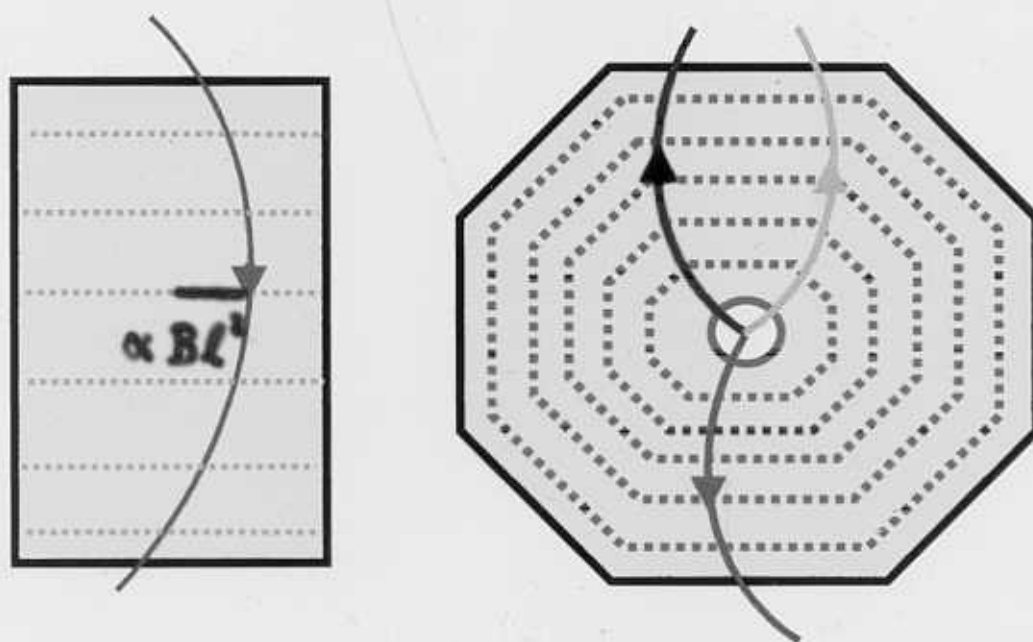




# Large Tracking Detectors

Yet with some accuracy



**Principle of measurement**

**Drift chambers in general**

**Drift detectors**

**Past**

**Present**

**Future**

**Ulrich Becker, MIT**

New England Particle Physics Student Retreat

North Woodstock, New Hampshire

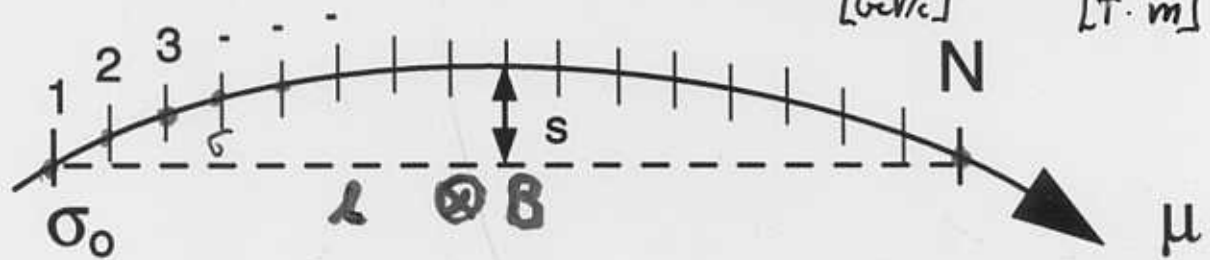
Aug. 18-23, 2002

# WHY? $\vec{p}$ from curvature $\rho$ in $\vec{B}_\perp$

$$p \sin \lambda = 0.3 B \cdot \rho$$

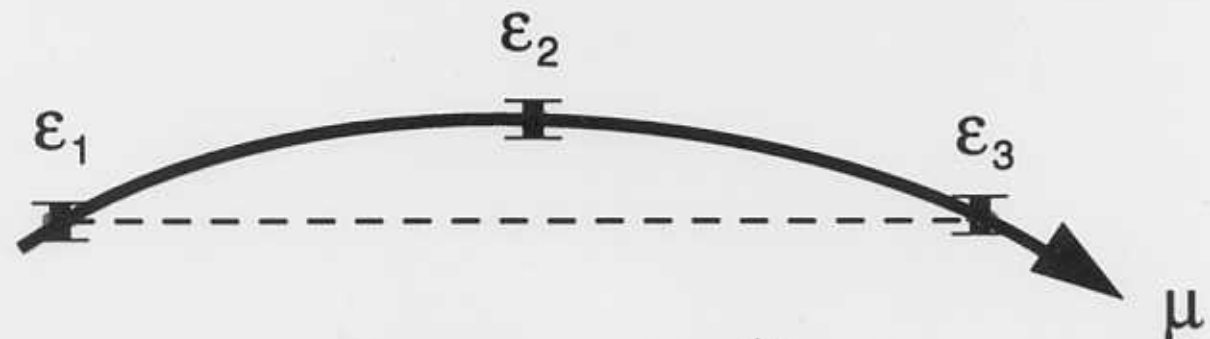
[GeV/c]                      [T · m]

a)



$$\frac{\Delta p_\perp}{p_\perp} = \frac{\Delta s}{s} = \frac{p_\perp \delta}{.3 B \ell^2} \sqrt{\frac{720}{N+5}}$$

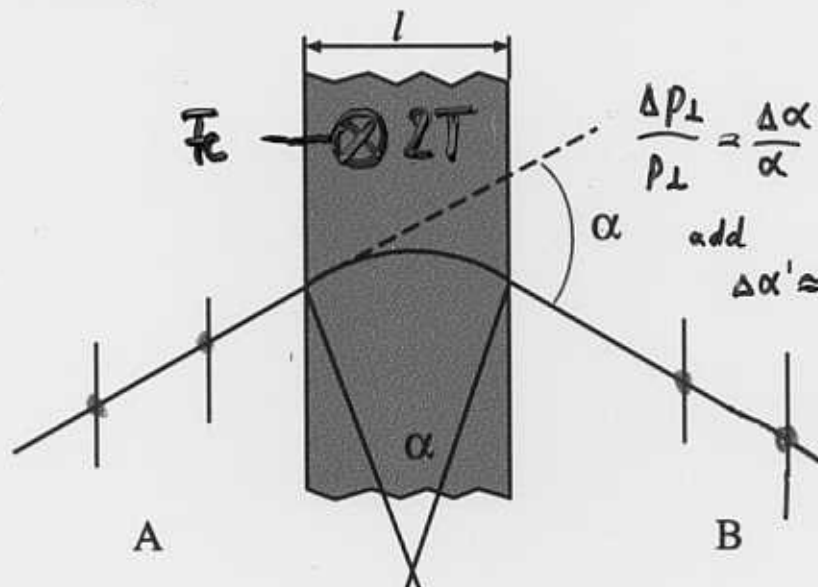
b)



$$\frac{\Delta p_\perp}{p_\perp} = \frac{p_\perp}{.3 B \ell^2} \sqrt{\left(\frac{\epsilon_1}{2}\right)^2 + \epsilon_2^2 + \left(\frac{\epsilon_3}{2}\right)^2}$$

$\ell^2 \rightarrow$  large detectors  
many channels

c)



$$\frac{\Delta p_\perp}{p_\perp} \approx \frac{\Delta \alpha}{\alpha}$$

add

$$\Delta \alpha' \approx \frac{.016}{p X} \sqrt{\frac{X'}{X_0}}$$

for Mult. Scatt.

# $\gamma\gamma$ particle Spectrometer

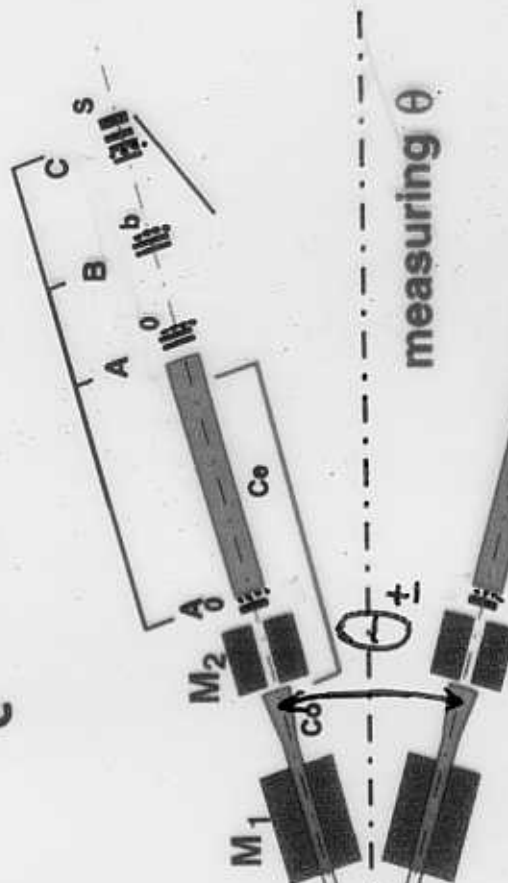
$$L \approx 1036 \frac{1}{\text{cm}^2 \text{s}}$$

$$\frac{P}{e} = 10^{10}$$



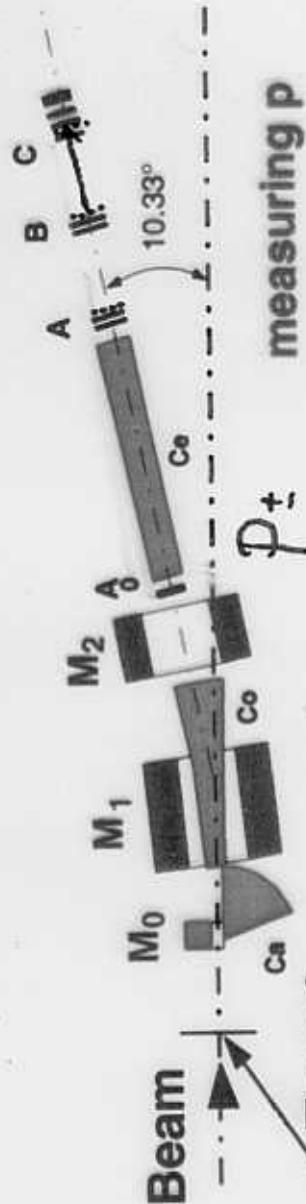
Beam

Target



measuring  $\theta$

MWPC's



measuring  $p$

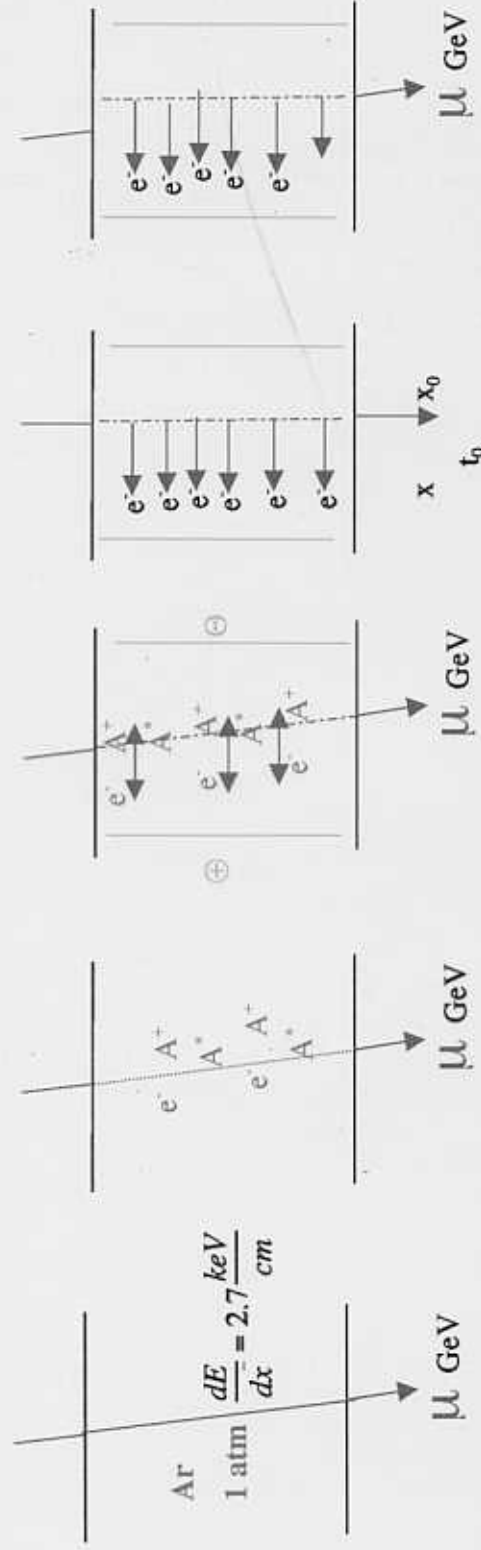
$p_{\pm}$

$$m_{ee}^2 = p_+ p_- (1 - \cos \theta_{+-})$$

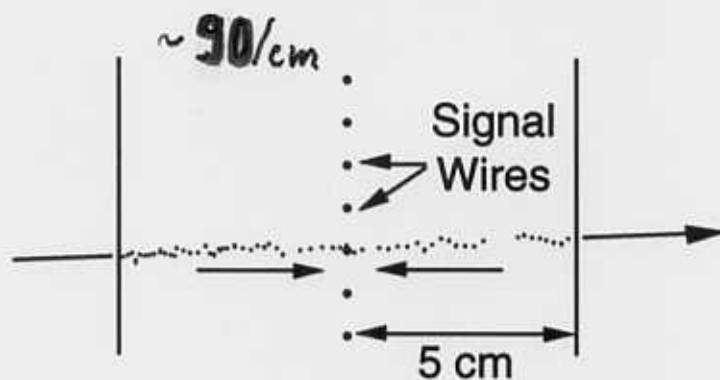
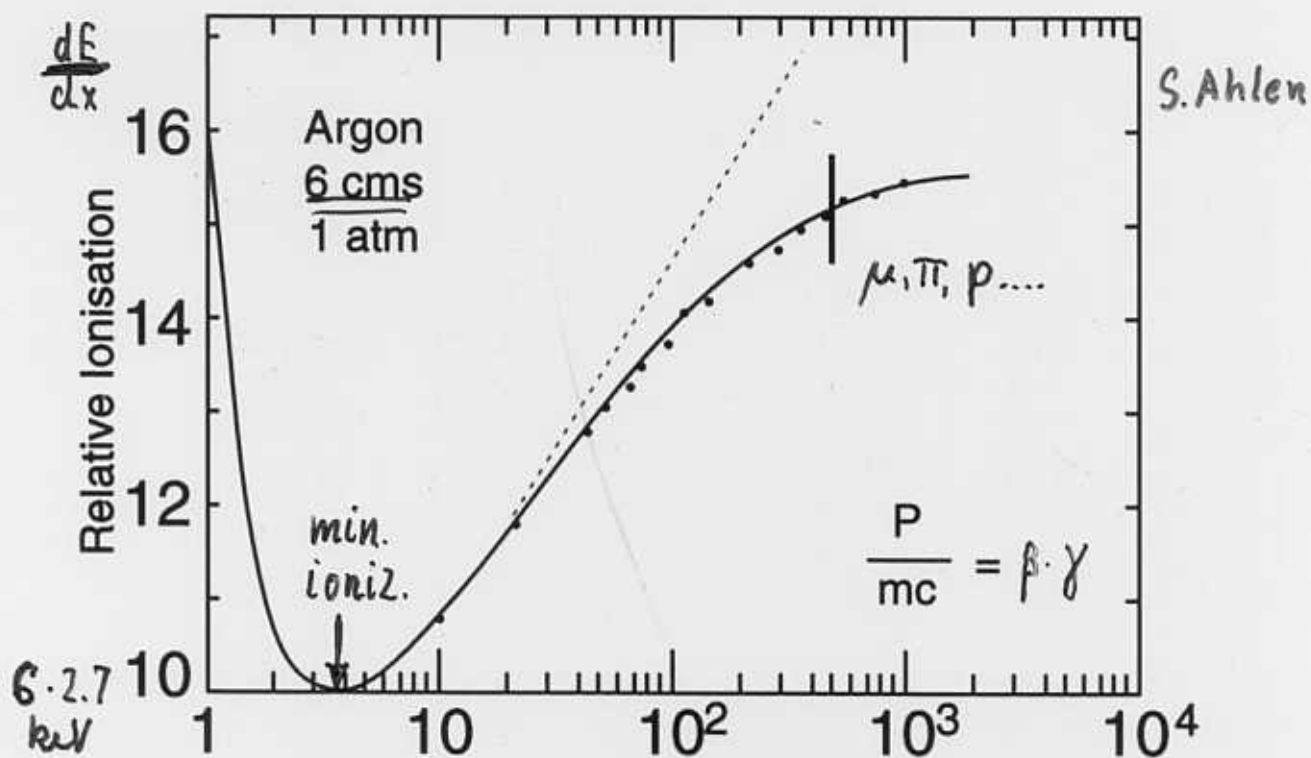


# Ionizing tracks in Drift Chambers: How does it work?

Let a min.ionizing Particle traverse gas

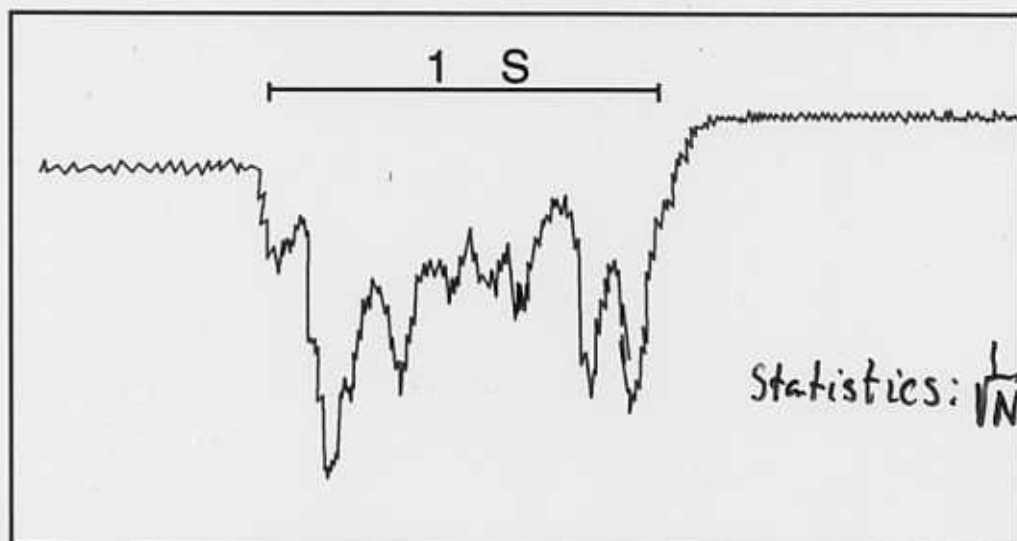


|                                                                 |                                                                |                                                           |                                                                |                                                             |
|-----------------------------------------------------------------|----------------------------------------------------------------|-----------------------------------------------------------|----------------------------------------------------------------|-------------------------------------------------------------|
| Noble Gas<br>so that $e^-$ are<br>NOT attached<br>To gas molec. | $E_{ion}(Ar)=15.8eV$<br>+ inel.collisions<br>$E_{eff} = 33 eV$ | $\sim 30 e^-/cm$<br>separated<br>by E-field<br>$A^+$ slow | $x-x_0=v_D(t-t_0)$<br>t known<br>pos.meas.<br>$\sim 150 \mu m$ | diffusion<br>smears<br>$\sigma=200\mu\sqrt{x(cm)}$<br>1 atm |
|-----------------------------------------------------------------|----------------------------------------------------------------|-----------------------------------------------------------|----------------------------------------------------------------|-------------------------------------------------------------|



but  $\sim 25$  clusters of 1, 2, ... 15e<sup>-</sup>

$P(n)$  exp



## Drift Velocity

$V(e^-) \gg V_D$  "Drift velocity"



$e^-$  suffer  $dn$  random collisions in  $dx$ :

$$dn = \frac{1}{v\tau} dx$$

Note:  $v\tau$  = meanfree path

Collision rate  $1/\tau \propto$  to gas density  $N$ :

$$\frac{1}{\tau} = N\sigma v$$

$\vec{E}$  accelerates between collisions:

$$eE = m \frac{dv}{dt}$$

Causing a displacement of:

$$x(t) = \frac{1}{2} \frac{e}{m} Et^2$$

Prob. for time intervals between coll.

$$dP = \frac{1}{\tau} e^{-t/\tau} dt$$

Average path:

$$\langle x \rangle = \int_0^{\infty} \frac{1}{2} \frac{e}{m} Et^2 \frac{1}{\tau} e^{-t/\tau} dt = \frac{e}{m} E\tau^2$$

Average drift Velocity:

$$\langle v \rangle = v_D = \frac{\langle x \rangle}{\tau} = \frac{e}{m} \tau \stackrel{\text{def}}{=} \mu E$$

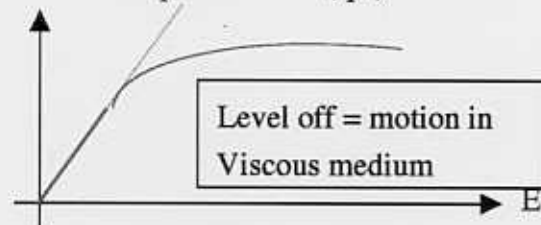
$\mu$  is called the 'mobility'

But  $\tau$  depends on density:

$$v_D = \mu E \frac{p_0}{p} = \mu \cdot p_0 \left( \frac{E}{p} \right),$$

"E/p Scaling"

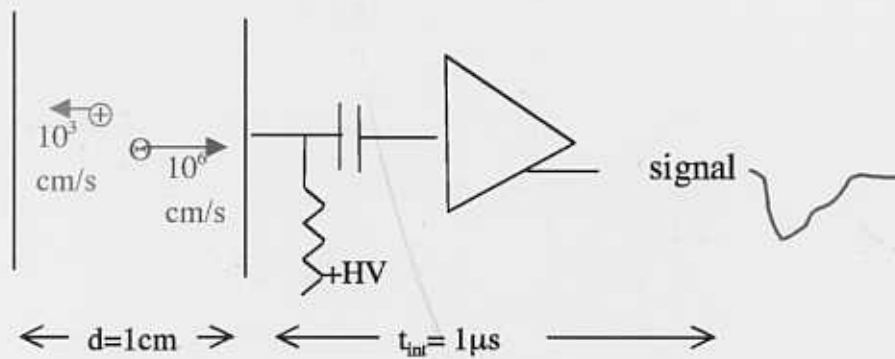
So far:



But  $\sigma$  and there fore  $\tau$  depend on the energy of the electron:

**important for drift chambers**

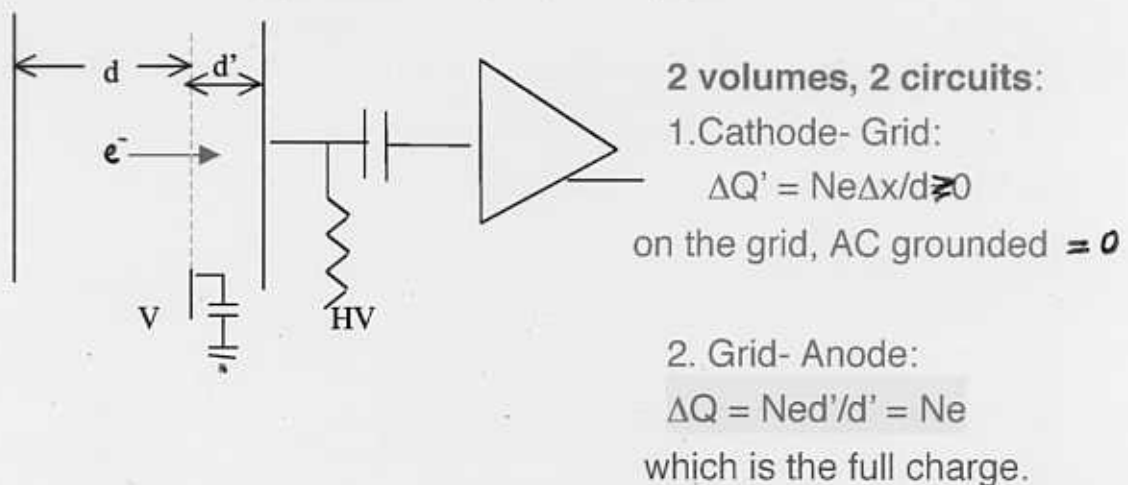
# Signal Basic Example I



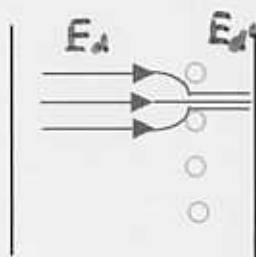
During the integration time charges move:  $\Delta x = v t_{\text{int}} = \begin{cases} 1\text{cm for } e^- \\ 10^{-3}\text{cm for } A^+ \end{cases}$

...the moving  $A^+$  induce:  $\Delta Q = n \Delta x/d = 10^{-3} n$

but the induced charges  $q$  depend on the position:  $0 < q < Ne$ , which can be avoided by introducing a (Frisch) grid



Can the grid be very transparent??



YES!

if  $E_{d'} \geq 3 E_d$  98% get through

Program: Maxwell Garfield...

## Drift Velocity of IONS

$$v^+ = \mu^+ E p/p_0$$

Ions are heavy, have large  $\sigma \rightarrow$  the mobility  $\mu^+ \approx \text{const.}$ , small

|                                              |                                                 |                            |
|----------------------------------------------|-------------------------------------------------|----------------------------|
| He <sup>+</sup>                              | in He                                           | 10.2 cm <sup>2</sup> /(Vs) |
| A <sup>+</sup>                               | in A                                            | 1.7                        |
| iC <sub>4</sub> H <sub>10</sub> <sup>+</sup> | in iC <sub>4</sub> H <sub>10</sub> <sup>+</sup> | 0.61                       |
| CO <sub>2</sub> <sup>+</sup>                 | in A                                            | 1.1                        |
| CH <sub>4</sub> <sup>+</sup>                 | in A                                            | 1.87                       |

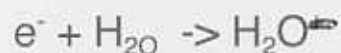
multiply by a typical drift field of 1KV/cm to get a typical ion velocity

$$v^+ \approx 10^3 \text{ cm/s,}$$

small compared to electrons  $v=v_D \approx 5 \cdot 10^6 \text{ cm/s} = 5 \text{ cm}/\mu\text{s}$

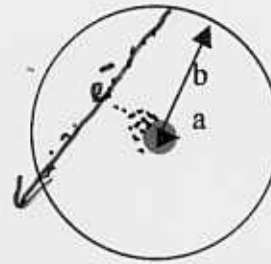
The slow drifting ions can be neglected for signal formation in the integration time of 1  $\mu\text{s}$ . However, they will affect the rate capability by charging up the gas volume. Worst; TPC's. Best are straws of 4mm diameter; still ok at rates  $>10^7/\text{s}$ ..

Attachment (R.Dinner, MIT BS thesis 2001) converts fast electrons to slow ions, useless for signals in 1  $\mu\text{s}$ .



**Air (O<sub>2</sub> not N<sub>2</sub>) is bad for you!**

## Signal Example II induced on the Wire



Potential  $\phi \propto \ln(r)/\ln(b/a)$

electrons  $\phi_{elec} = -Ne(\phi(a) - \phi(r)) = -Ne \ln(r/a)/\ln(b/a)$

ions  $\phi_{ion} = Ne(\phi(b) - \phi(r)) = Ne \ln(b/r)/\ln(b/a)$

The electron avalanche starts, when the field is high enough:

$e E_{crit} \lambda > 30 \text{ eV}$ . then  $r \approx 3a$ ,  $\ln(r/a) = 1.1$

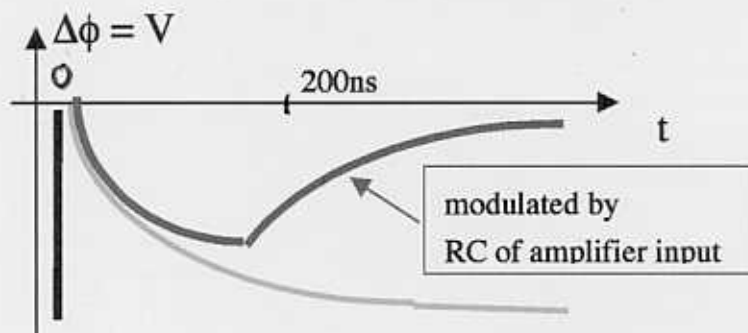
For the  $A^+$  ions  $b/r \approx 1000$   $\ln(b/r) = 7$

**SURPRISE !!** The signal comes from  
the mirror charges of the ions



Of course the  $e^-$  current is much higher (peaked), but only lasts

$50 \mu\text{m}/50\text{mm}/\mu\text{s} = 1\text{ns}$ , which normal amplifiers cannot follow. So the electronic voltage signal is dominated by the avalanche ions (not ionization) slowly drifting away.



## Basic Example III

## Prop Tubes & Chambers

At high  $\vec{E}$ ,  $N$  electrons drifting along  $x$  ionize secondaries off the gas molecules. These amplify the signal causing a "Gas Gain"  $G$ .

Townsend coeff.: secondaries in  $dx$ :  
and consequently

$$dN = \alpha(E) N dx$$

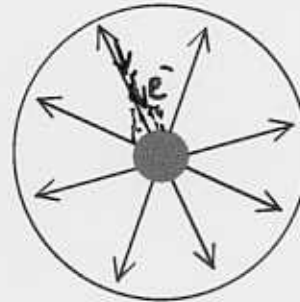
$$G = N/N_0 = e^{\alpha(E)\Delta x}$$



For a 'Geiger Geometry'

$$E(r) = \frac{V}{\ln(b/a)} \frac{1}{r}$$

The avalanche starts, when  
 $eE\lambda \approx 33\text{eV}$  or  $E_{\text{crit}} \approx 40 \text{ KV/cm}$



This is close to the wire:  $r_{\text{crit}} = \frac{V}{\ln(b/a) E_{\text{crit}}} \approx 3a$  typically

No grid is needed, since Amplif. volume =  $10^{-6}$  gas volume

Gain =  $N/N_0$

$$\int dN = N_0 \int_{r_{\text{crit}}}^a \alpha(r) dr$$

But  $\alpha$  depends on  $\vec{E}$

$$\ln G = \int_{r_{\text{crit}}}^a \alpha(r) dr = \int_{E_{\text{crit}}}^{E(a)} \alpha(E) \frac{dr}{dE} dE$$

Diethorn approximation:  $\alpha \approx \beta \frac{\vec{E}}{|\vec{E}|} p/p_0 = \ln 2 / \Delta V * E p/p_0$

**SOLUTION**

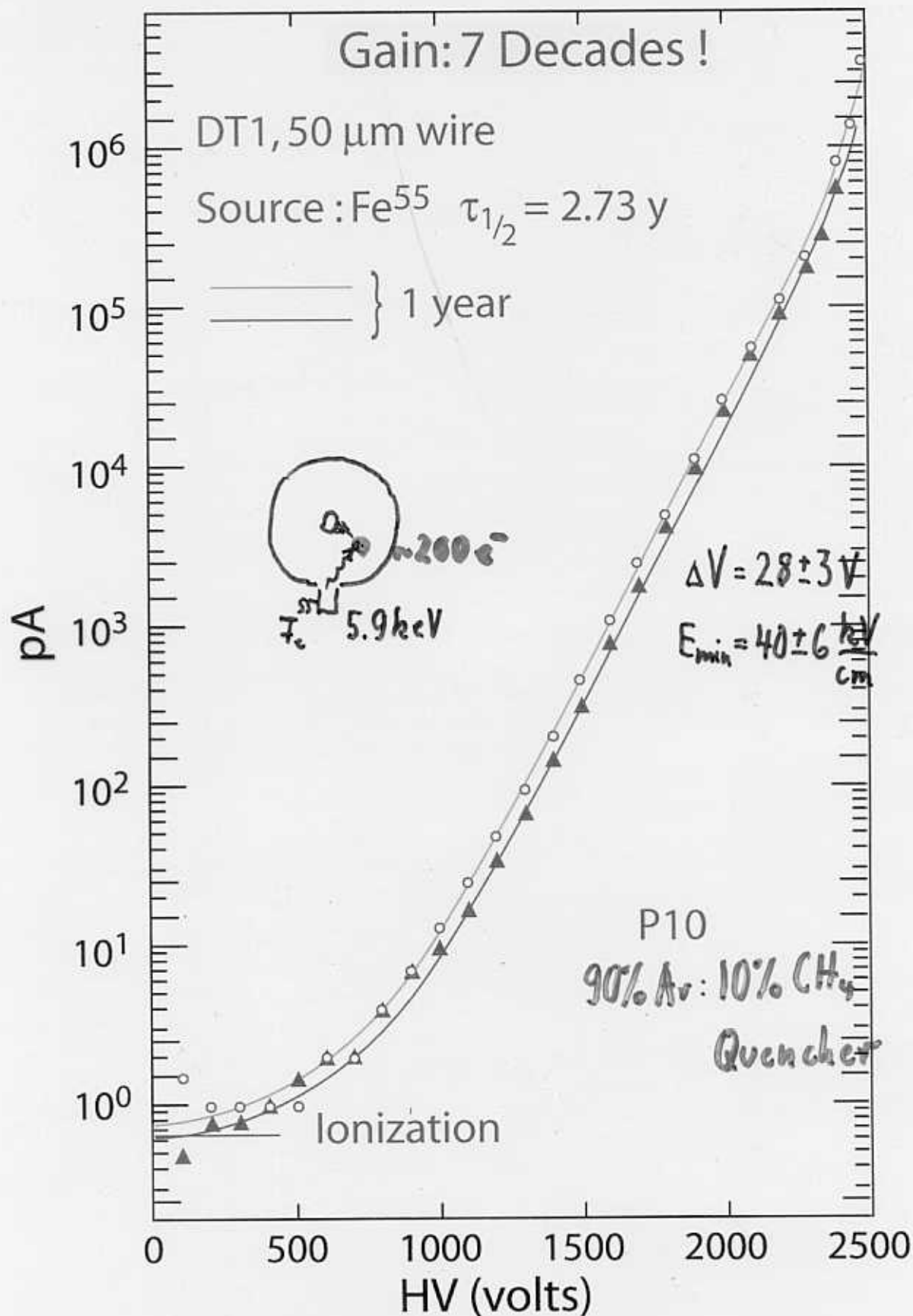
$$\ln G = \frac{\ln 2}{\Delta V} \frac{V}{\ln b/a} \ln \left\{ \frac{V}{\ln b/a E_{\text{crit}}(r_{\text{crit}}, p) \cdot a \cdot (p/p_0)} \right\}$$

where  $\Delta V \approx 33\text{V}$  is the effective ionization potential

$V$  the applied voltage,  $p_0$  the reference pressure,

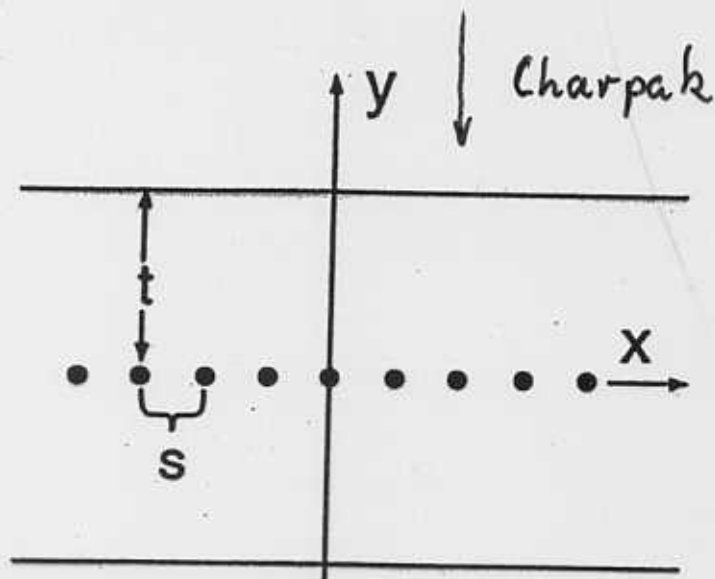
$E_{\text{crit}}(r, p)$  field where avalanche starts

# World record

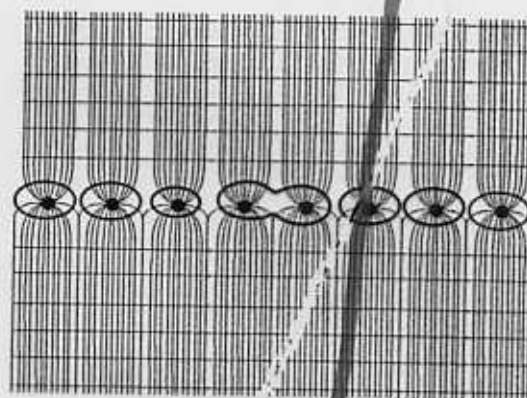


# PROPORTIONAL CHAMBERS

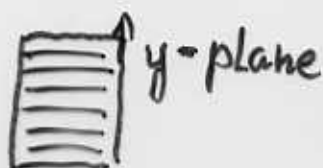
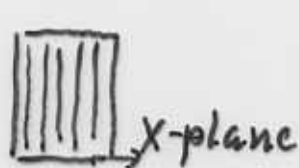
○○○○○○○○○○ N\* Geiger



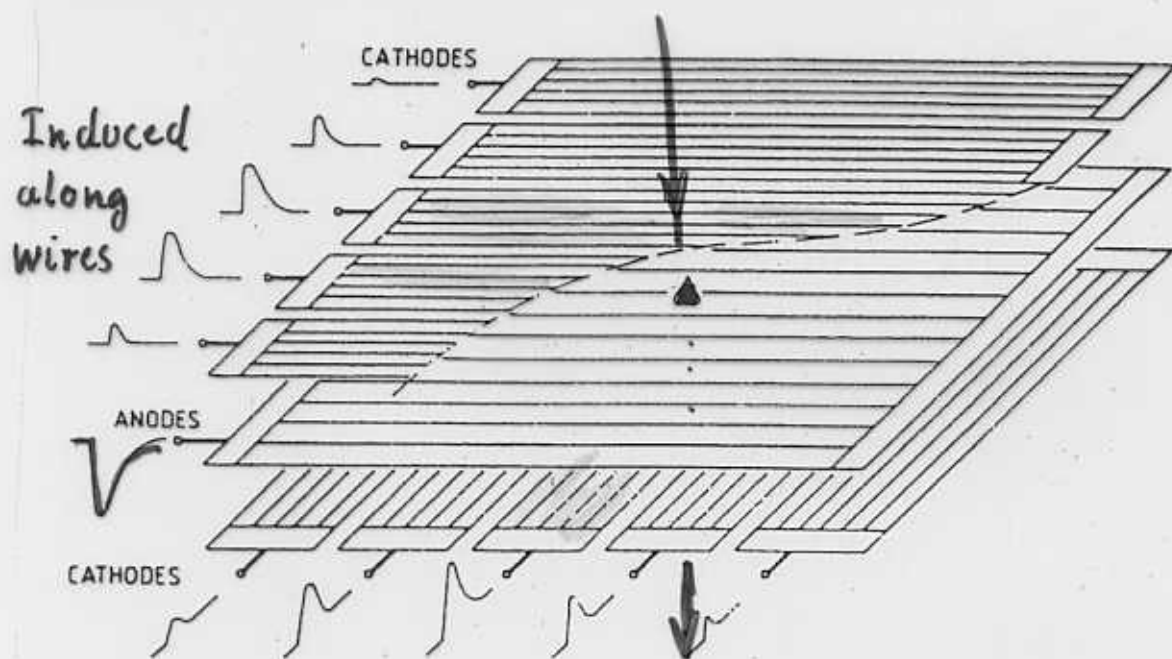
Sauli, CERN



$\frac{2 \text{ mm resol.}}{\sqrt{2}}$



OR



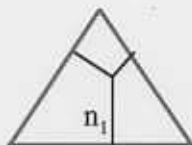
X-y Cathode Strip Readout

(from Charpak)

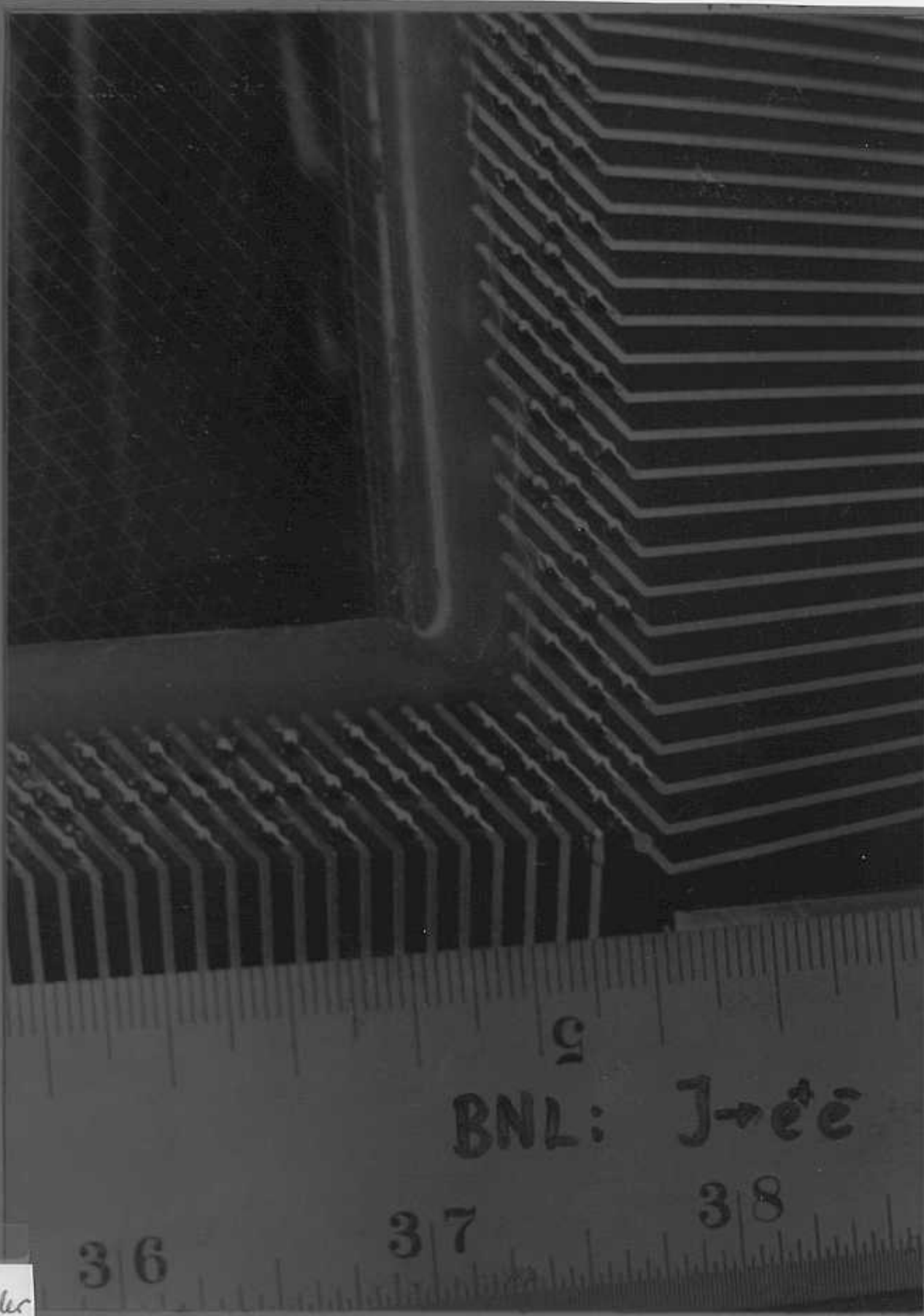
# M<sub>ulti</sub> W<sub>ire</sub> P<sub>rop.</sub> C<sub>hambers</sub> -BNL 598 J-Exp.

3 planes:

2mm

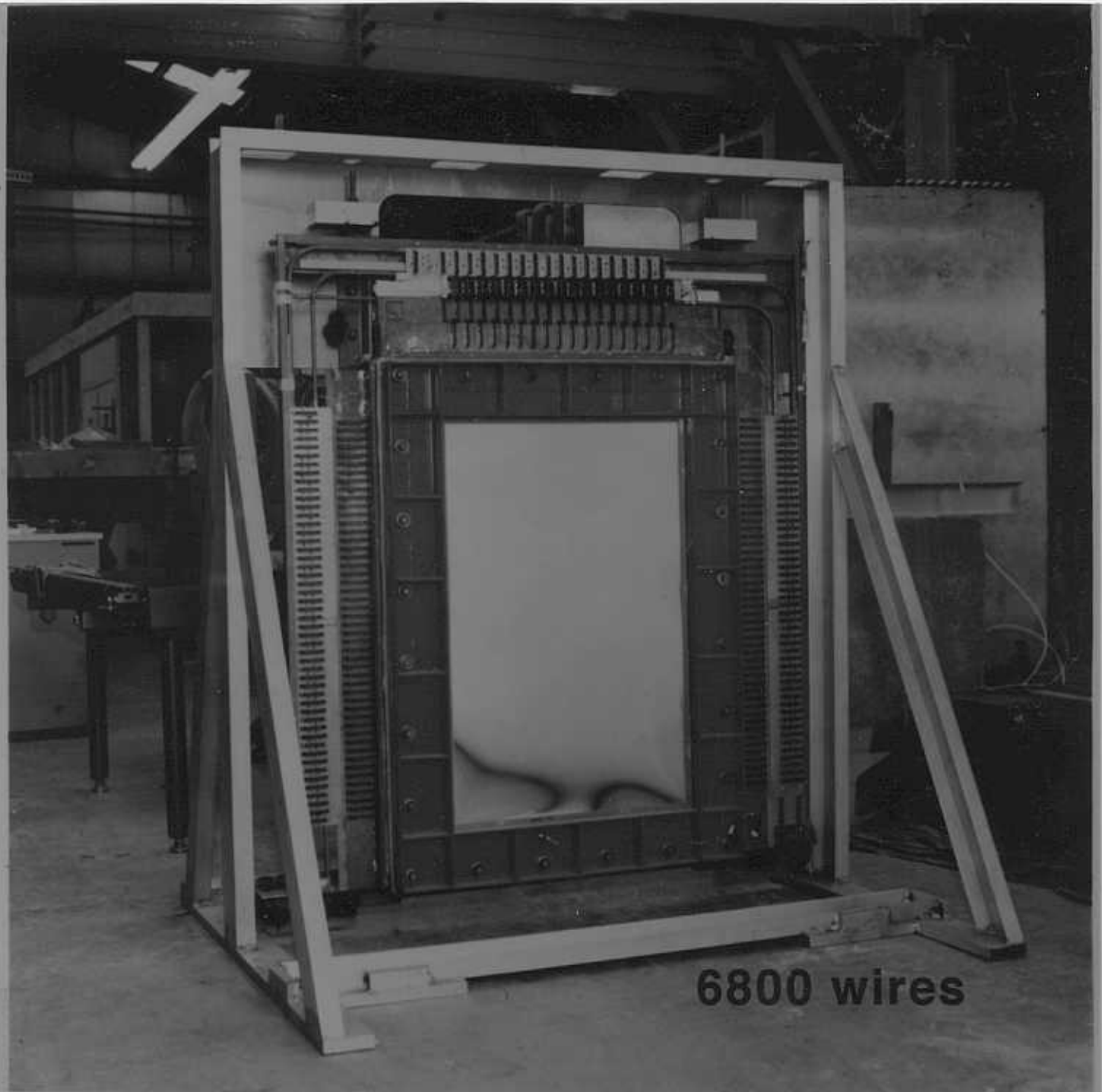


$$n_1 + n_2 + n_3 = \text{const}$$

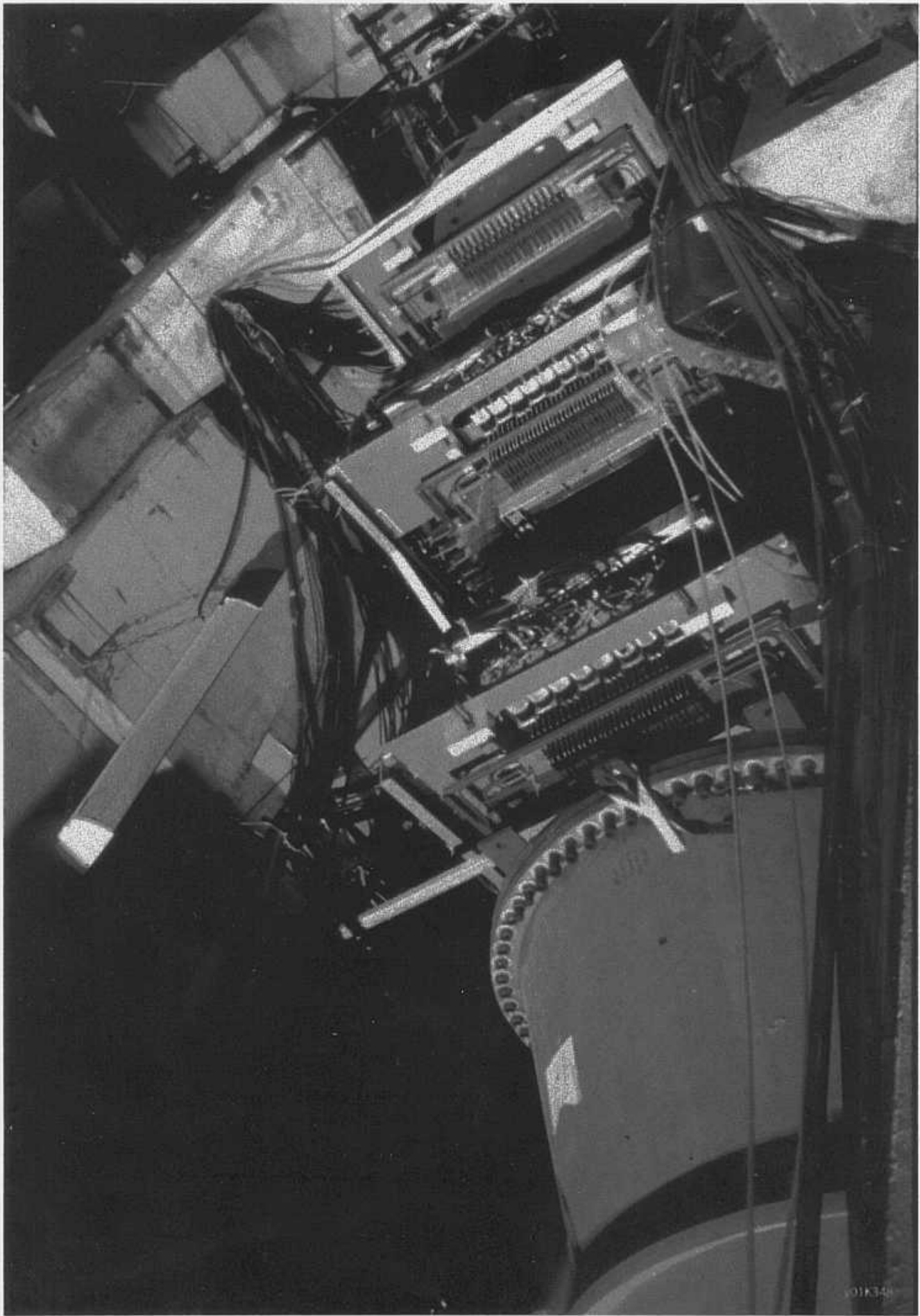


glue + solder

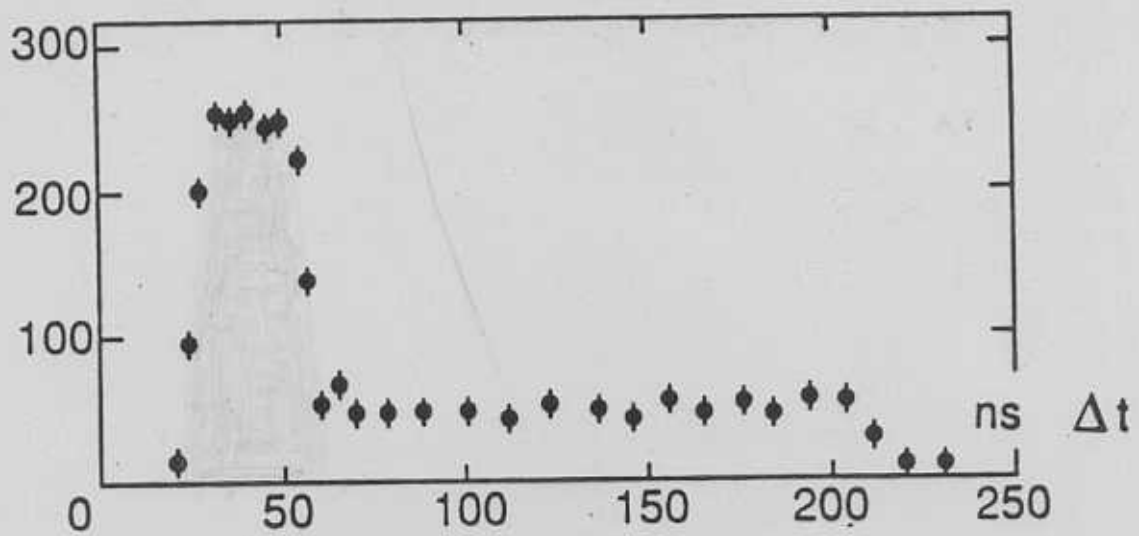
**but AGS...  $L = 10^{36} \text{ cm}^{-2} \text{ s}^{-1}$  Ageing!**  
**Argon-Methylal -> No Ageing!**



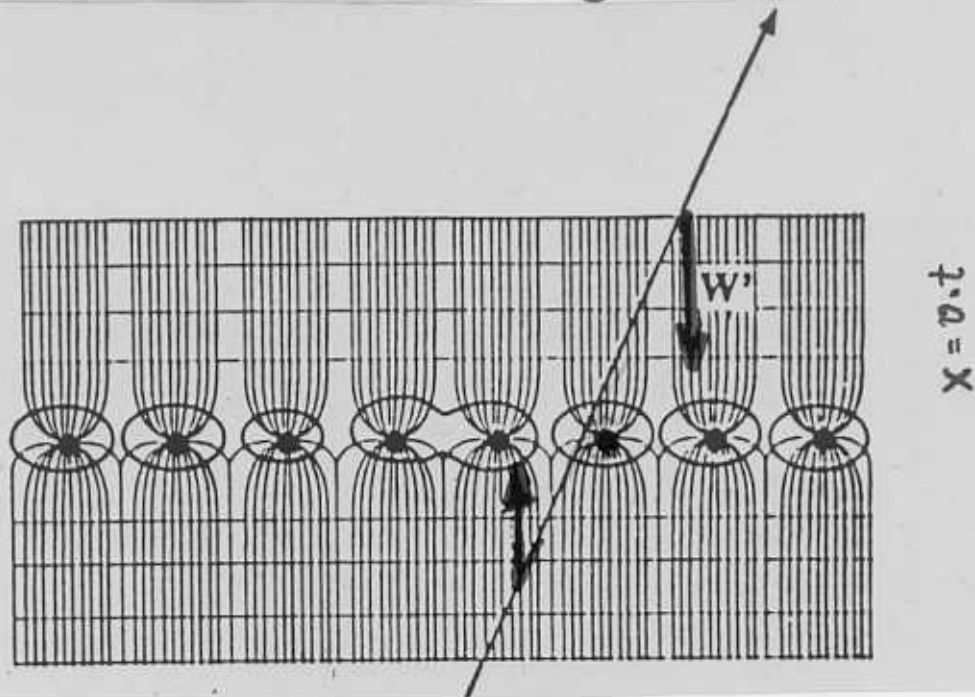
**2 Chambers->  $\Upsilon$  - FNAL**  
**1 Chamber -> Smithsonian**



**100% eff. But why a tail?**



**Neighbour wires fire, too, but later  
ionization 'drifts' along E- lines**



**⇒ missed invention of Drift Chamber**

# A Word on Wirology

See U.Becker "large Area and Muon Detectors" in World Scientific  
Instrumentation in High Energy Physics (1992),p513-

## Mechanical stuff

Parallel to earth all wires sag:

$$z = \frac{\mu g x^2}{T} \frac{1}{2}$$

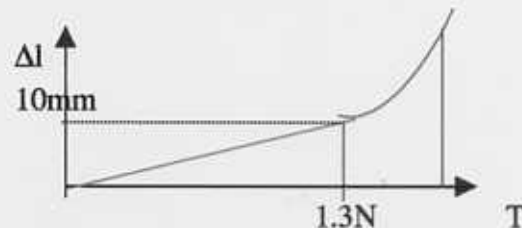
A Tungsten-Rhenium wire of 30  $\mu\text{m}$  dia.  
(4% Au plated) has 0.138 mg/cm and can be  
elastically stretched to 1.3N. For  $l=3\text{m}$  the sag is:

$$z_{\text{max}} = 117 \mu\text{m}$$

Sag or tension is easily verified by the resonance  
frequency. Putting AC between wire and a plate

$$v = \frac{1}{2l} \sqrt{\frac{T}{\mu}} = \frac{1}{4} \sqrt{\frac{g}{2z_{\text{max}}}}$$

Tungsten-Rhenium is the best wire  
material:  $\phi 30 \mu\text{m}$



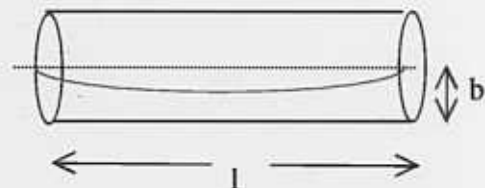
## Electrostatic Stability

*a 'sagged'*

Putting a Voltage on ~~the~~ wire in a coaxial  
Arrangement, makes ~~it~~ worse. It will touch

The wall at  $U_{\text{max}} = 1.43 \left[ \frac{V^2}{gr} \right] \sqrt{T} \frac{b}{l} \ln \frac{b}{a}$

The elstat, displacement grows with  $\text{init.} \delta^2$ !



Wire planes get unstable by the degeneracy:

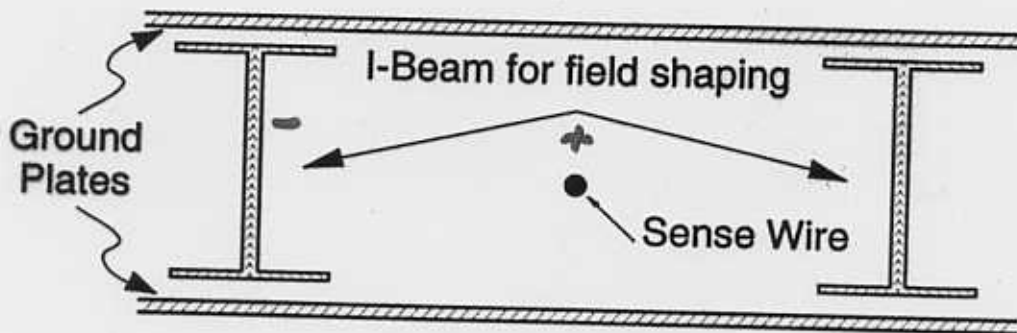
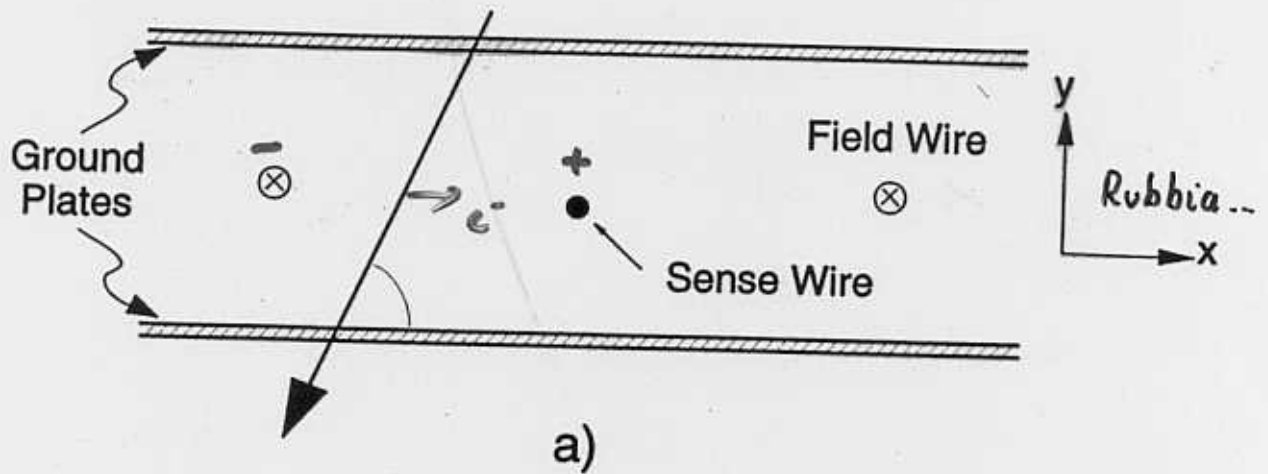
Typically for dia.=20 $\mu\text{m}$  wires at 60 g and 2.4kV

$$l \leq 80 \text{ cm}$$

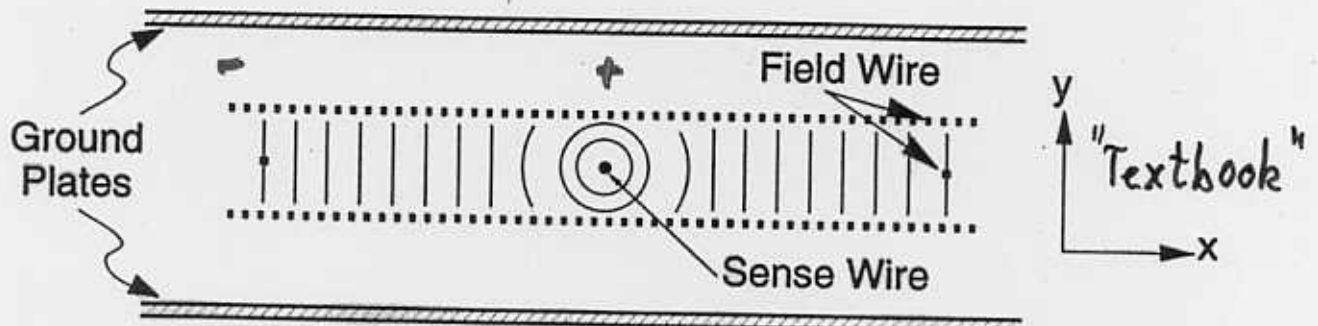
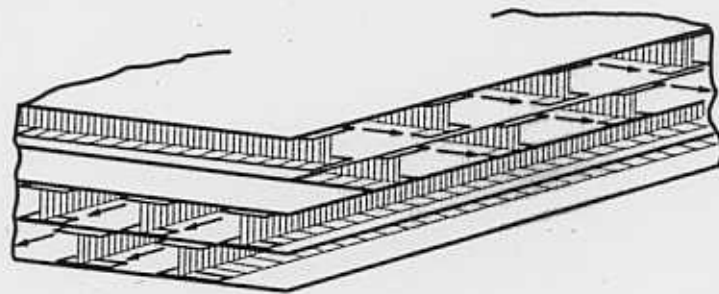


# DRIFT CHAMBERS

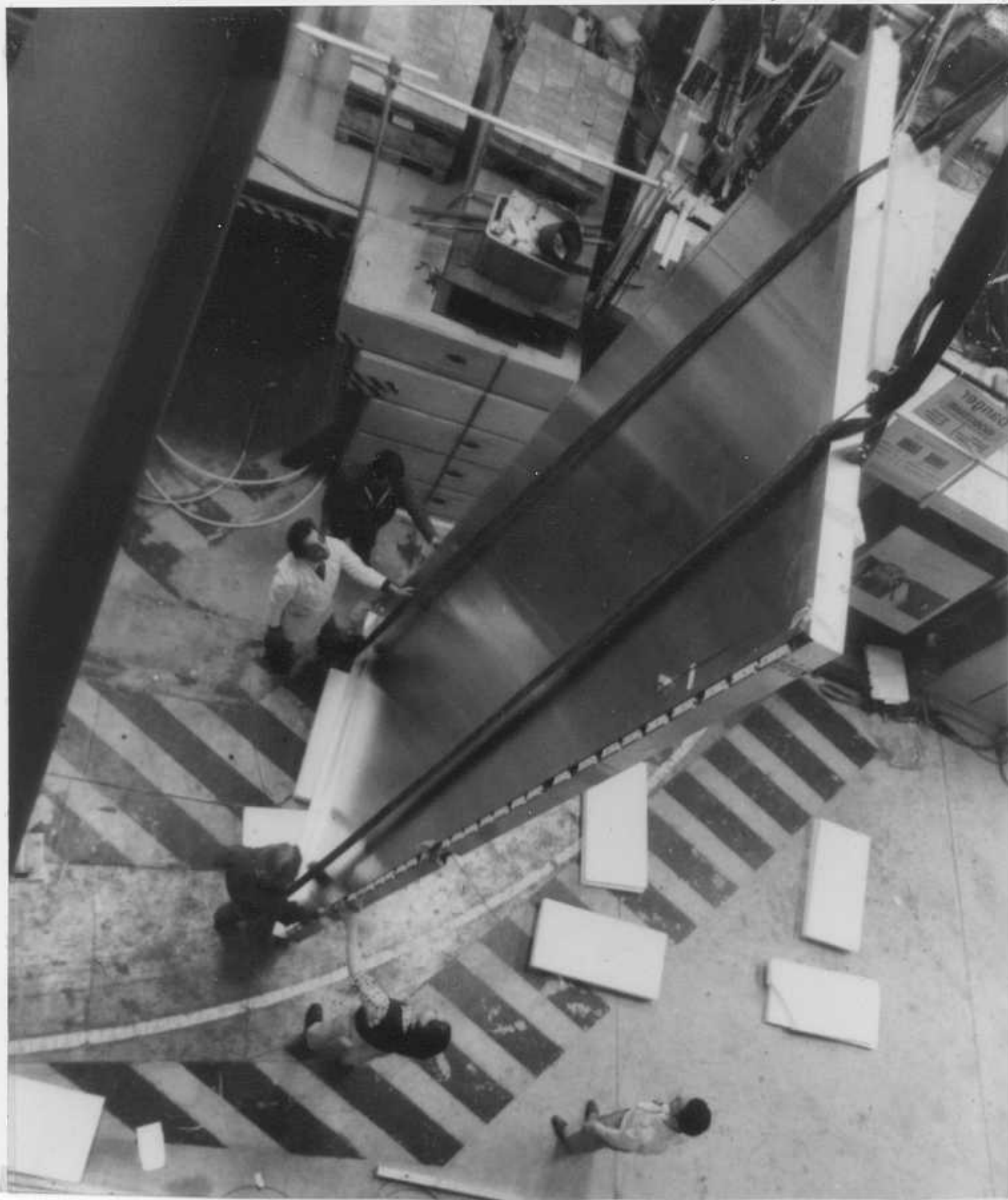
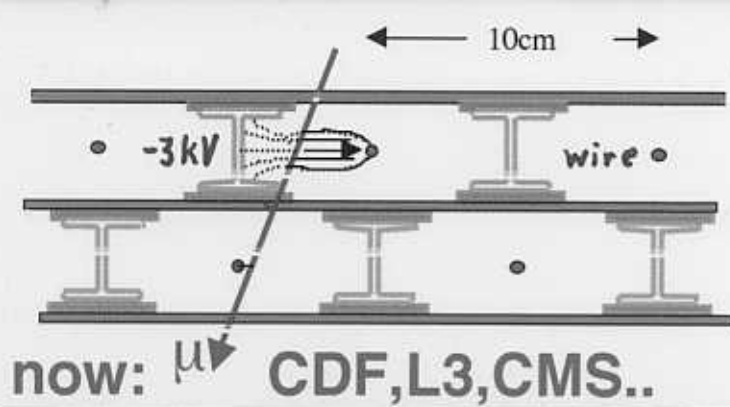
Instead 1 wire / 2 mm  $\rightarrow$  1 wire / 10 cm  $\rightarrow$  large coverage!



Becker 75  
CDF 85  
CMS 00



**New Design**  
**I - Chamber**  
**6m mechanical**  
**& Fieldshaping**  
**ISR,PETRA**



## Recall E & M

Charges (e) follow field line of E

- Metals are equipotentials  $\phi = \text{const}$

- 
- 

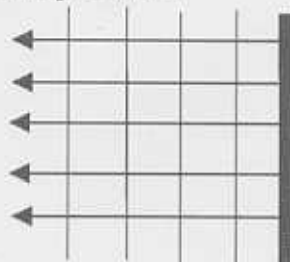
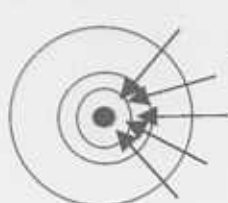
wire



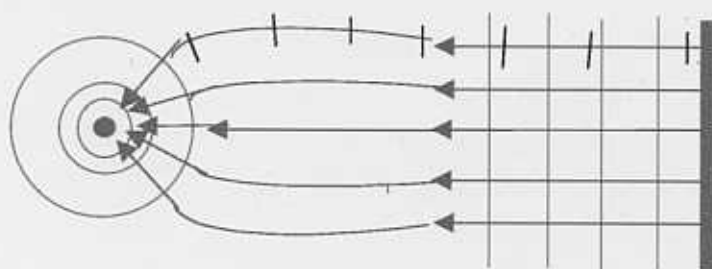
plate



- $E = - \text{grad } \phi$
- Superposition valid at all points



Continuous functions

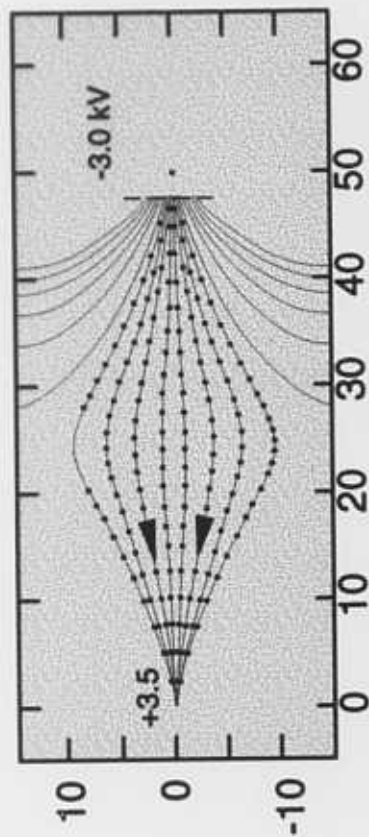


Laplace - Poisson

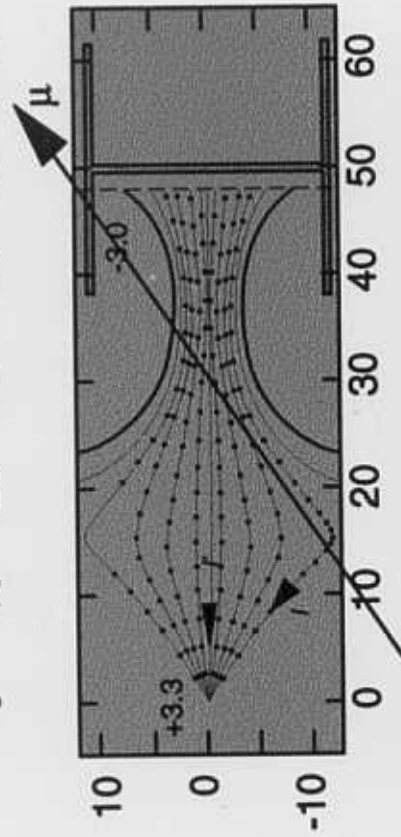
$$\nabla^2 \phi = 0, 4\pi g$$

Programs: Maxwell

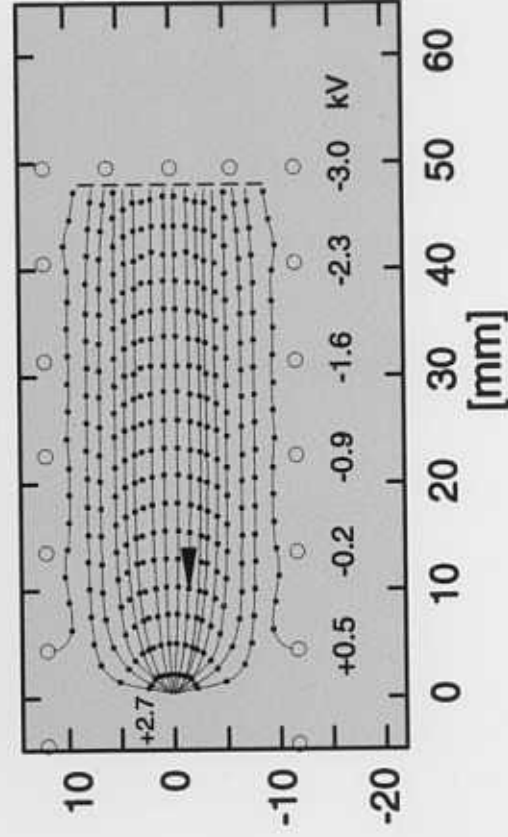
Garfield ....



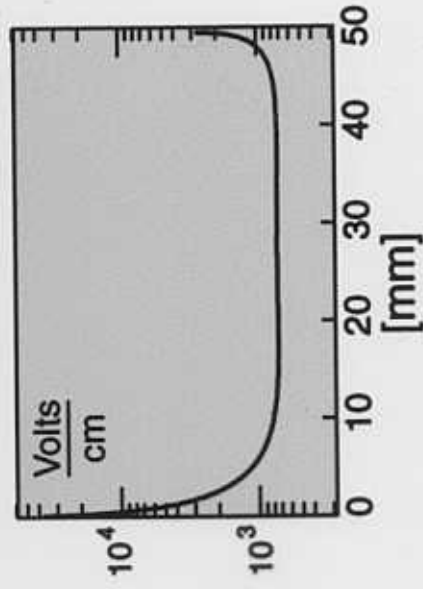
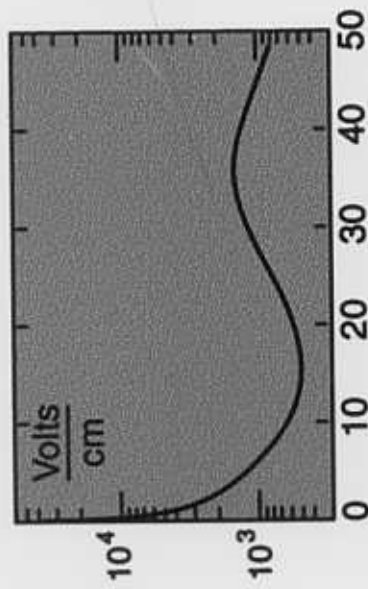
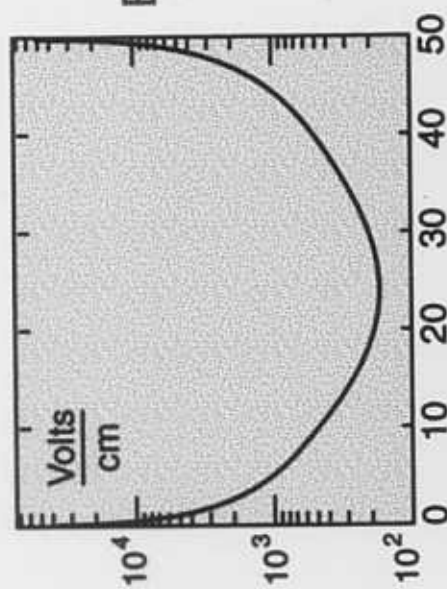
EARLY DRIFT  
Chambers



CLASSICAL  
R209, PETRA, L3  
CDF, UA1, CMS, ...



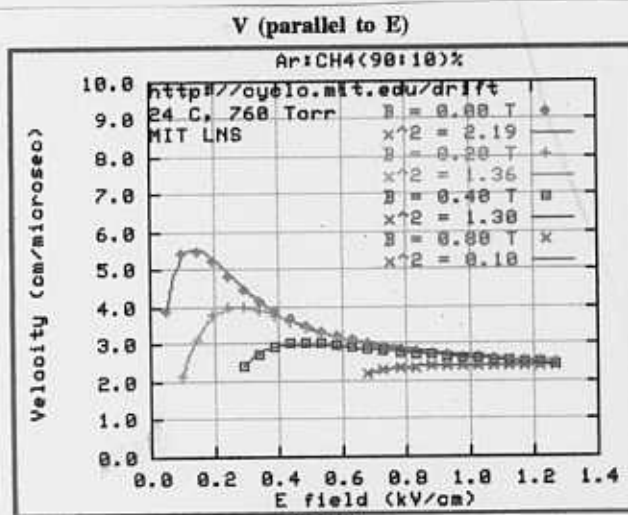
IDEAL  
impractical



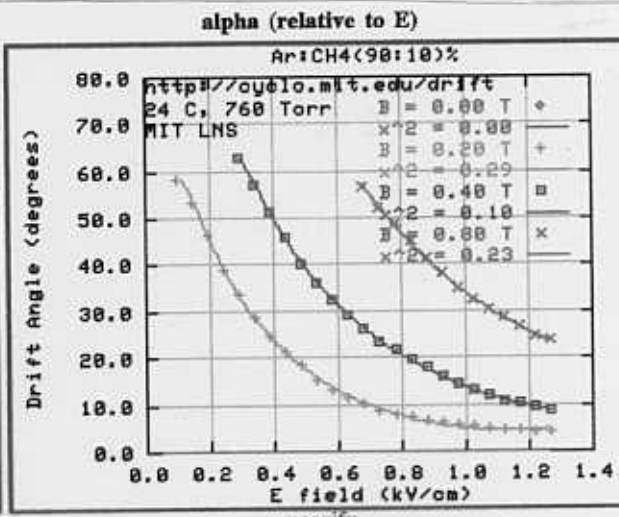
U. Becker in "Instrumentation in High Energy Physics" Ed. Sauli  
World Scientific, Adv. Series, Vol. 9, (1998) 513

# Data you requested from Drift Gas R&D Home Page

If used, please reference: "U. Becker et. al. Gas R&D Home Page (<http://cyclotron.mit.edu/drift>)"



magnify  
Postscript Velocity graph

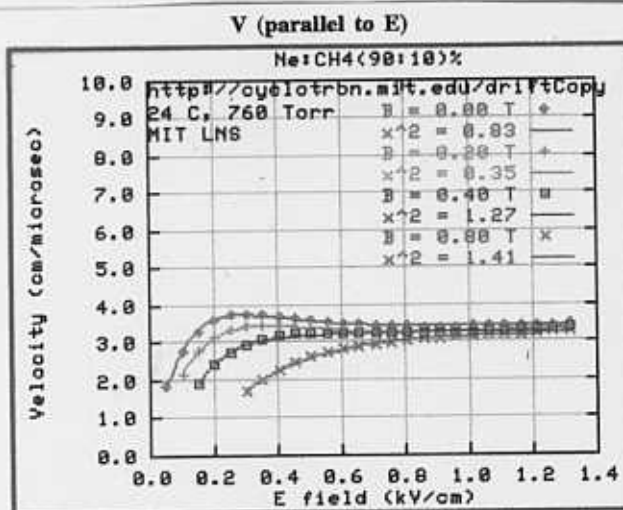


magnify  
Postscript Angle grapha

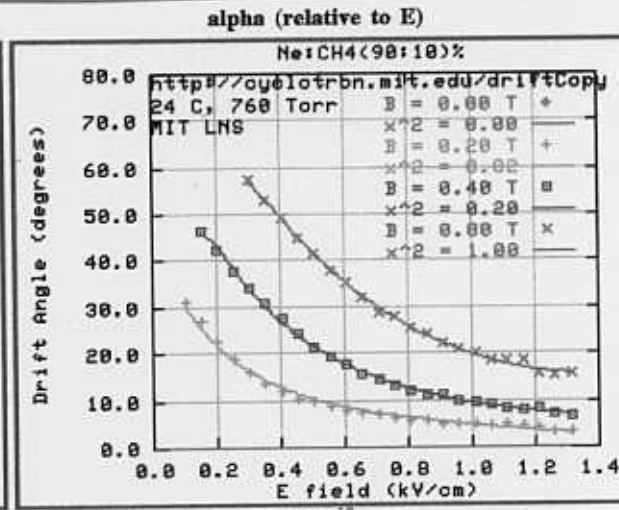
$$V_{||} = U_1(1 - e^{-(E-a_1)/E_1}) + U_2(E-a_1)e^{-(E-a_1+a_2)E_2} + W(E-a_1)$$

$$\sin(\alpha) = V_{||}B / (10^6 E) + P_1 + P_2 E + P_3 E^2$$

| B(T) | U <sub>1</sub> | E <sub>1</sub> | U <sub>2</sub> | E <sub>2</sub> | W      | a <sub>1</sub> | a <sub>2</sub> | X <sup>2</sup> /dof | P <sub>1</sub> | P <sub>2</sub> | P <sub>3</sub> | X <sup>2</sup> /dof |
|------|----------------|----------------|----------------|----------------|--------|----------------|----------------|---------------------|----------------|----------------|----------------|---------------------|
| 0    | 3.523          | 0.10           | 85.932         | 9.80           | -0.834 | 0.000          | 0.000          | 2.19                | 0.000          | 0.000          | 0.000          | 0.000               |
| 0.2  | 2.532          | 0.17           | 35.640         | 5.91           | 0.000  | 0.041          | 0.000          | 1.36                | 0.487          | -0.841         | 0.388          | 0.290               |
| 0.4  | 3.236          | 0.06           | 0.000          | 0.00           | -0.752 | 0.203          | 0.000          | 1.30                | 0.855          | -1.124         | 0.400          | 0.101               |
| 0.8  | 2.411          | 0.07           | 0.000          | 0.00           | 0.000  | 0.499          | 0.000          | 0.10                | 1.287          | -1.293         | 0.372          | 0.235               |



magnify  
Postscript Velocity graph



magnify  
Postscript Angle grapha

→ better

# Detector R&D at MIT

U. Becker, P. Fisher, K. Ensslin, J. Thompson\*,  
T. Fazio\*, R. Henning, B. Demirköz, J. Lue, M. Sekora,  
E. Rhode, S. Yue, J. Pate, B. Stacey

\*graduated, 2002

## Drift MWPC



Google™

[Advanced Search](#) [Preferences](#) [Search Tips](#)

drift gas

Google Search

I'm Feeling Lucky

Searched **English** pages for **drift gas**. Results **1 - 10** of about **150,000**. Search took **0.33** seconds.

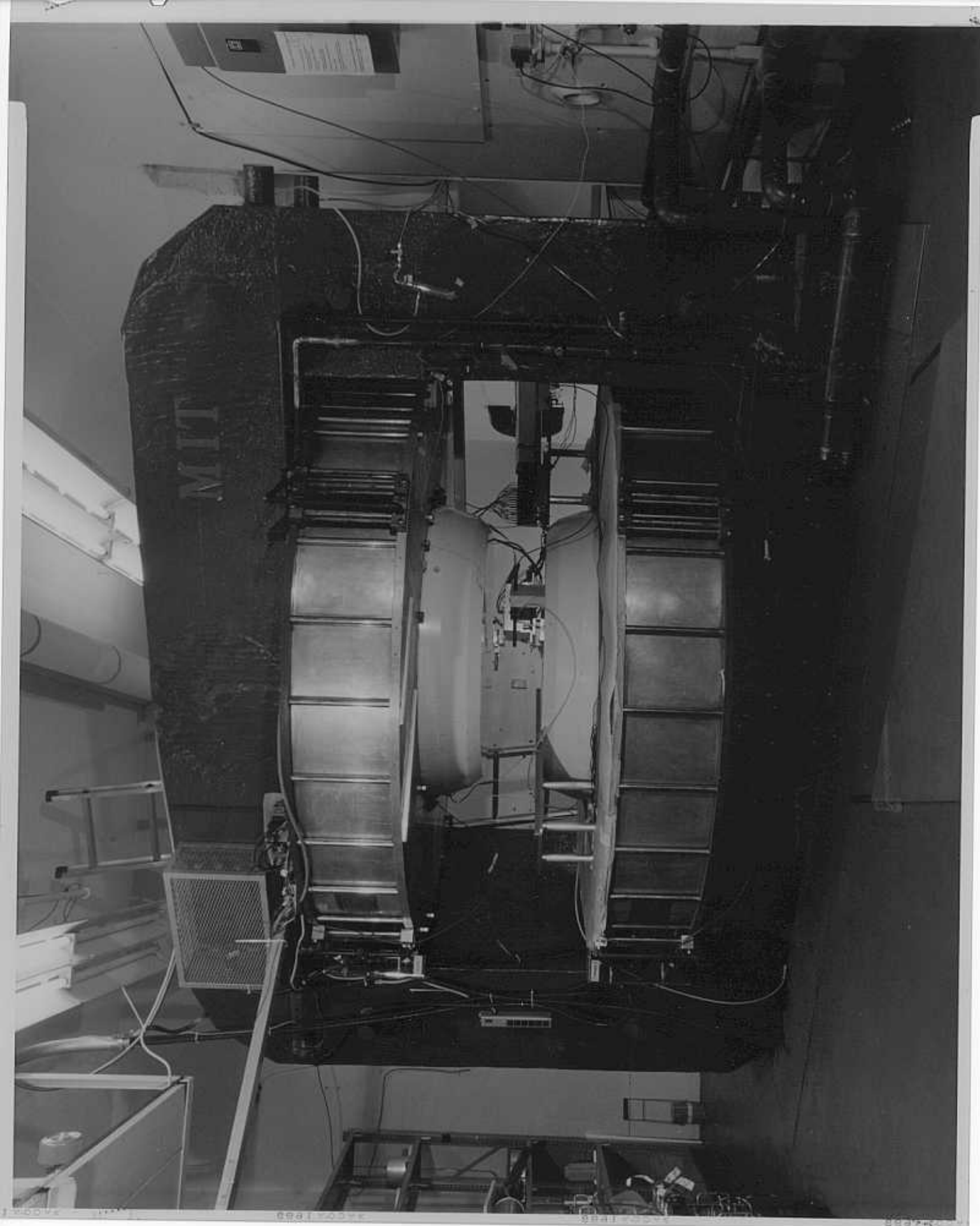
Category: [Science > Physics > Nuclear > Fusion > Magnetic](#)

[The MIT LNS Drift Gases R&D Experiment](#)

... **Drift** Gases R&D Database Search. Please choose the required options from among the following, and then submit your search request. We currently have the **gas** ...

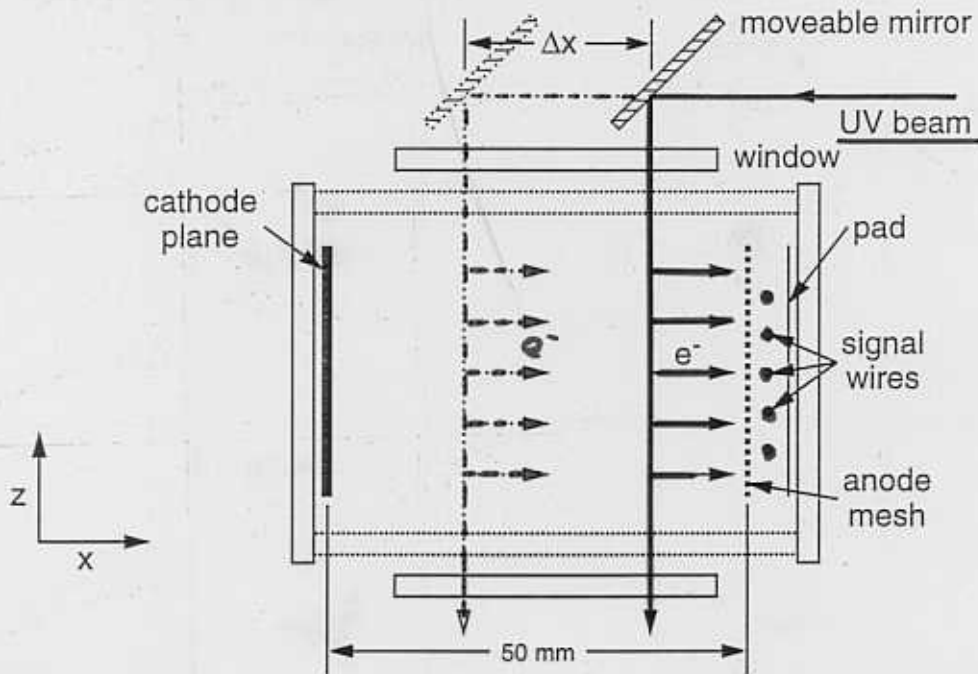
[cyclotron.mit.edu/drift/](#) - 6k - [Cached](#) - [Similar pages](#)

→ 773+ drift gas mixtures on the web

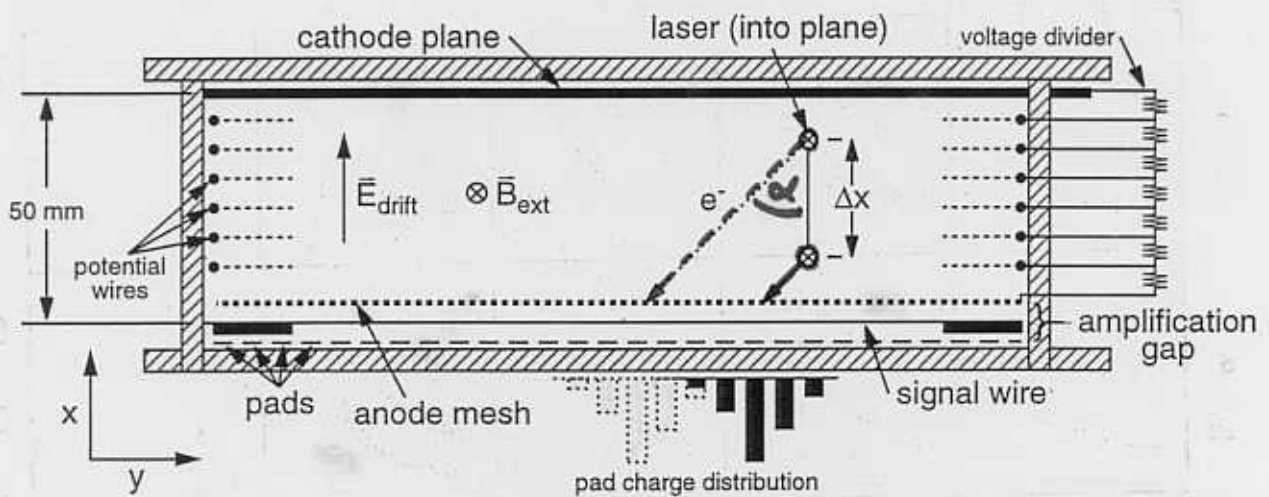


Noble Gases:  $V(B), \alpha(T)$

## $V_{||} - \alpha$ Measurement



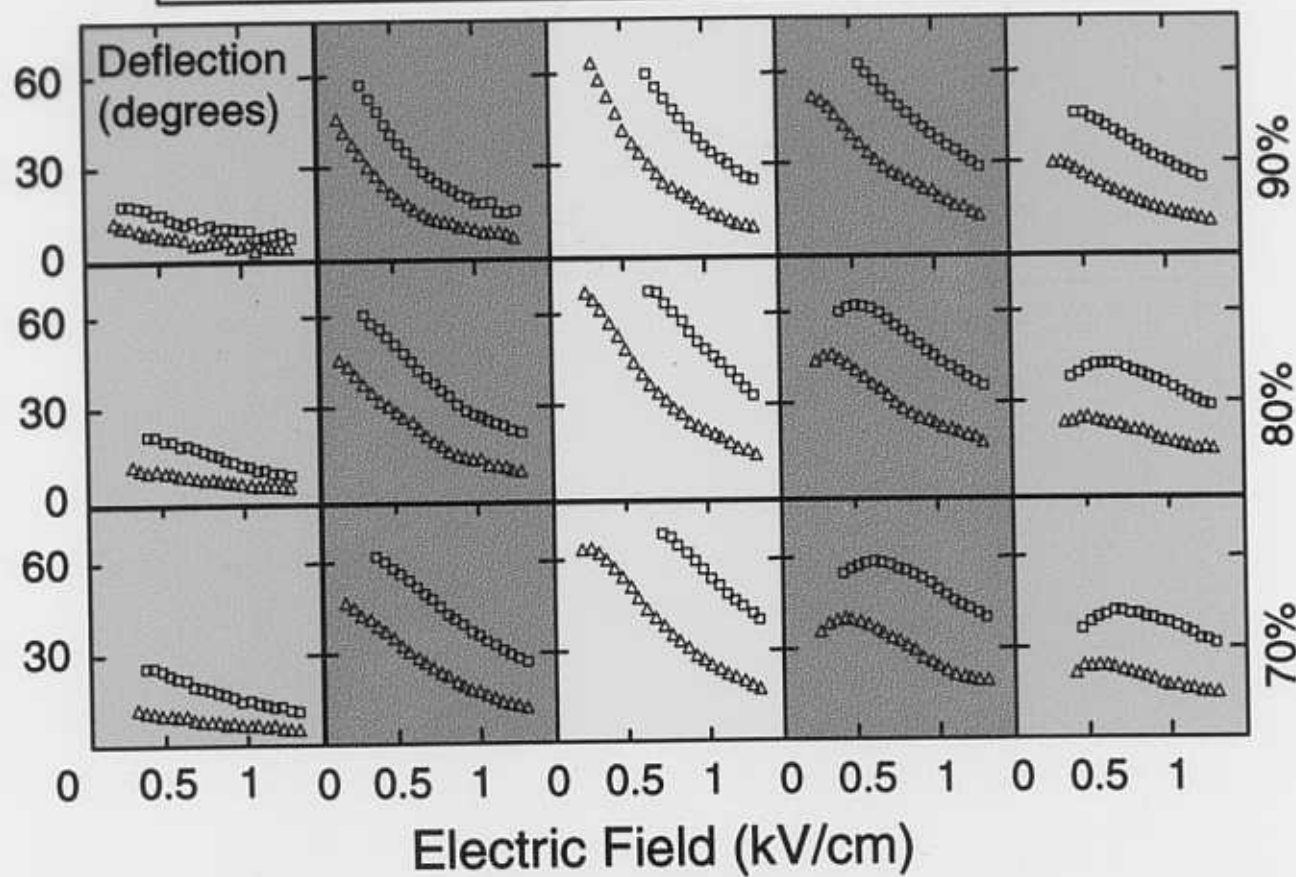
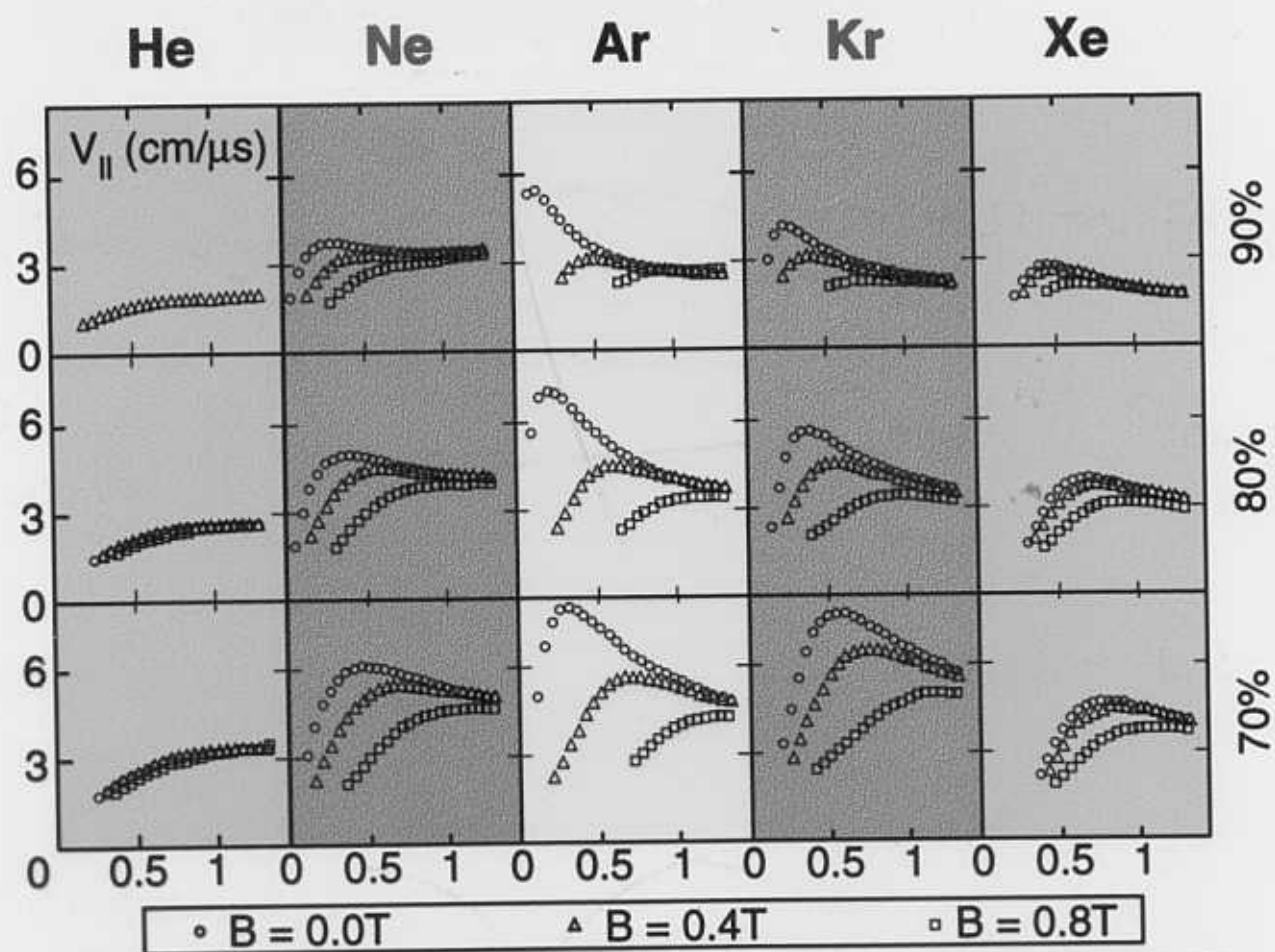
$$v_{||} = \frac{\Delta x}{\Delta t}$$



$$\tan \alpha = \frac{\Delta y}{\Delta x}$$

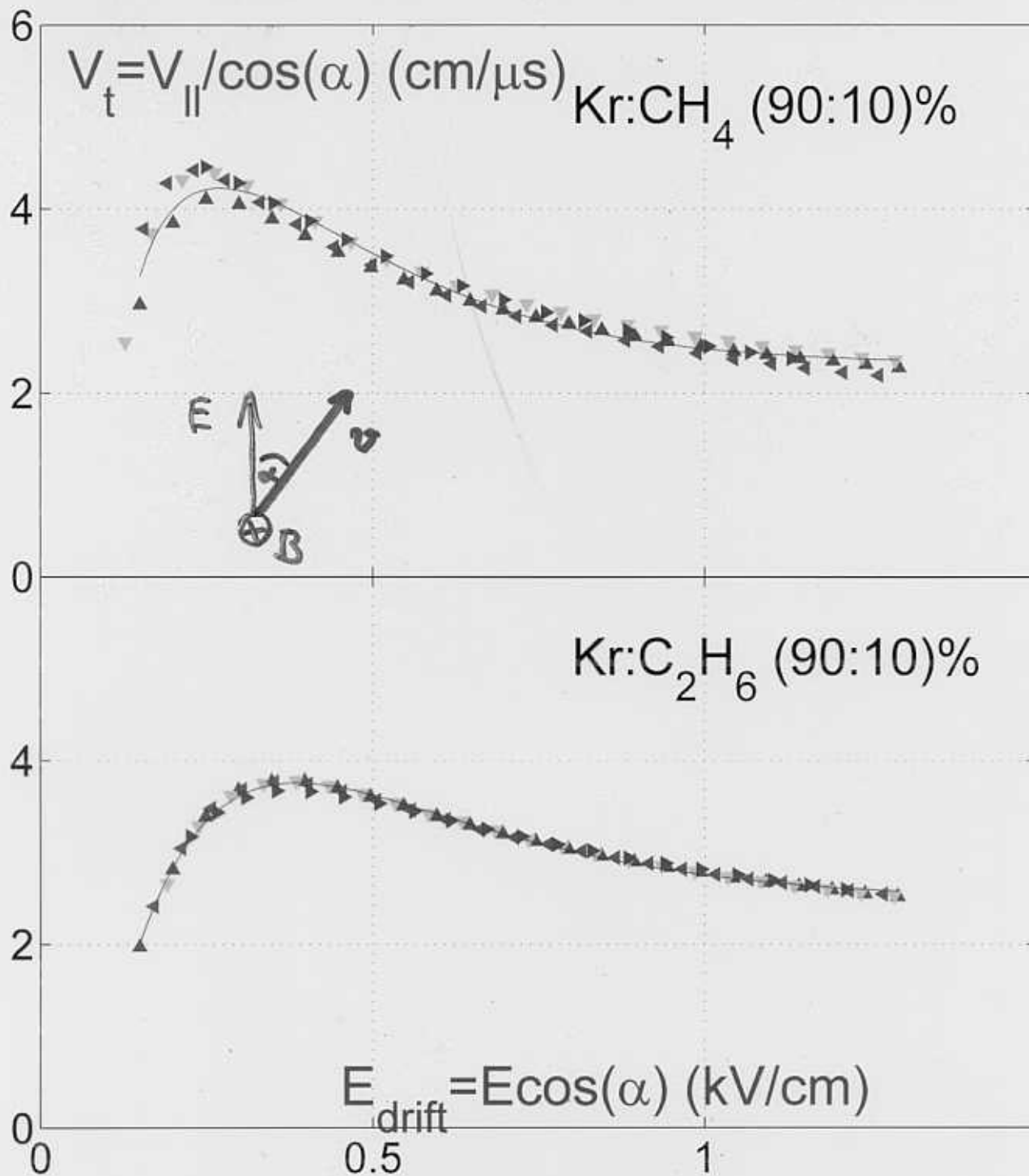
Differential  $\rightarrow$  ACCURATE

# Noble Gases: $V(B)$ , $\alpha(B)$





"Universal Curve" describes all  $\vec{B}$  data



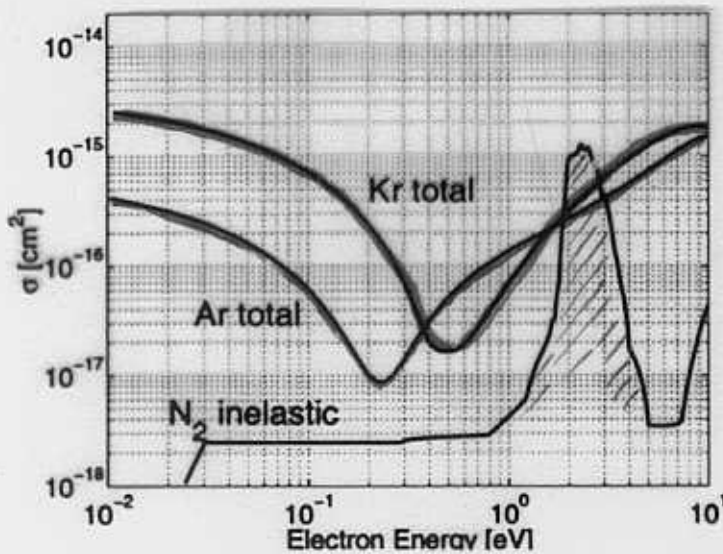
Universal Fit Information

| B(T)  |                                                                                                                            |
|-------|----------------------------------------------------------------------------------------------------------------------------|
| 0.0 ▲ | $V_t = U_1(1 - e^{-(E_d - \epsilon)/E_1}) + U_2(E_d - \epsilon)e^{-(E_d - \epsilon + \epsilon_2)/E_2} + W(E_d - \epsilon)$ |
| 0.2 ▼ | 1 <sup>st</sup> . $U_1 = 2.3$ $E_1 = 0.033$ $U_2 = 29$ $E_2 = 5.6$ $W = 0$ $\epsilon = 0.086$ $\epsilon_2 = 0$             |
| 0.4 ▲ |                                                                                                                            |
| 0.8 ► | 2 <sup>nd</sup> . $U_1 = 2.5$ $E_1 = 0.21$ $U_2 = 26$ $E_2 = 4.8$ $W = 0$ $\epsilon = 0.079$ $\epsilon_2 = 0$              |

Reduce Data and Interpolate!!!

# Understanding the Influence of Cross Sections

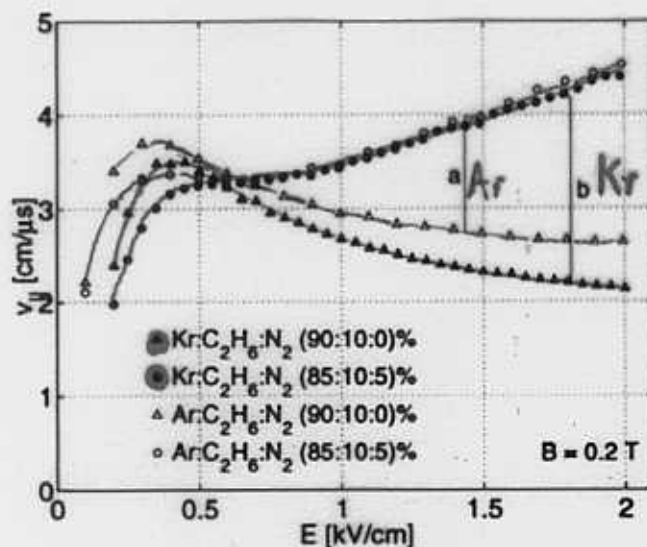
Example:



$\text{N}_2$  moderates  $e^-$  energy into minima

→ increase of  $v_{||}$

Proof of Understanding:



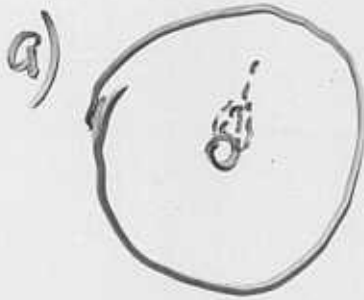
Kr has larger effect.

Ref: E. Fortunato, U. Becker, R. Dinner. Understanding the impact of additives with large inelastic cross-sections on drift chamber performance. NIM A421 (1999), 278-283.

→ Tailor Features of Drift Gas

4. Consider a normal drift tube working in proportional mode.  
at  $G = 10^3$ . You increase the voltage (gain) on the wire.

- What will limit the Gain eventually?
- What is the function of the quencher?

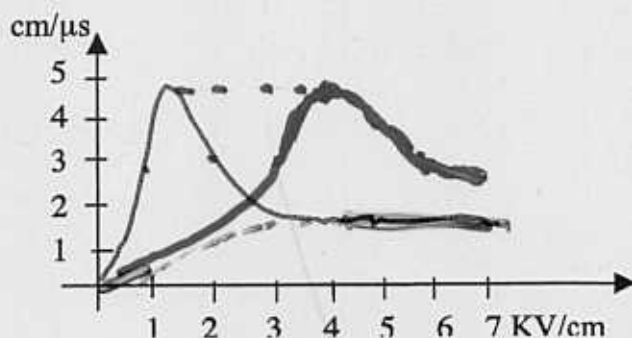


Backward propagation  
of UV from the avalanche

- proportional region
- streamer mode
- Geiger mode
- Spark ↓

b) Suppress UV.

2. You are given the drift velocity in a gas at 1 atm as shown below.



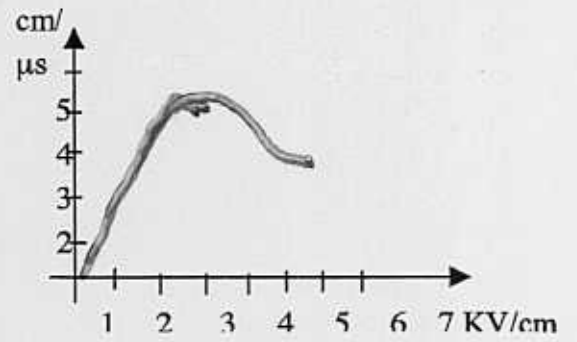
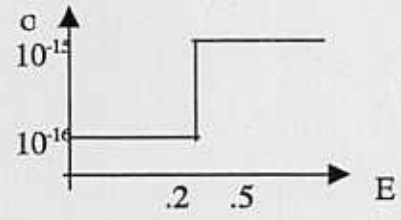
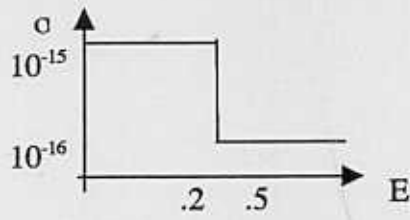
- Sketch the expectation for 3 atm.
- A magnetic field of 0.5T is turned on and the electrons by the Lorentz force are deflected by  $\tan \alpha = .77 (v \times B)/E$ . Roughly how would the curve look then?

a)  $E/p$  scaling  $\rightarrow E' = 3E_0$

b)  $E \rightarrow \infty \quad \tan \alpha \rightarrow 0 \quad E \cos \alpha \sim E$   
 $E \rightarrow 0 \quad \tan \alpha \rightarrow \infty \quad E \cos \alpha \rightarrow 0$

$K \cdot \frac{v \times B}{E}$

3. Given the following cross sections for electrons in a hypothetical gas, sketch your guess of a drift velocity vs  $E$  (or  $E/p$ ).



## Quick Check

1. If a minimum ionizing particle leaves in Argon at 1 atm 90 e<sup>-</sup>/cm in 20 clusters behind as a "track memory", a) what would expect in Helium?  
b) Estimate the efficiency of a 0.5 cm parallel plate counter.

a) Bethe-Bloch

$$-\frac{dE}{dx} = K Z^2 \left( \frac{Z}{A} \right) \frac{1}{\beta^2} \left[ \frac{1}{2} \ln \frac{2m_e c^2 T_{max} \beta^2 \gamma^2}{I^2} - \beta^2 - \frac{C}{Z} \right]$$

$$\frac{Z_{He}}{Z_{Ar}} = \frac{2}{18} \rightarrow N_{Ar} \sim 90/9 = 10 \quad (10)$$

$$N_{He} \sim 20/9 = 2.2 \quad (5)$$

b) Relevant: clusters

Probability to have no cluster in 0.5 cm

$$P(0, \mu) = e^{-\mu d} = e^{-\frac{2.2}{2}} = \frac{37}{100} = 37\%$$

$$E_{eff} = 1 - e^{-\frac{2.2}{2}} = 63\% \quad (91\%)$$