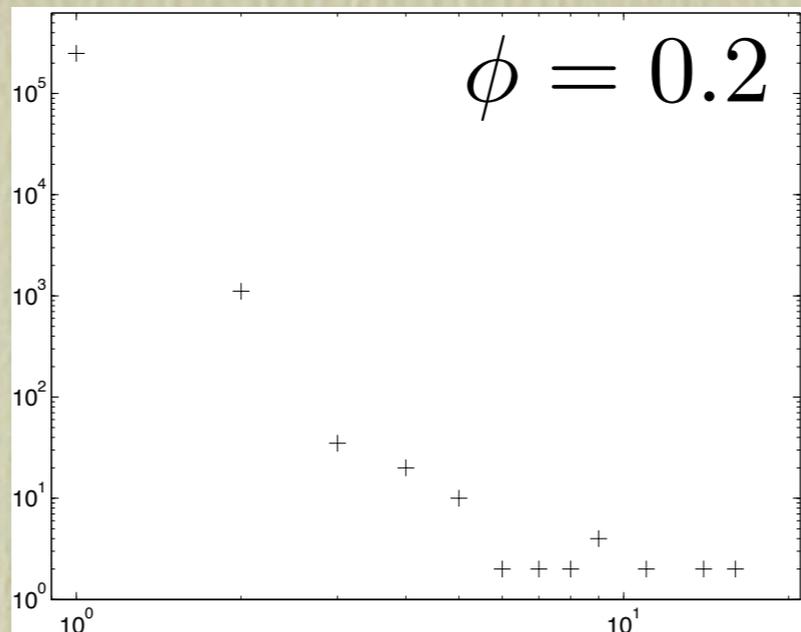
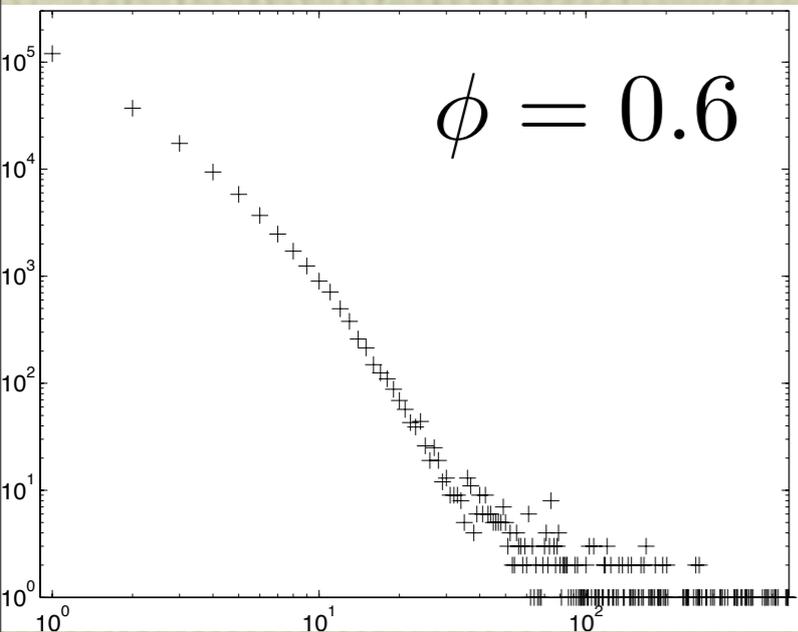


# Reduced Scaling Regime

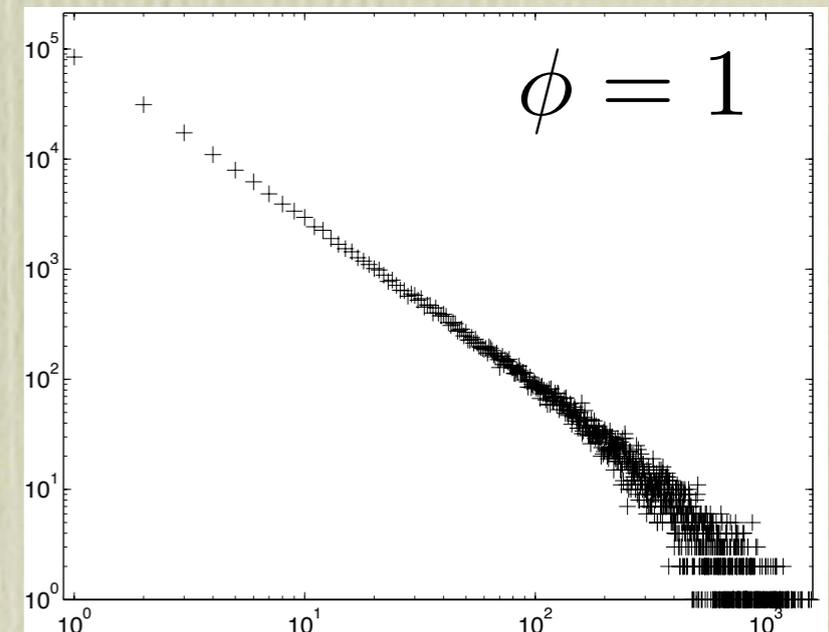
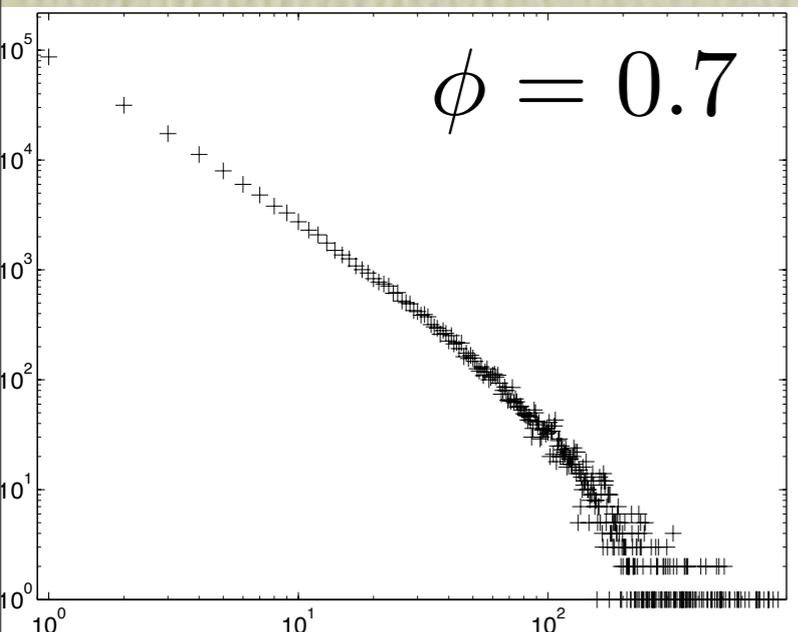
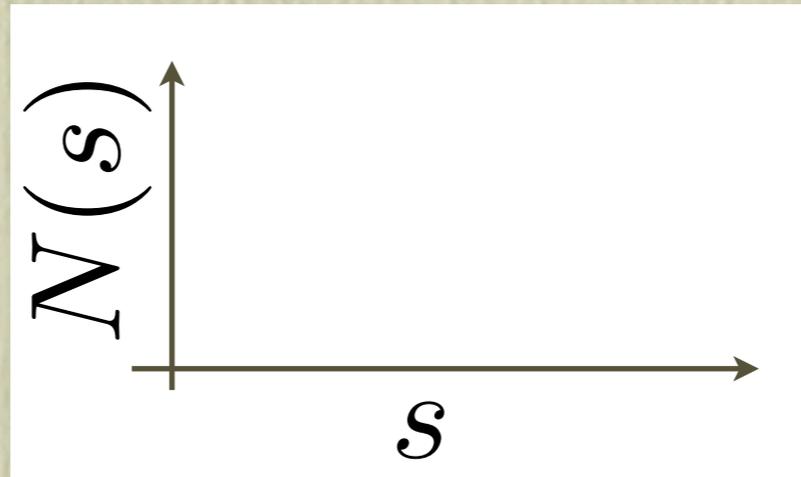
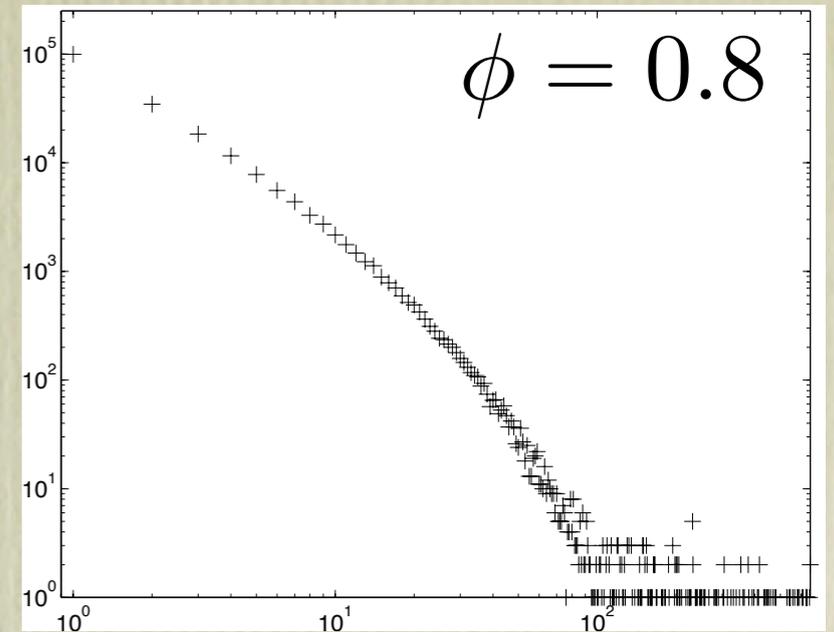
$N(s)$



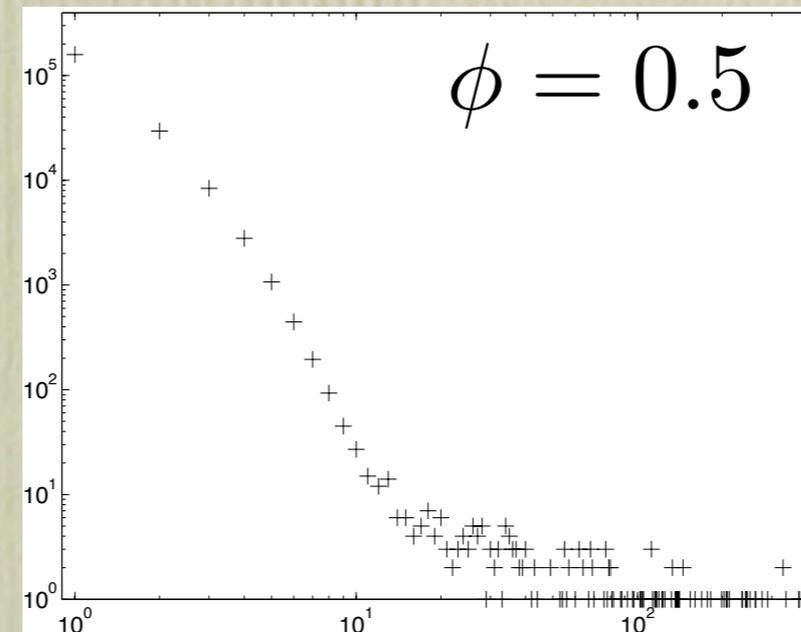
$\phi = 0.1$



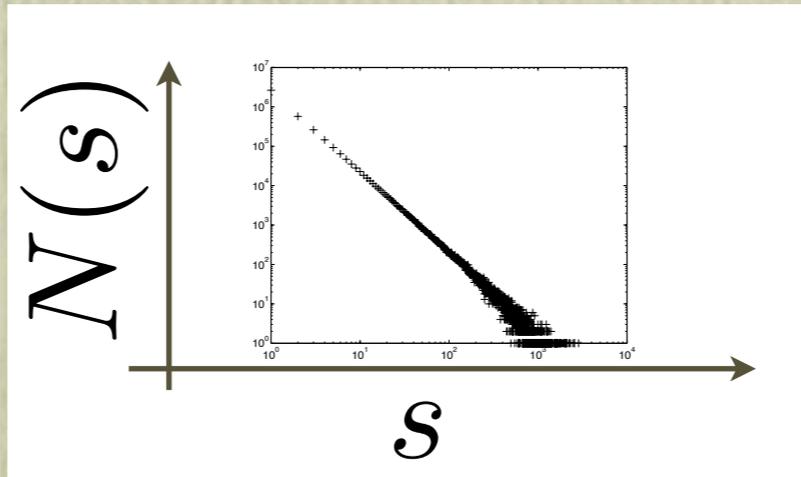
$\phi = 0.3$



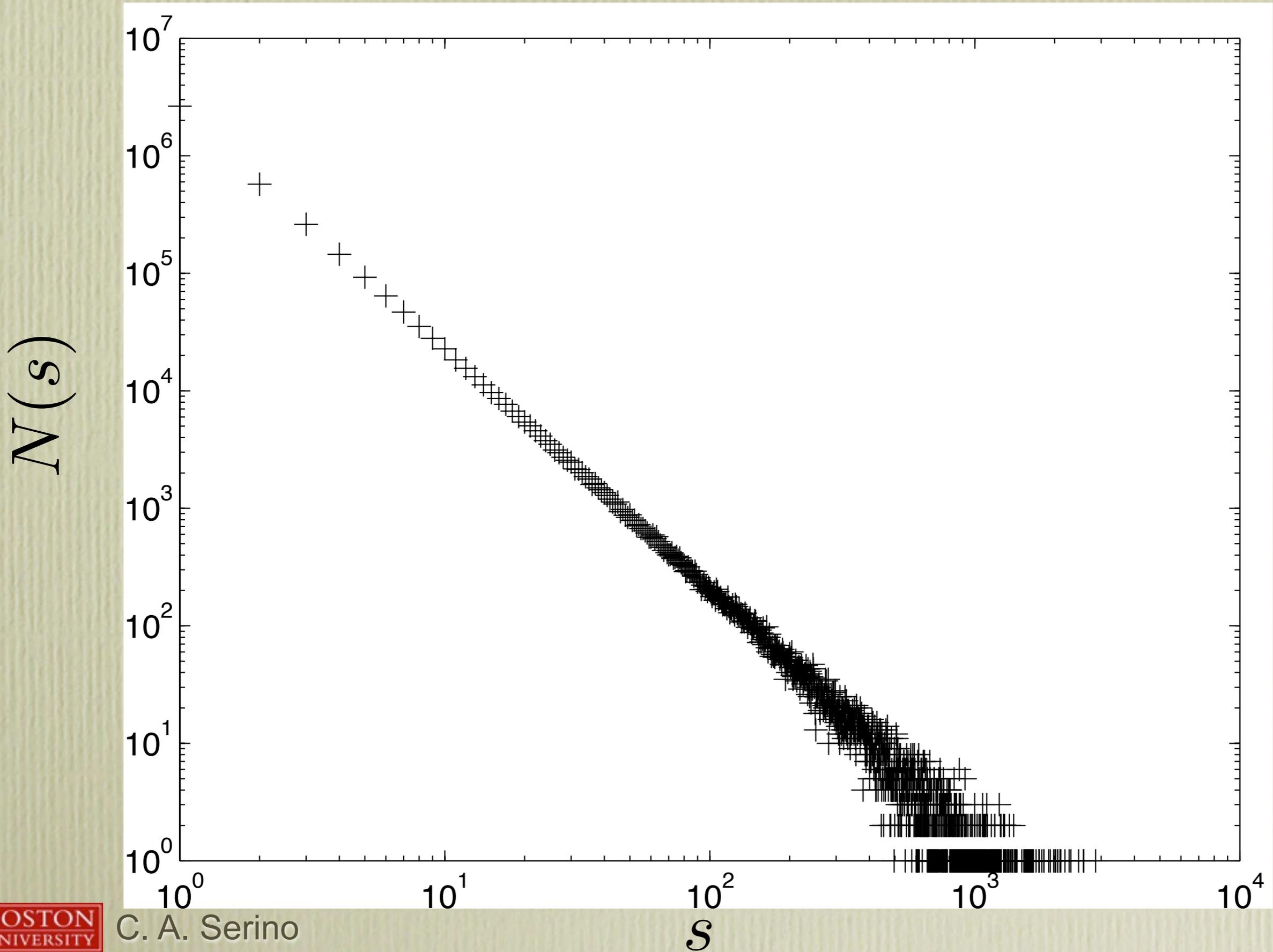
$\phi = 0.4$



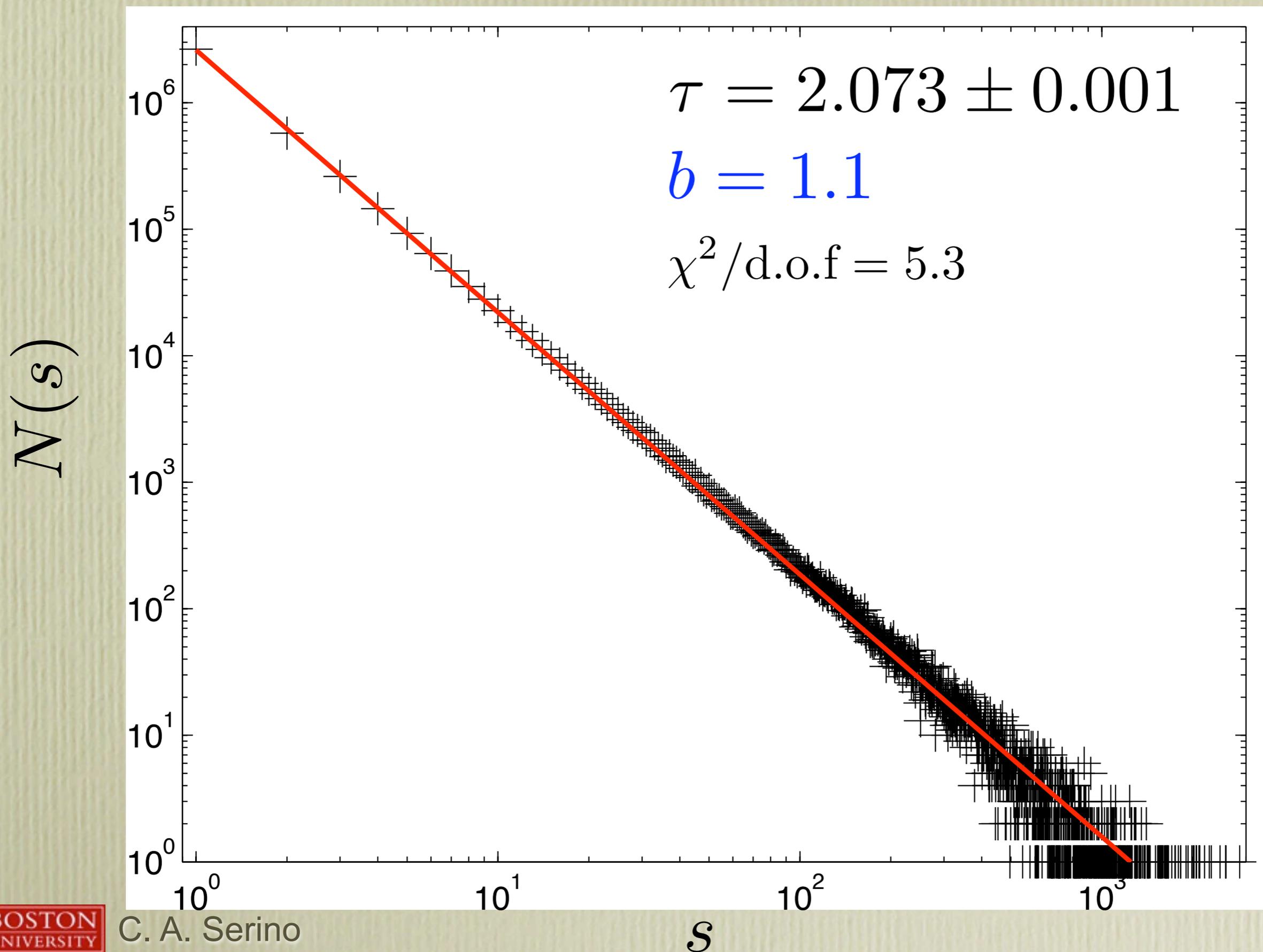
$\phi = 0.9$



# “New” Scaling



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# Summary

- Seismologists have observed that the frequency of earthquakes scales as a **power-law** with respect to the size or magnitude of the event.
- Empirical evidence suggests that most **exponents**,  $b$ , lie in a small window about  $b = 1$ .
- The **OFC** model gives rise to scaling with  $b = 0.5$ .
- The **modified OFC** model with damage produces new scaling with exponent  $b = 1$ .

# Thank You

Further information:

C. A. Serino *et. al.* arXiv:0905.3860 [cond-mat.stat-mech]

