

# NEUTRINOS II

## The Sequel

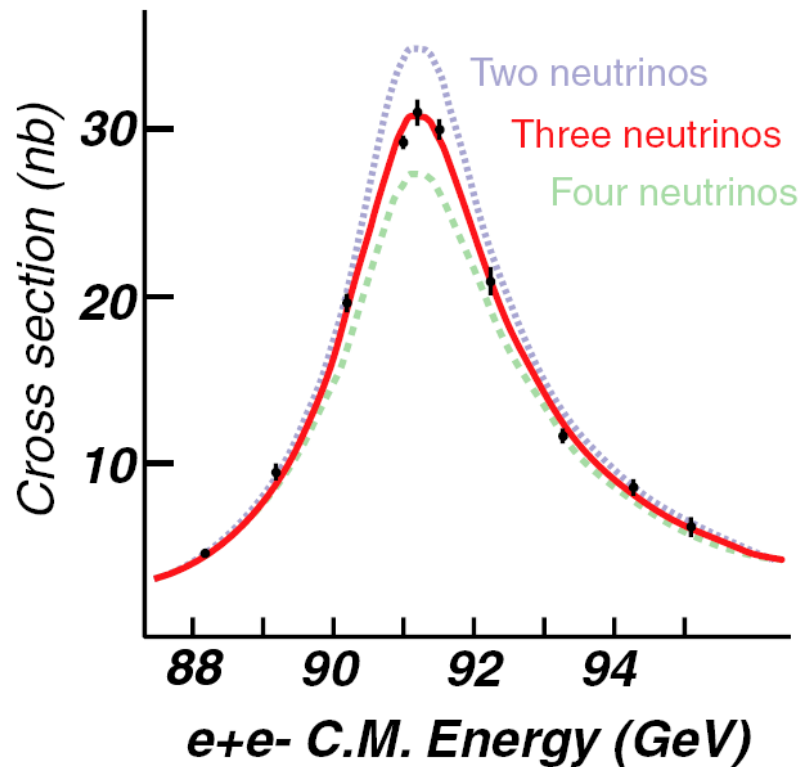
### *More About Neutrinos*

Ed Kearns – Boston University

NEPPSR V - 2006

There is something unusual about this neutrino talk compared to many other neutrino talks you may have seen. Can you discern it?

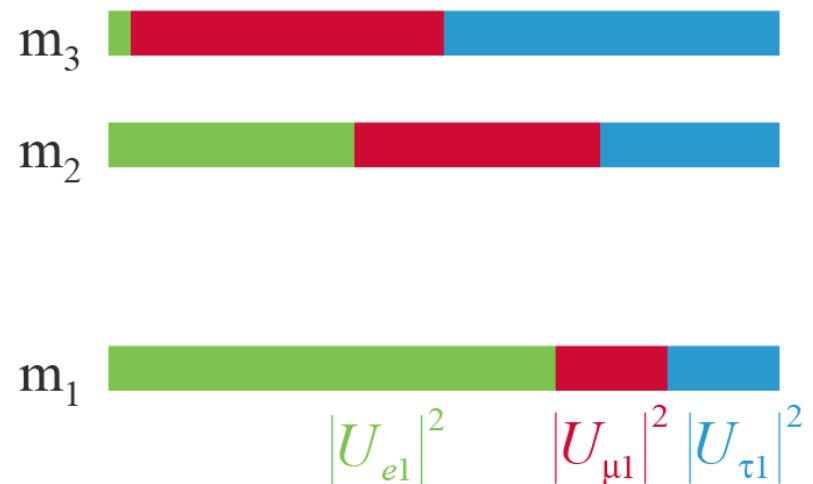
# The Number of Neutrinos is Three

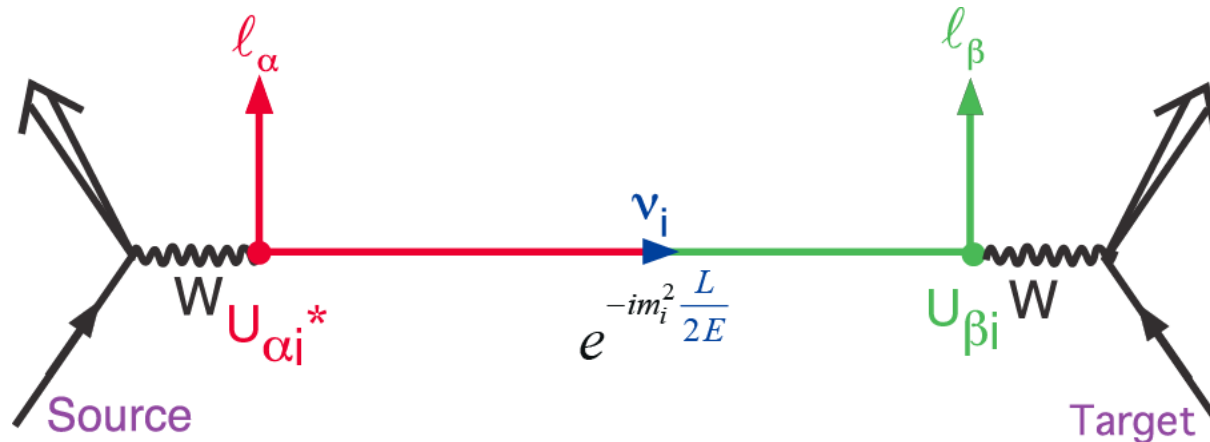


*results from LEP experiments  
at CERN (1990's)*

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

Pontecorvo-Maki-Nakagawa-Sakata Matrix (PMNS or MNS)



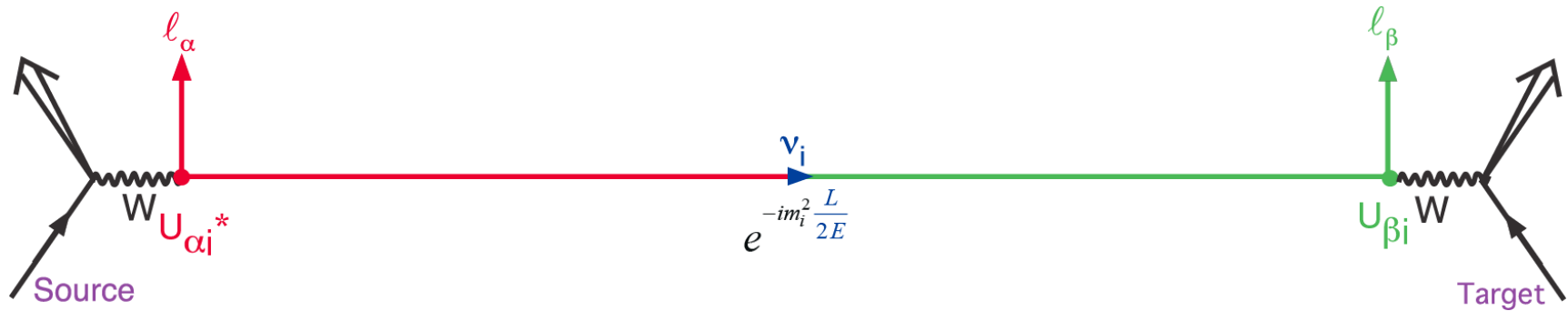


$$P(\nu_\alpha \rightarrow \nu_\beta) = \delta_{\alpha\beta} - 4 \sum_{i>j} \text{Re}[U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*] \sin^2 \left( \Delta m_{ij}^2 \frac{L}{4E} \right) \\ \text{- sign for antineutrinos} \quad \pm 2 \sum_{i>j} \text{Im}[U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*] \sin \left( \Delta m_{ij}^2 \frac{L}{4E} \right)$$

often the case: one of the oscillatory terms remains zero  
under the experimental conditions (i.e.  $L$  too short,  $E$  too large etc.)

$$P(\nu_\alpha \rightarrow \nu_\beta) = \sin^2 2\theta \sin^2 \left( 1.27 \Delta m_{ij}^2 \frac{L}{E} \right)$$

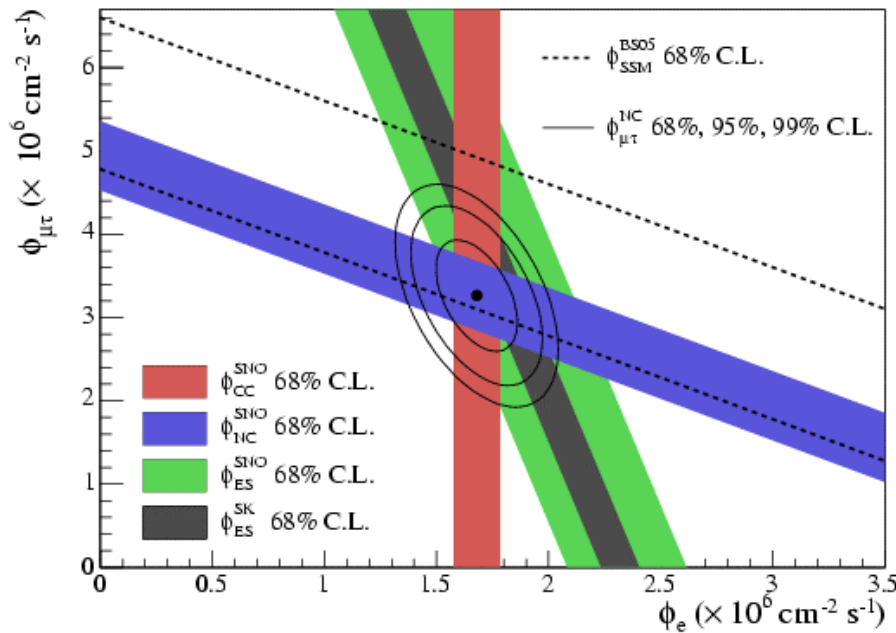
( $L$  in km,  $E$  in GeV) or ( $L$  in m,  $E$  in MeV)



|               | Flavor Produced                                    | Baseline    | Energy       | Flavor Detected                                    |                        |
|---------------|--|-------------|--------------|--|------------------------|
| The Sun       | $\nu_e$  | $10^{11}$ m | 0.1-15 MeV   | $\nu_e$ , NC                                       | SNO, Super-K, others   |
| Reactor       | $\bar{\nu}_e$                                      | 1-200 km    | 0.3 GeV      | $\bar{\nu}_e$                                      | KamLAND, Chooz         |
|               | $\bar{\nu}_e$                                      | 0.3+2 km    | 0.3 GeV      | $\bar{\nu}_e$                                      | Double Chooz, Daya Bay |
| Cosmic rays   | $(\nu_\mu + \bar{\nu}_\mu), (\nu_e + \bar{\nu}_e)$ | 10-10000 km | subGeV – TeV | $(\nu_\mu + \bar{\nu}_\mu), (\nu_e + \bar{\nu}_e)$ | Super-K, others        |
| Accelerator   | $\nu_\mu$  | 250, 735 km | 0.1-10 GeV   | $\nu_\mu, \nu_e$                                   | K2K, MINOS             |
|               | $\nu_\mu$  | 295, 810 km | 0.7, 2.2 GeV | $\nu_\mu, \nu_e$                                   | T2K, NOvA              |
|               | $\nu_\mu, \bar{\nu}_\mu$                           | 540 m       | 500 MeV      | $\nu_e, \bar{\nu}_e$                               | MiniBooNE              |
|               | $\nu_\mu, \bar{\nu}_\mu$                           | 295+1000 km | 0.5 GeV      | $\nu_e, \bar{\nu}_e$                               | T2KK                   |
| Stopped $\pi$ | $\bar{\nu}_\mu$                                    | 50 m        | 50 MeV       | $\nu_e, \bar{\nu}_e$                               | LSND, KARMEN           |
| Beta Beam     | $\nu_e, \bar{\nu}_e$                               | ??          | 0.2-10 GeV?  | $\nu_e, \bar{\nu}_e, \nu_\mu, \bar{\nu}_\mu$       | ???                    |
| $\nu$ Factory | $(\nu_\mu + \bar{\nu}_e), (\nu_e + \bar{\nu}_\mu)$ | ??          | 20 GeV ?     | $(\nu_e + \bar{\nu}_\mu), (\nu_\mu + \bar{\nu}_e)$ | ???                    |

The first hints of neutrino mixing, and the first convincing results came from natural sources

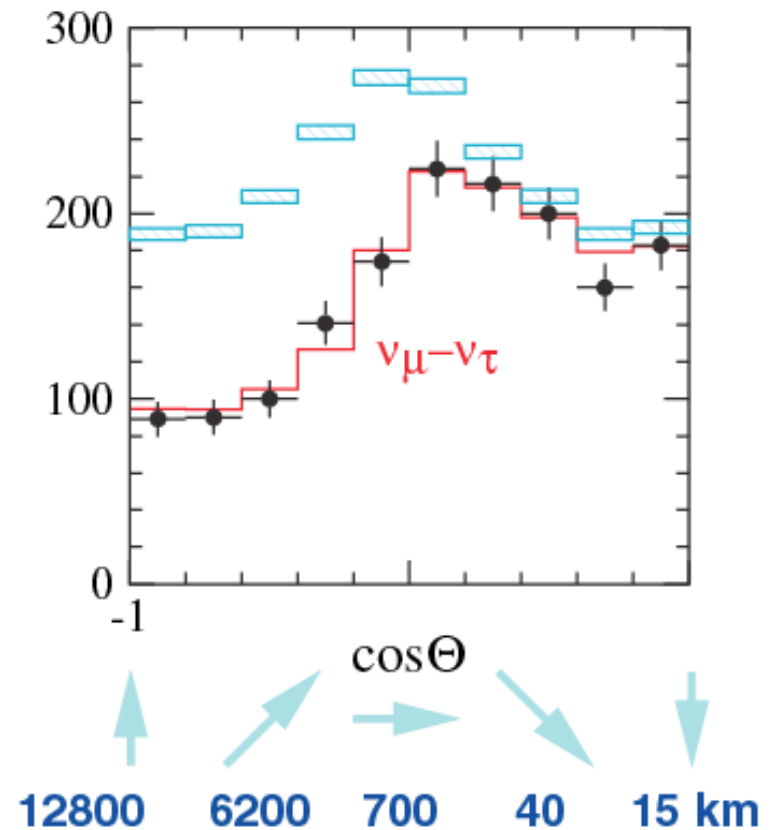
## Solar Neutrinos



$$\Phi(\nu_e) < \Phi(\nu_e + \nu_\mu + \nu_\tau) \approx \Phi(SSM)$$

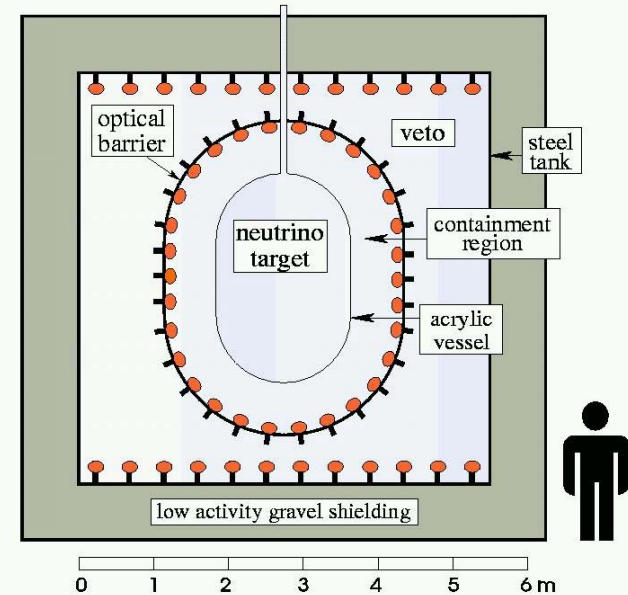
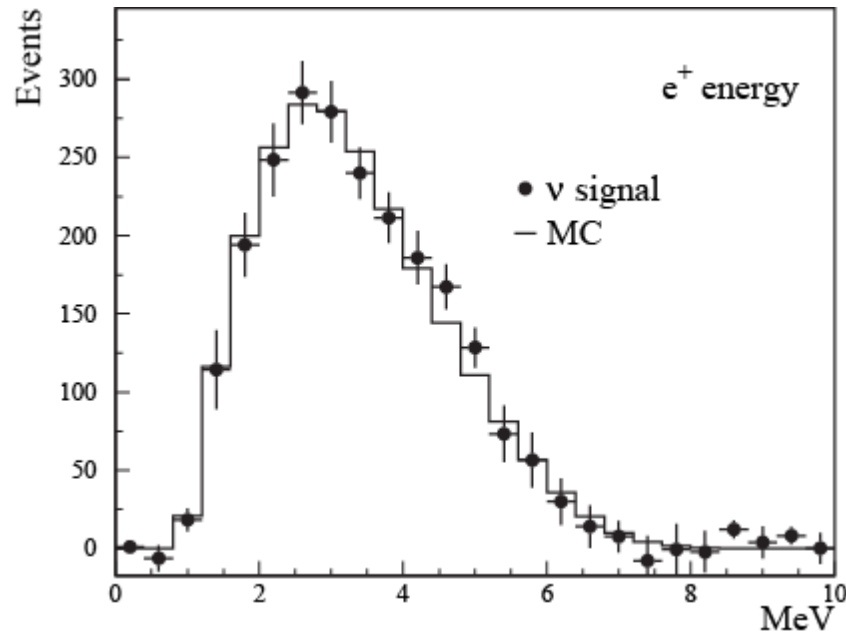
Also important: Super-K, Kamiokande, SAGE,  
Gallex/GNO, Homestake

## Atmospheric Neutrinos



Confirmed by MACRO, Soudan 2  
Started by Kamiokande and IMB

But we must keep in mind an important negative result – Chooz reactor experiment

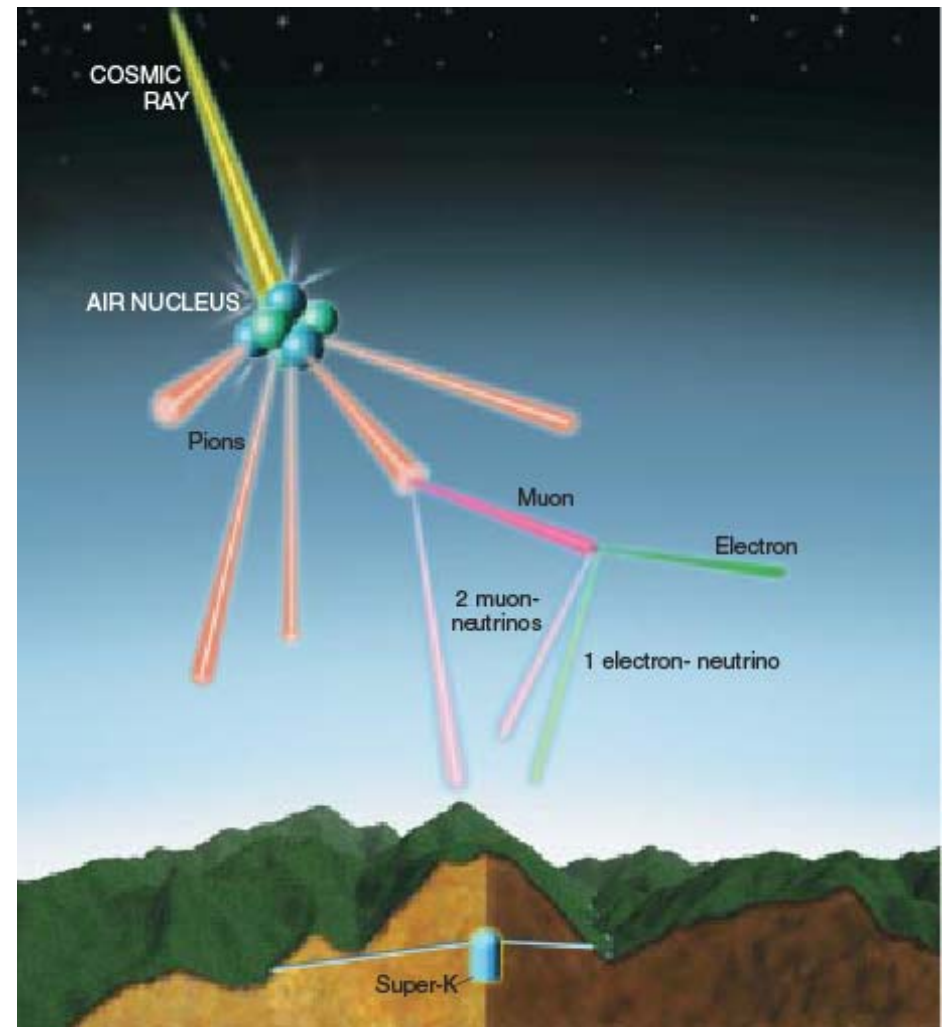
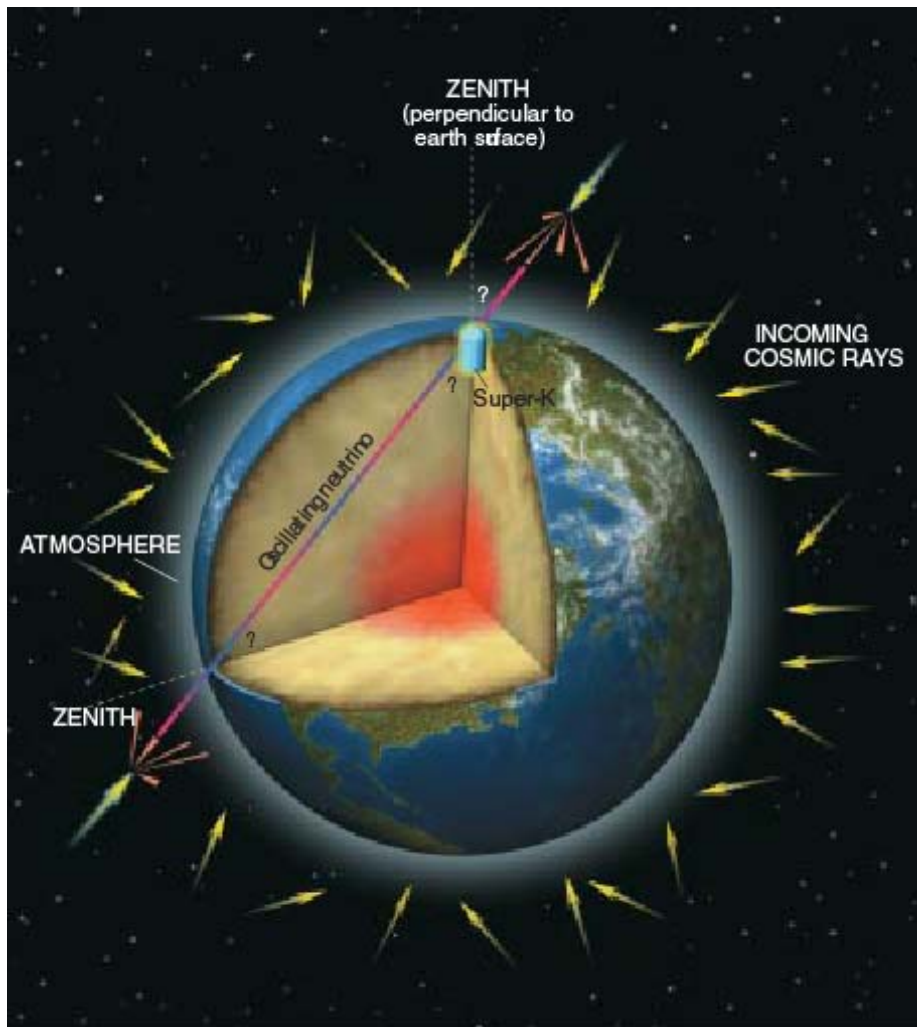


No evidence for electron neutrino disappearance over  $\sim 1$  km

$$\sin^2 2\theta < 0.2 \quad (\text{at } \Delta m^2 \sim 2 \times 10^{-3} \text{ eV}^2)$$

Also Palo Verde Reactor experiment

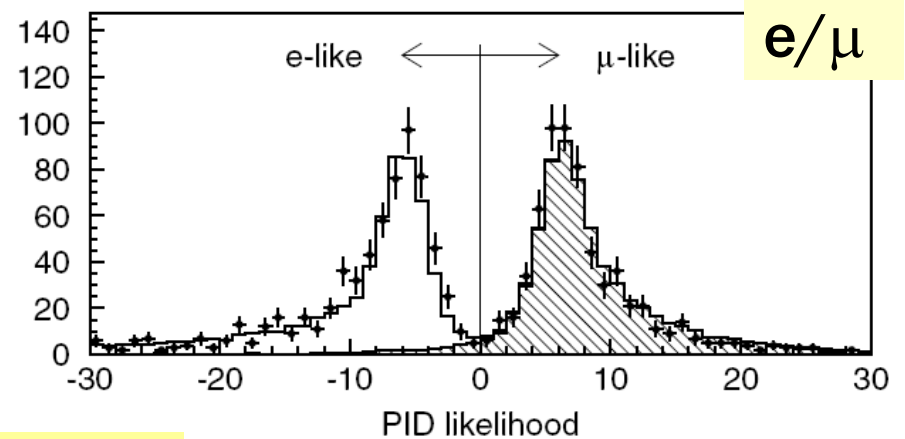
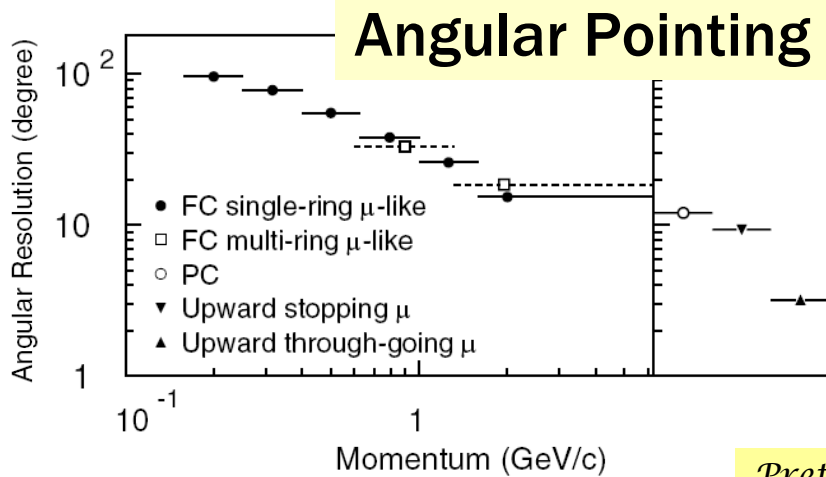
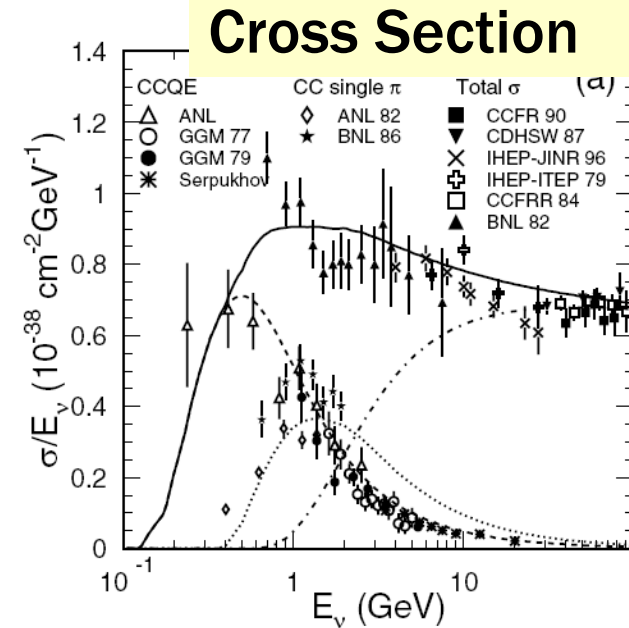
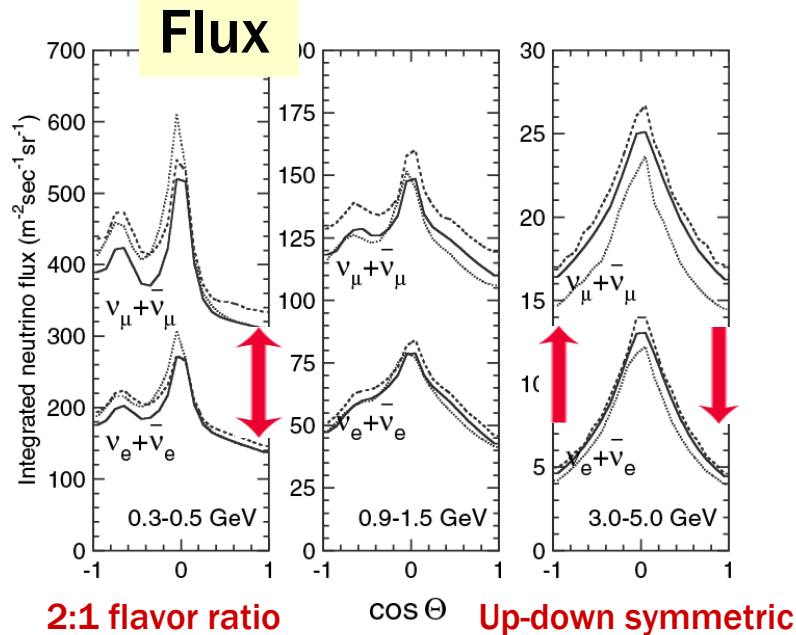
# Atmospheric Neutrinos



*Pretty!*



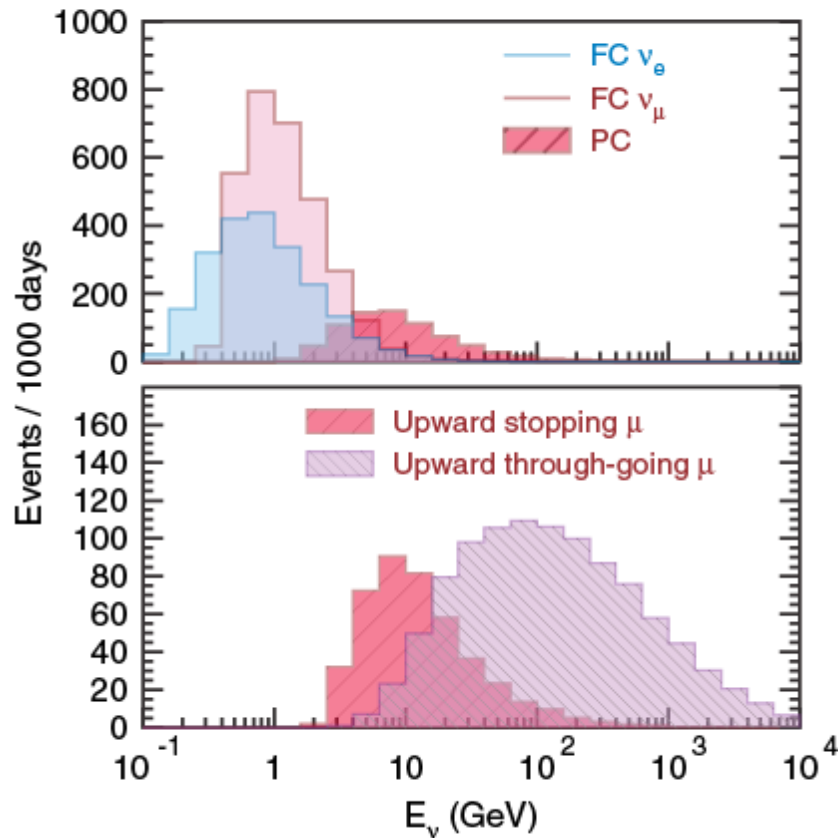
# Atmospheric Neutrinos



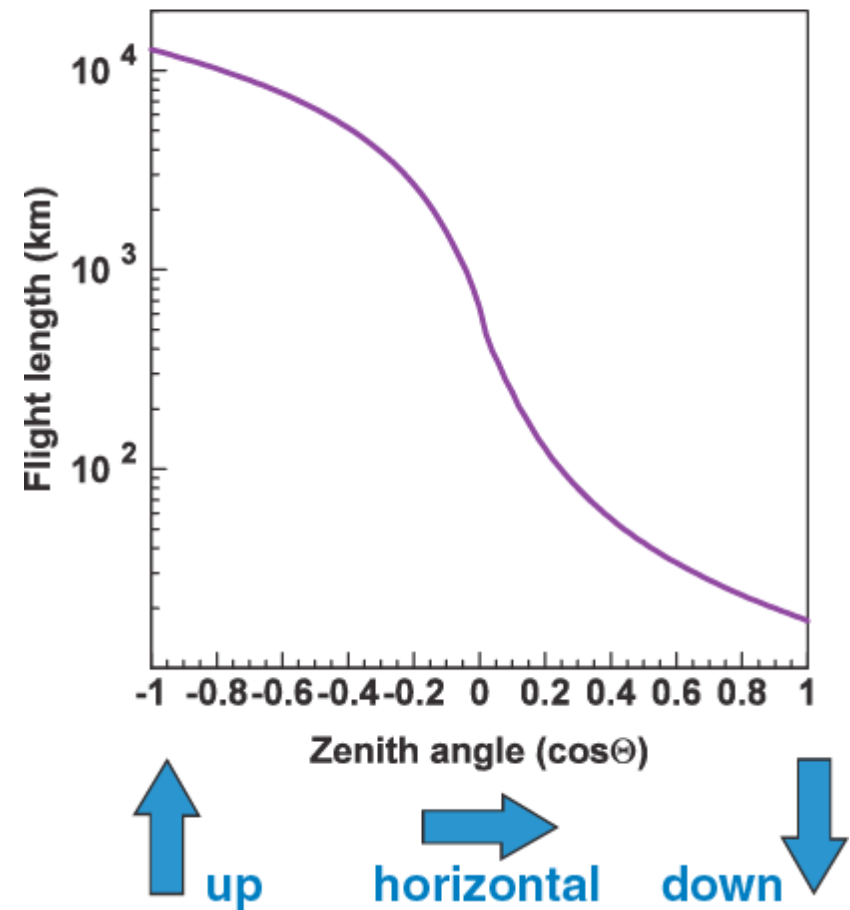
*Pretty technical!*

# Atmospheric Neutrinos

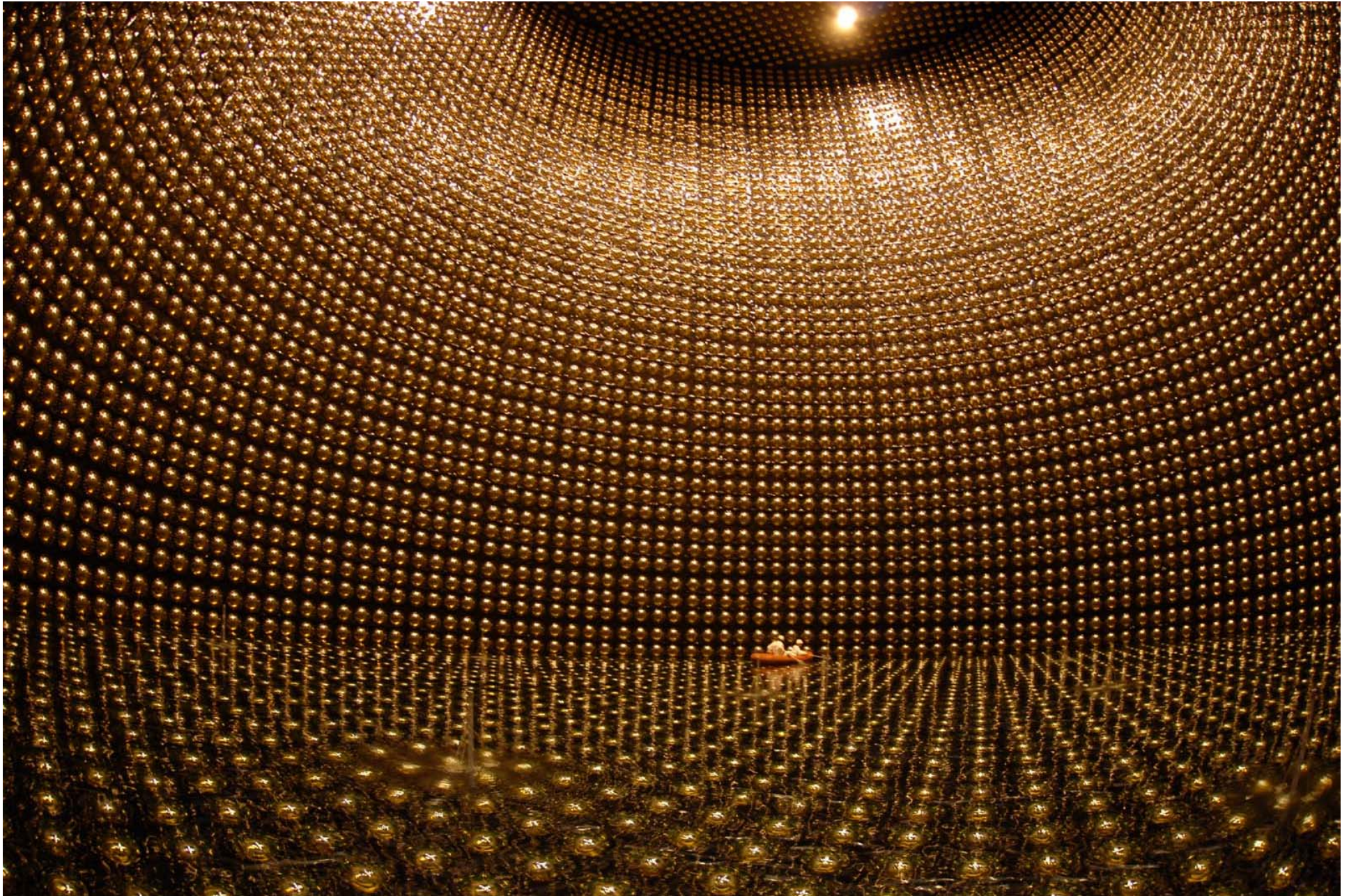
*5 decades of neutrino energy*



*Three decades of pathlength*







Super-Kamiokande III (newly rebuilt, filling in May 2006)



# Super-Kamiokande

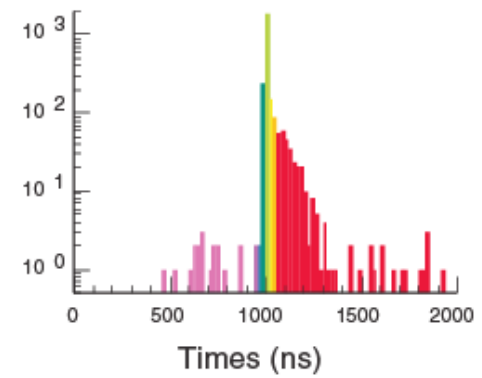
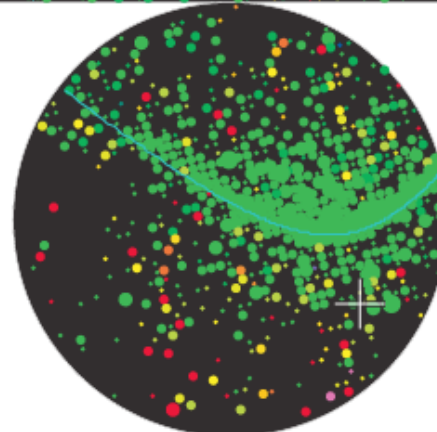
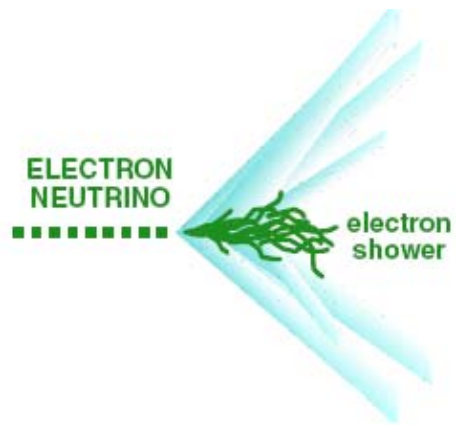
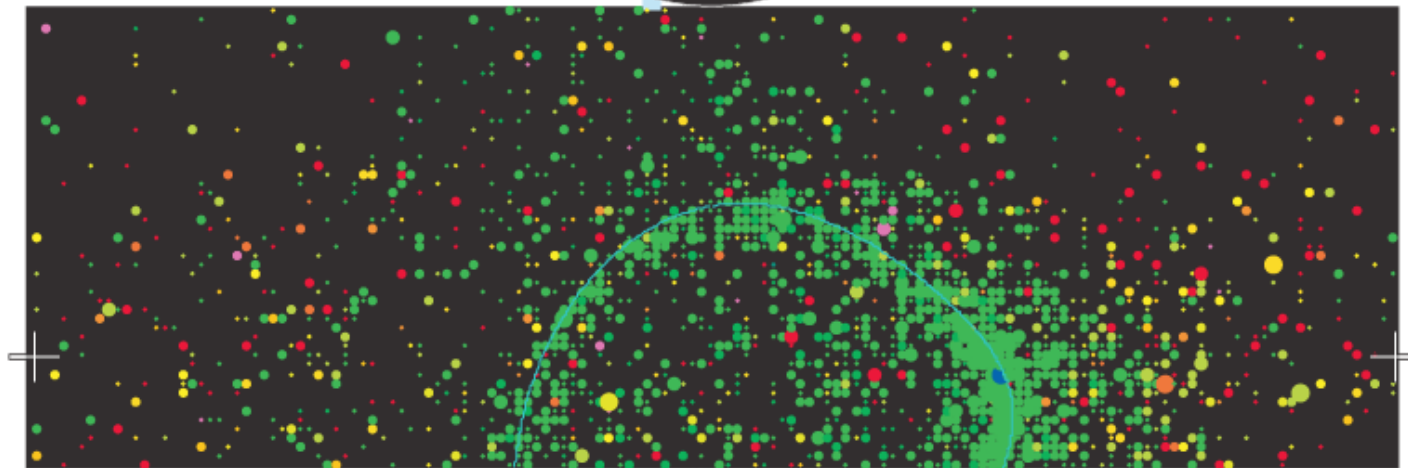
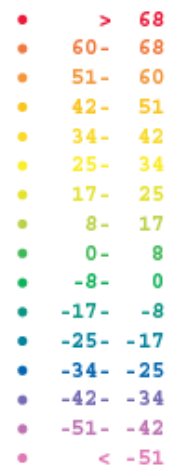
Run 4268 Event 7899421

97-06-23:03:15:57

Inner: 2652 hits, 5747 pE

~620 MeV/c

Resid(ns)



## Super-Kamiokande

Run 21703 Sub 26 Ev 1030957

03-02-08:19:24:46 00b7 d02d 55af

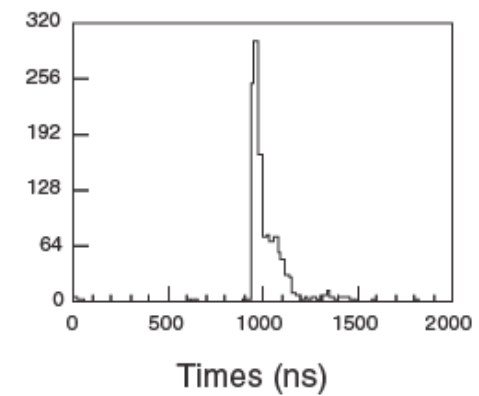
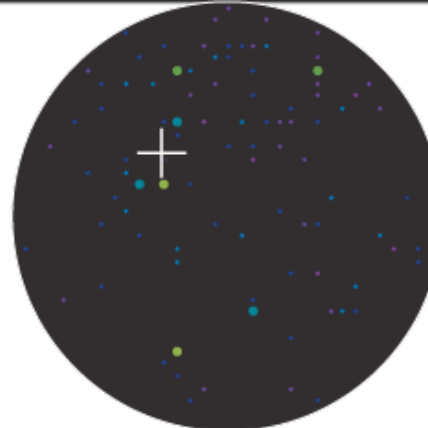
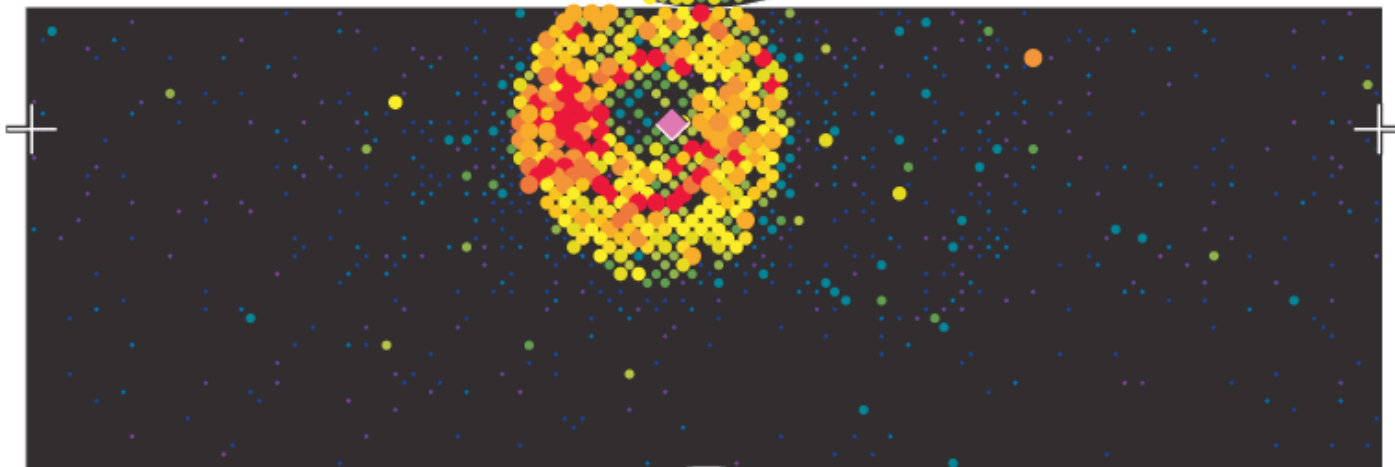
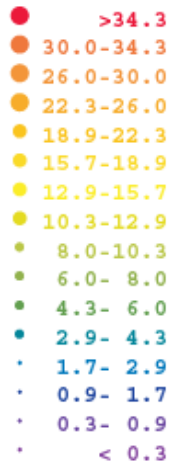
Inner: 1289 hits, 8528 pB

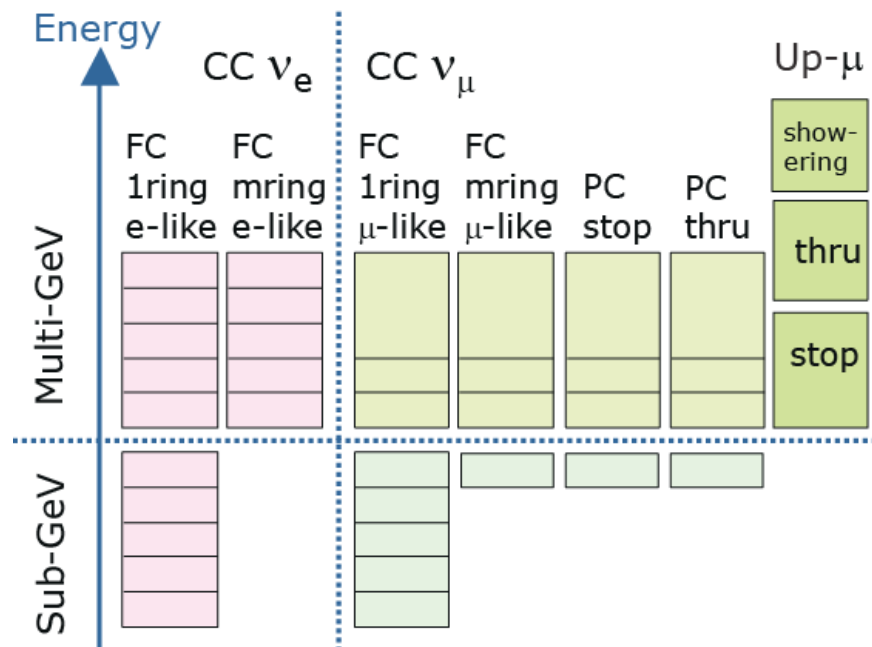
Outer: 2 hits, 0 pB (in-time)

Trigger ID: 0x03

D wall: 945.2 cm

### Charge (pe)





## How we bin and fit the data at SK

380 bins  $\times$  (SK-I+SK-II)  
+ 70 systematic terms

number of  
 $p, \Theta$  bins

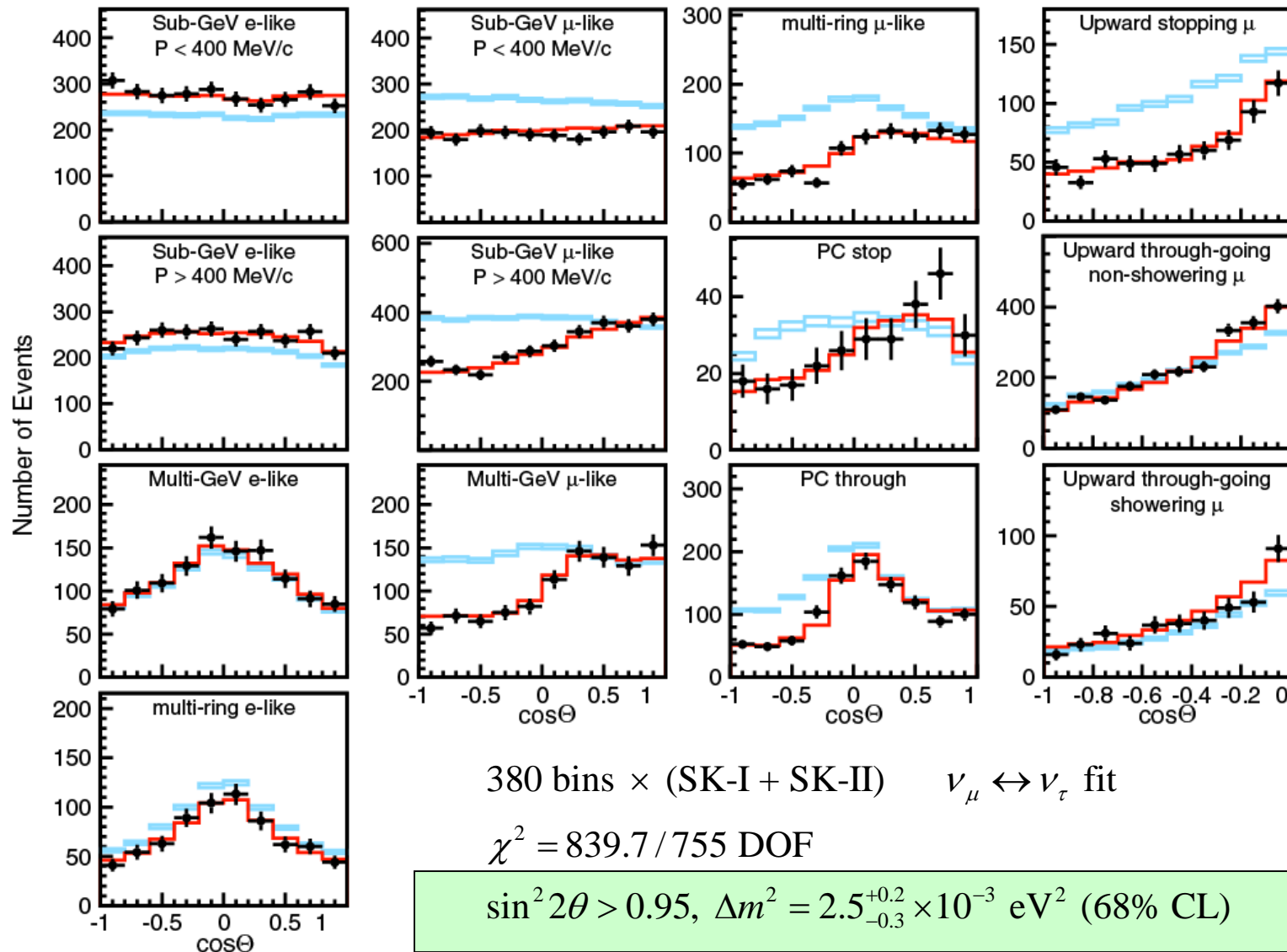
$$\chi^2 = \sum_{i=1}^{380} \frac{\left( N_i^{obs} - N_i^{exp} \left( 1 + \sum_{j=1}^{70} f_j^i \cdot \epsilon_j \right) \right)^2}{\sigma_i^2} + \sum_{j=1}^{65} \left( \frac{\epsilon_j}{\sigma_j} \right)^2$$

number of  
sys. effects  
(some norms.  
are free)

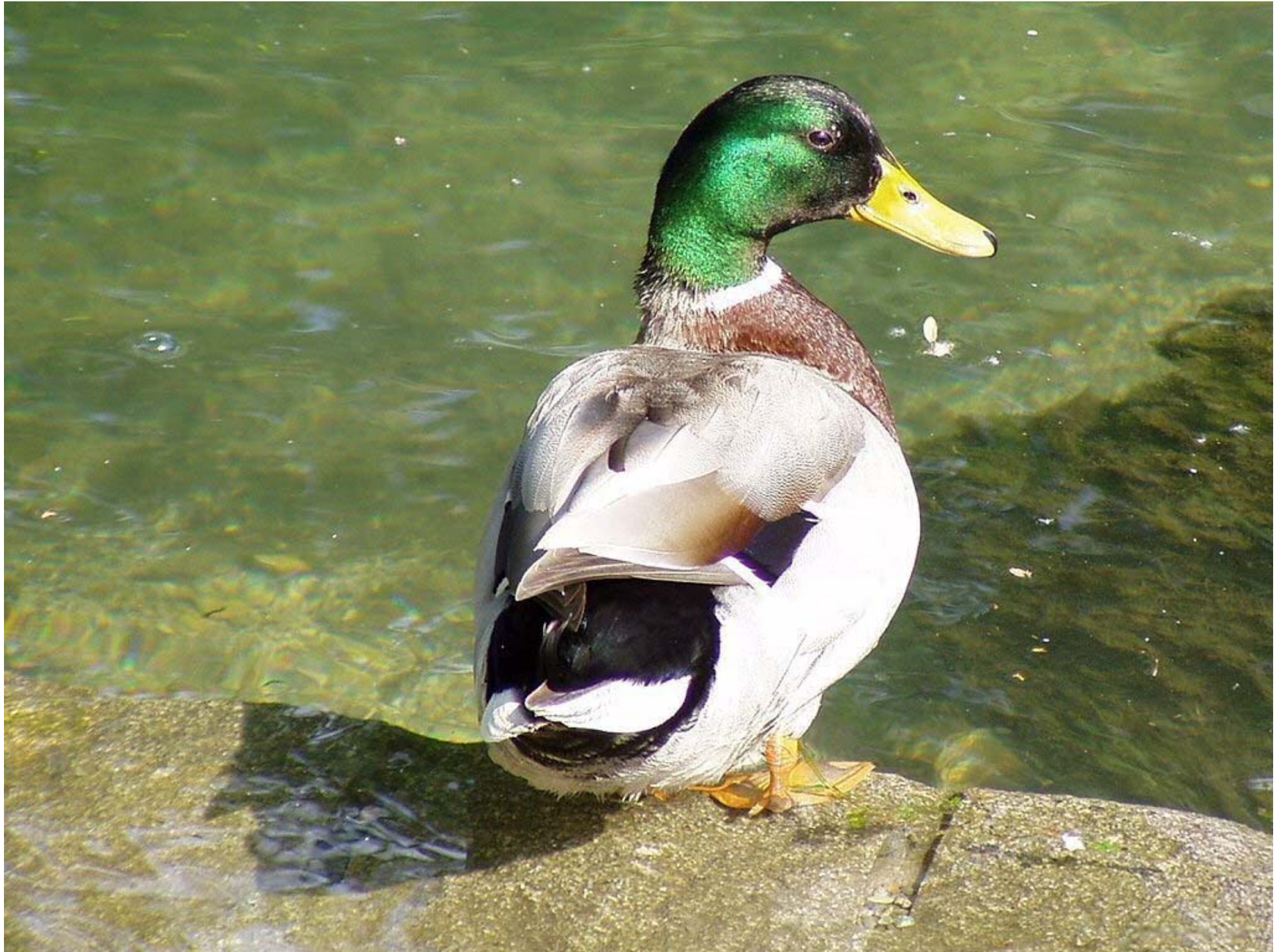
$$N_i^{exp} = N_i^0 \cdot P(\nu_\alpha \rightarrow \nu_\beta) \cdot \left( 1 + \sum_{j=1}^{39} f_j^i \cdot \epsilon_j \right)$$

fractional change in  
predicted event rate  
due to variation in  
systematic parameter  $\epsilon$

# Muon Neutrino – Tau Neutrino Mixing



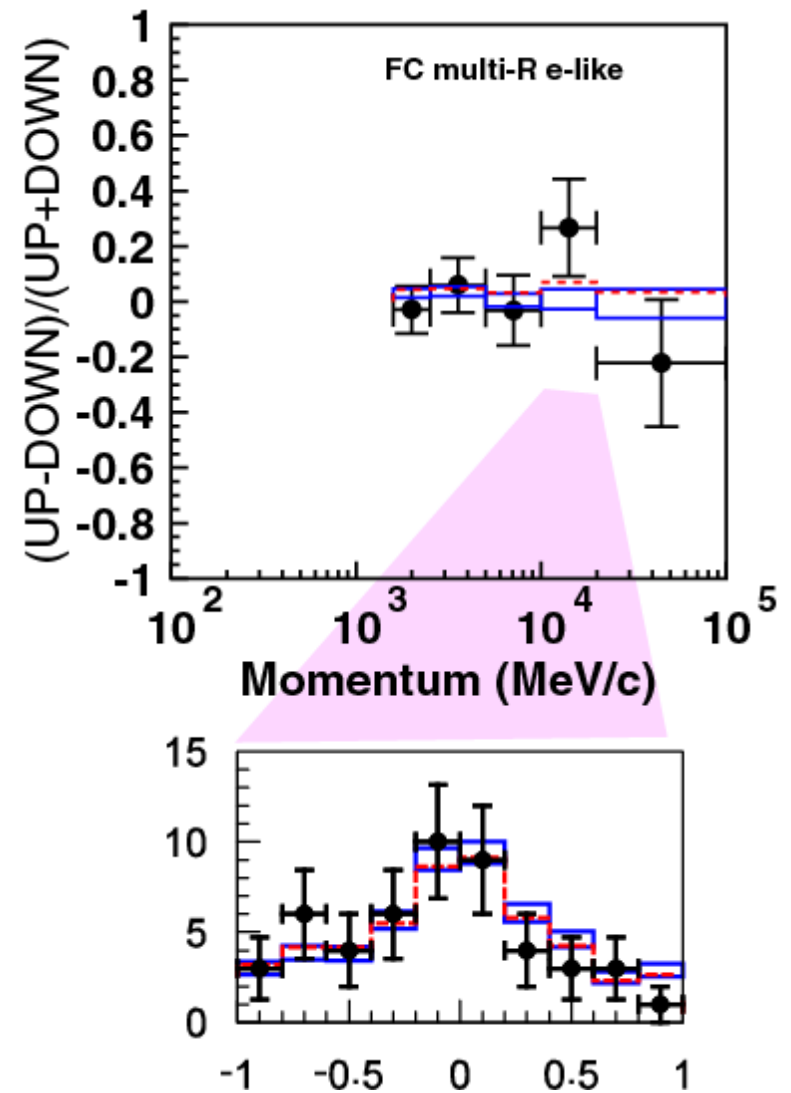
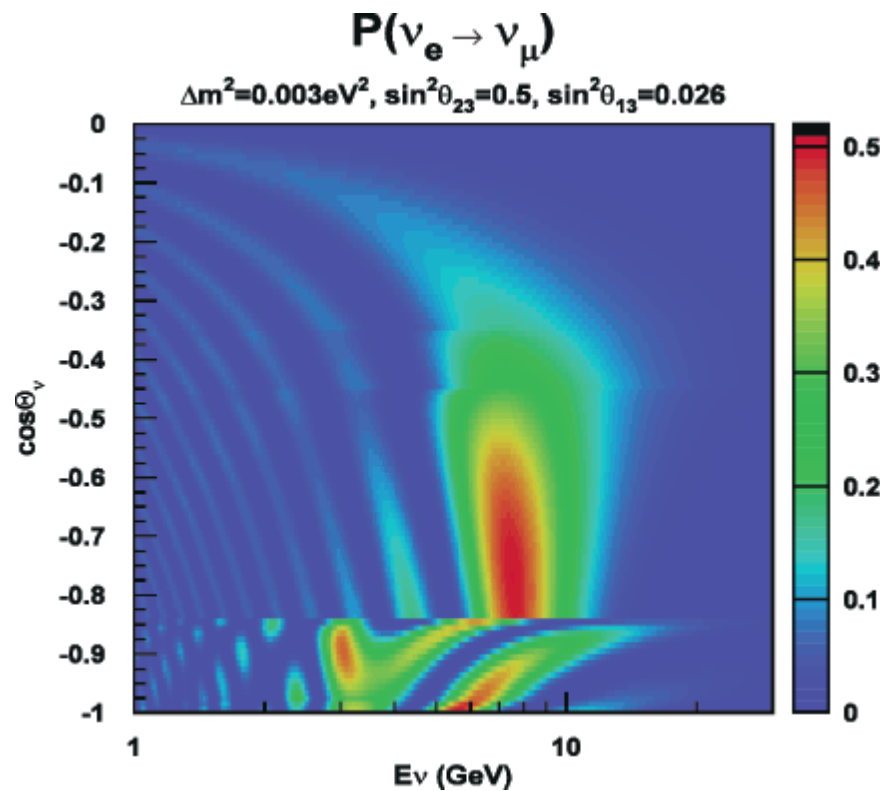






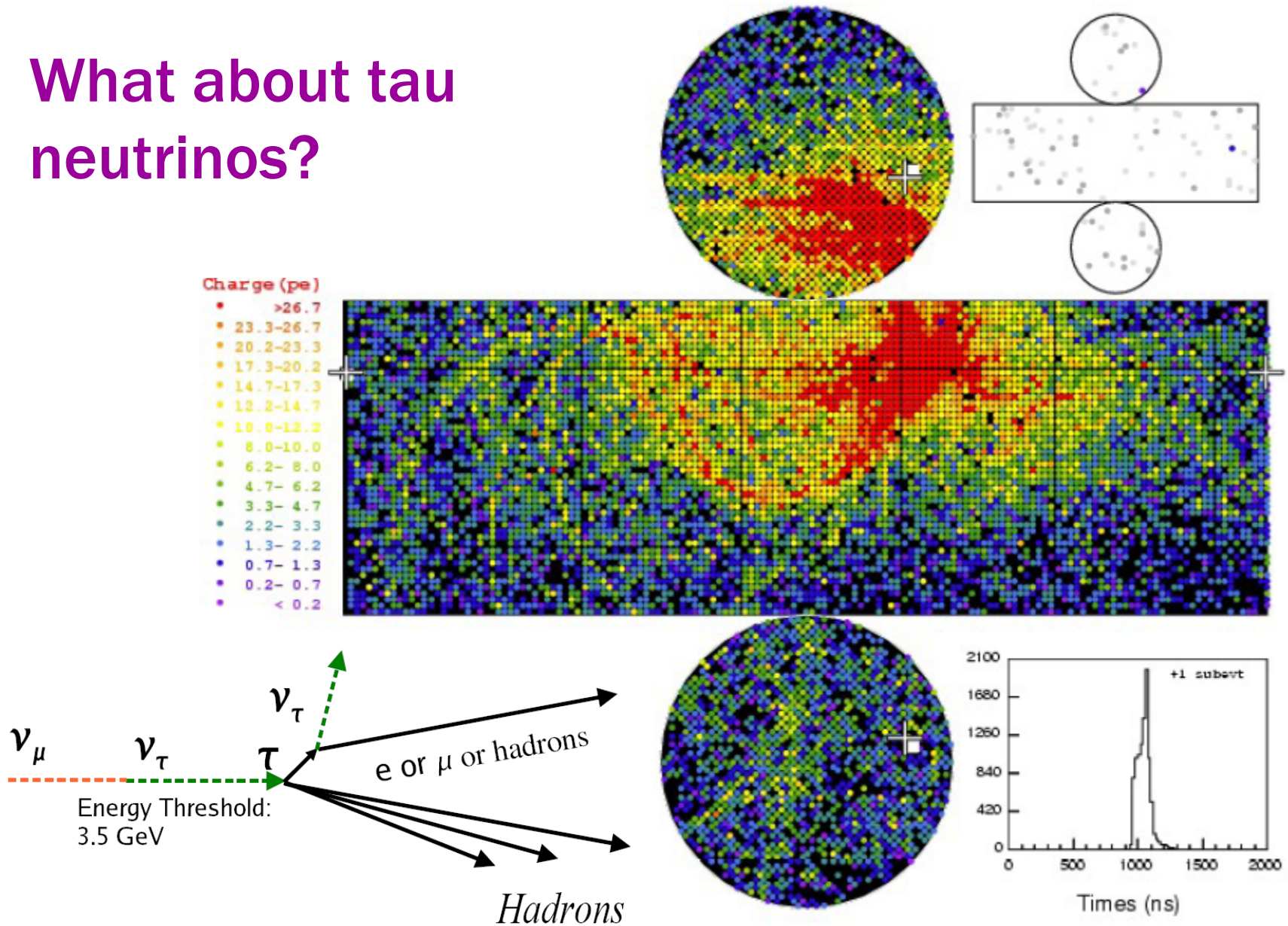
# What about electron neutrinos?

*Strategy: bin data very finely and look for enhancement at certain energies and angles due to electron neutrino resonance in earth*

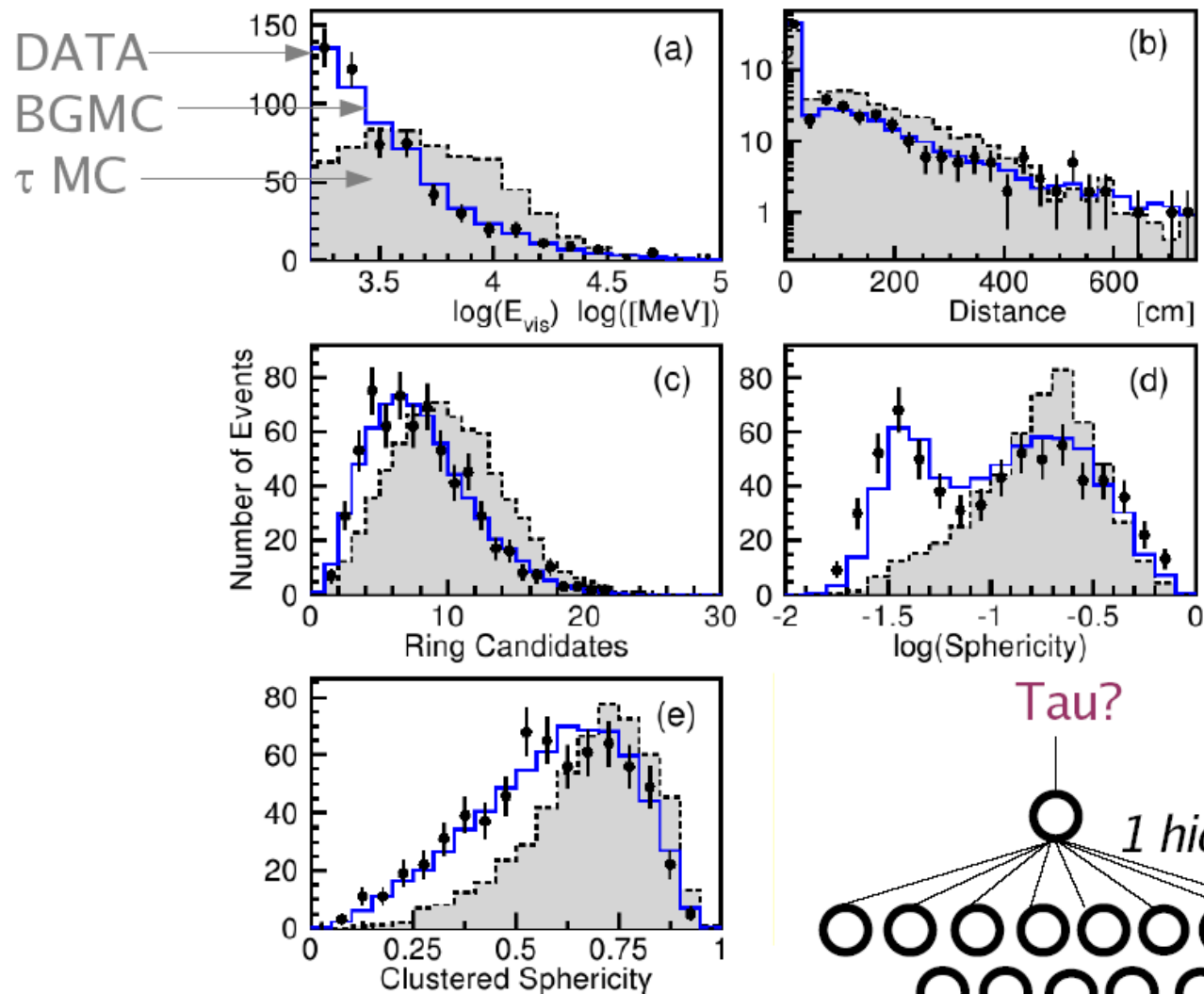


*no signs of enhancement in this or other data sub-samples.*

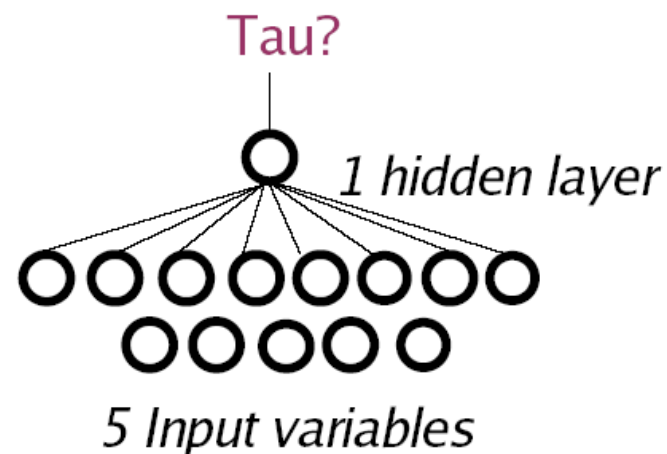
# What about tau neutrinos?



# Neural Network Analysis of Tau Appearance



There should be no tau events in the down-going data.



# Neural Network Analysis of Tau Appearance

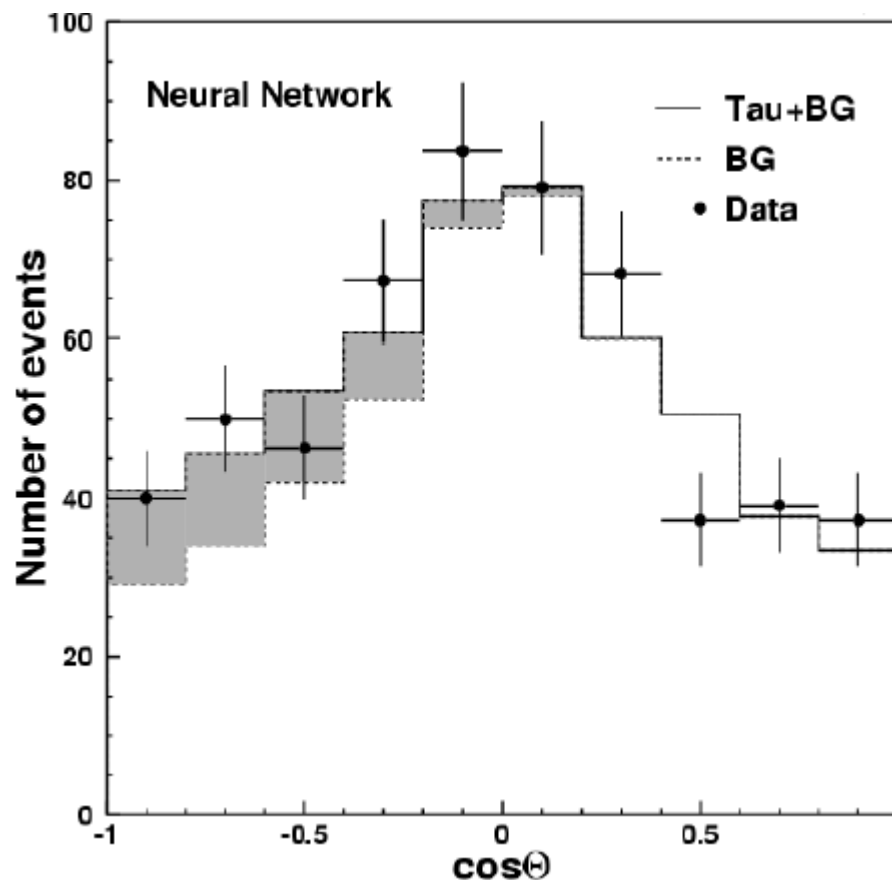
$$f(\cos(\theta)) = \alpha \times (\text{Tau}) + \beta \times (\text{No Tau})$$

Tau Excess

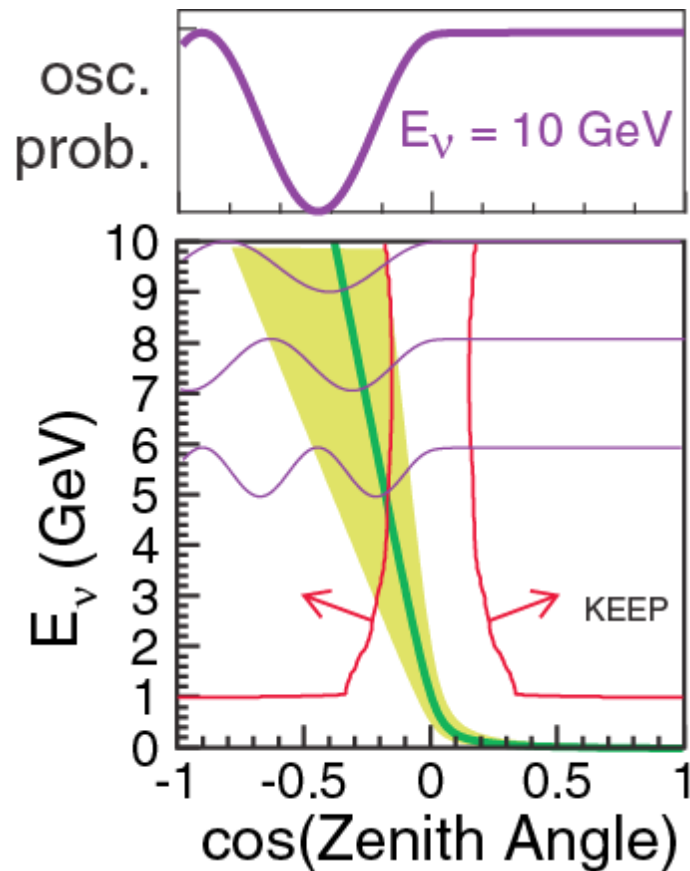
$134 \pm 48^{+16}_{-27}$  events in excess

*cf.*  $78 \pm 27$  excess events expected

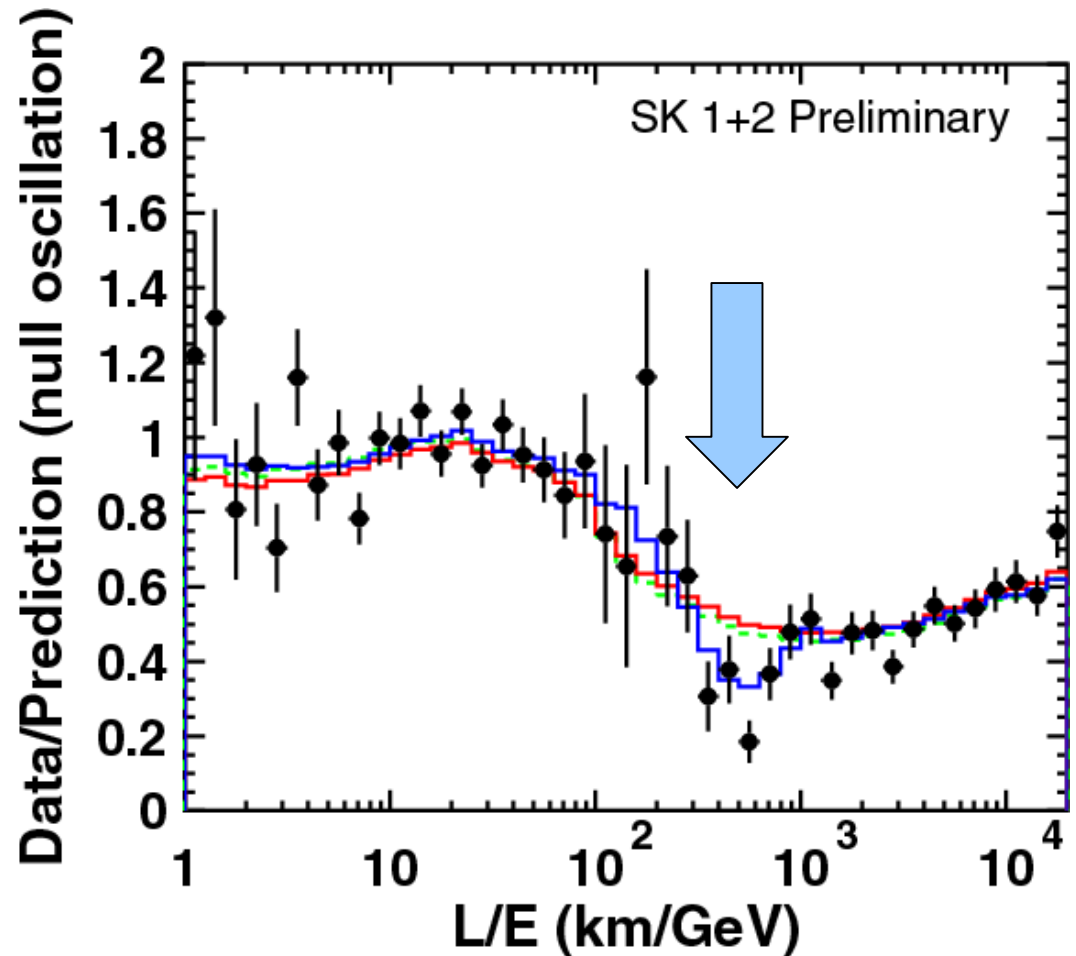
$\sim 2.4\sigma$  effect



## What about the oscillation pattern?



Expand Fiducial Volume  
Keep events with good L/E resolution



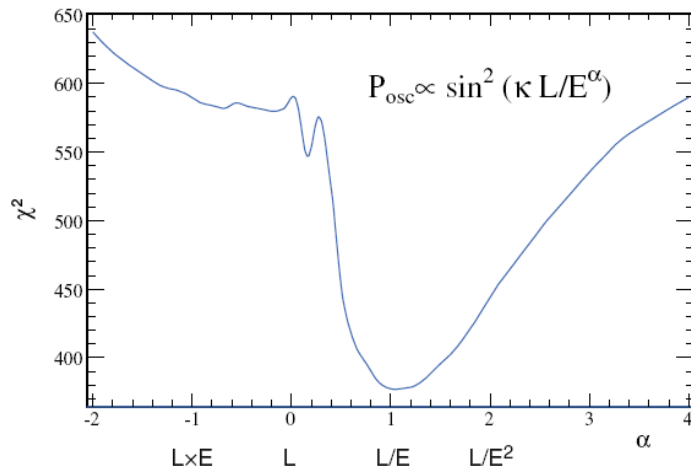


the DoDo & Given

by G. EDWARDS

F.R.S. AD. 1759.





## Lorentz Invariance Violation? Weak Equivalence Principle, CPT Invariance Violation?

Best fit is at  $L/E^1$ .

$\Delta\chi^2 > 100$  disfavored by  $> 10\sigma$

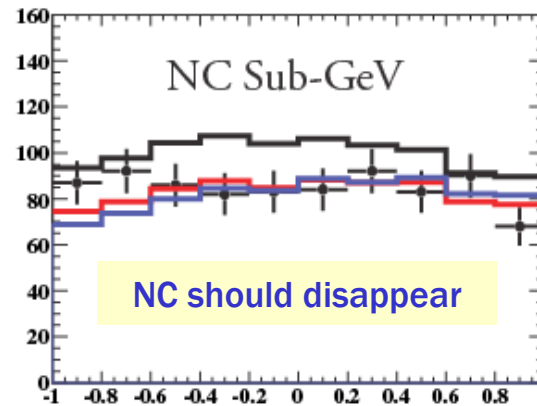
## Sterile Neutrinos?

$$\nu_\mu \leftrightarrow \nu_{sterile} \quad \chi^2 = 513.5 / 438 \text{ DOF}$$

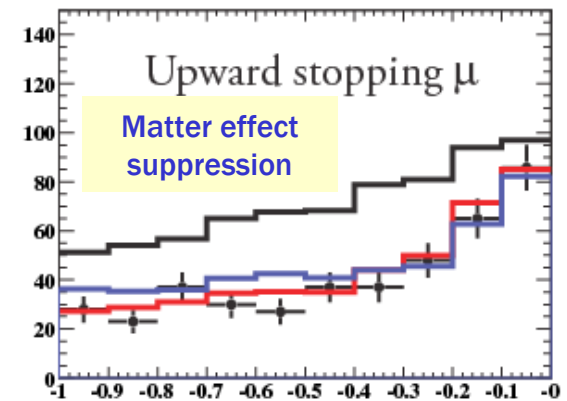
$$\nu_\mu \leftrightarrow \nu_\tau \quad \chi^2 = 481.5 / 438 \text{ DOF}$$

$$\Delta\chi^2 = 31$$

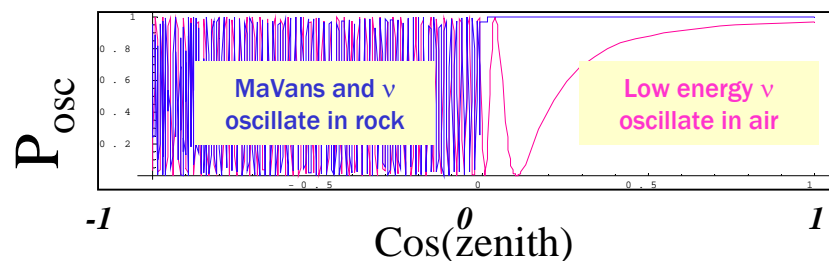
$$\sqrt{\Delta\chi^2} = 5.6\sigma$$



Blue:  $\mu$ -sterile



cosine of zenith angle



$$\Delta\chi^2 = 19.5$$

$$4.4\sigma$$

## MaVaNs?

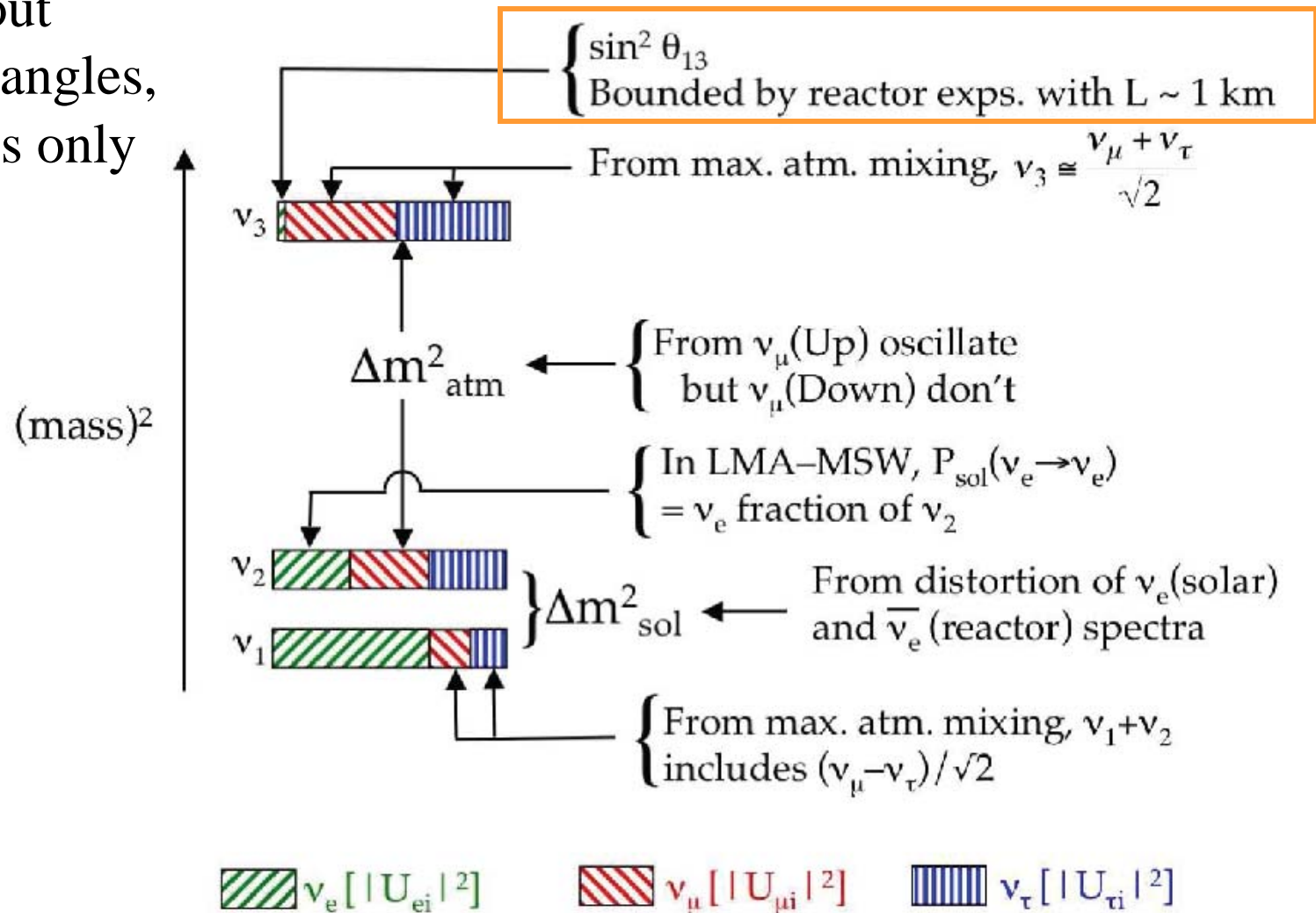
hep-ph/0401099 – Dark energy related scalar field causes  $\rho$  dependent  $\Delta m^2$







We know a certain amount about the mixing angles, except  $\theta_{13}$  is only bounded.



By B. Kayser

# Neutrino Mixing Matrix Parameterization

times Majorana Phases (not shown)

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \times \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \times \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$\theta_{23} \sim \theta_{atm.} \approx 45^\circ$$

$$\theta_{13} < 12^\circ$$

$$\theta_{12} \sim \theta_{solar} \approx 32^\circ$$

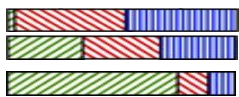
$\delta$  is totally unknown

WHY??

$$U_{CKM} = \begin{pmatrix} 1 & 0.2 & 0.005 \\ 0.2 & 1 & 0.04 \\ 0.005 & 0.04 & 1 \end{pmatrix} \quad U_{PMNS} = \begin{pmatrix} 0.8 & 0.5 & ? \\ 0.4 & 0.6 & 0.7 \\ 0.4 & 0.6 & 0.7 \end{pmatrix}$$

We know the neutrino is much lighter than the quarks and leptons, and we have measured the mass splittings pretty well. The most massive must have  $m > 0.05 \text{ eV}$  ( $\sqrt{\Delta m_{atm}^2}$ ). We know the hierarchy between 1 and 2. But we don't know:

**Degenerate**



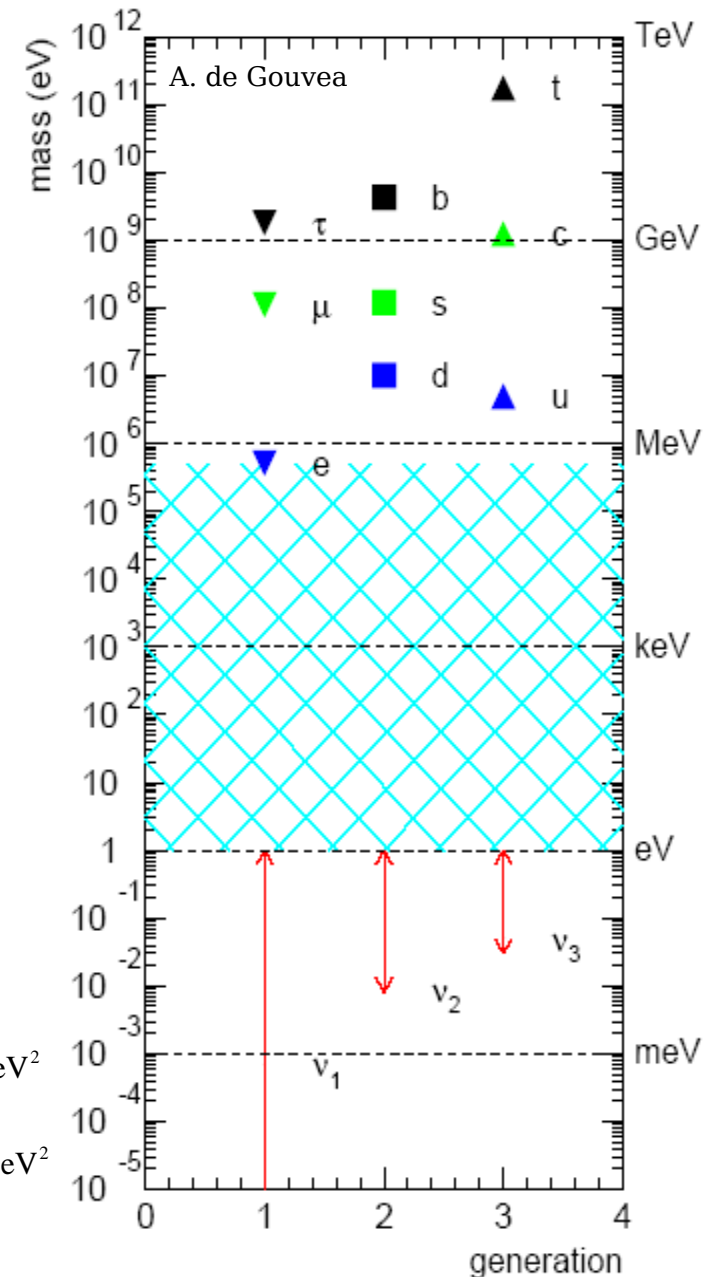
**Inverted hierarchy**



**Normal hierarchy**



$$\left. \begin{array}{l} 2.5 \times 10^{-3} \text{ eV}^2 \\ 7 \times 10^{-5} \text{ eV}^2 \end{array} \right\}$$



## Three Active Neutrinos



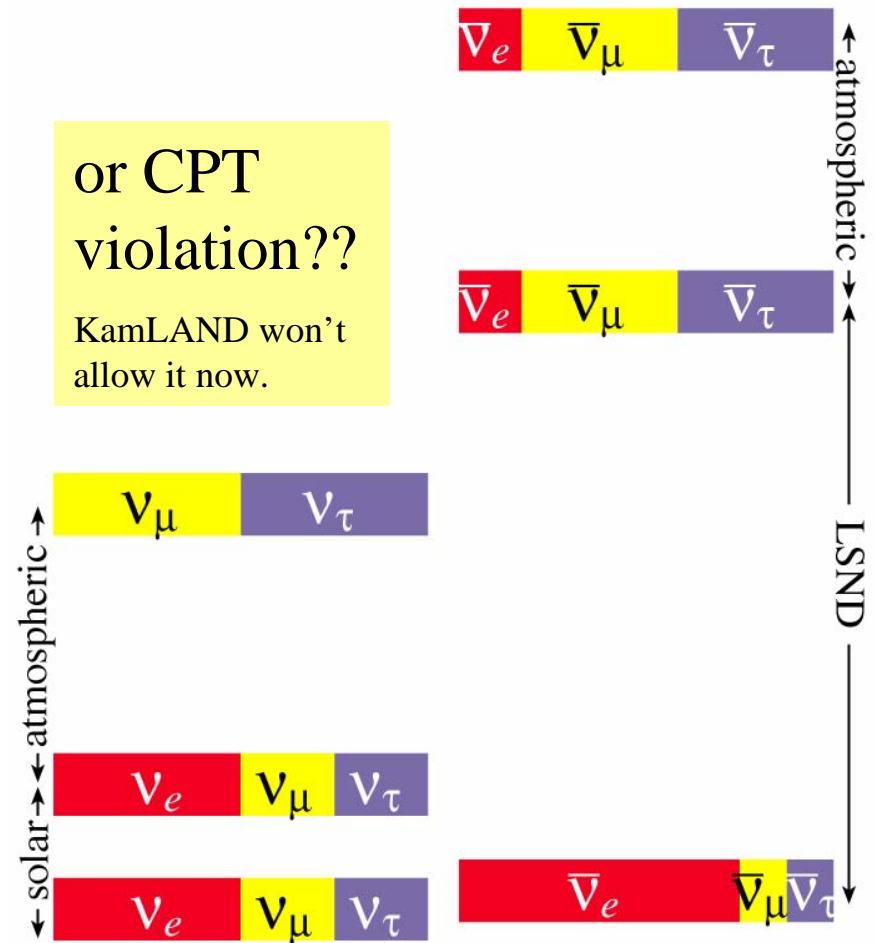
*LSND*:  $\Delta m^2 \sim eV^2$   
*Atmospheric*:  $\Delta m^2 \sim 2.5 \times 10^{-3} eV^2$   
*Solar*:  $\Delta m^2 \sim 8 \times 10^{-5} eV^2$

**Pick any two!**

or a sterile  
neutrino??

or CPT  
violation??

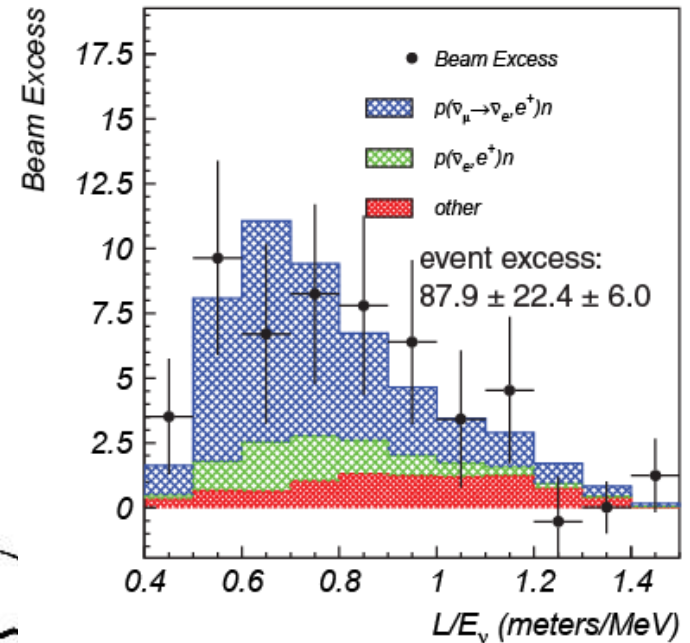
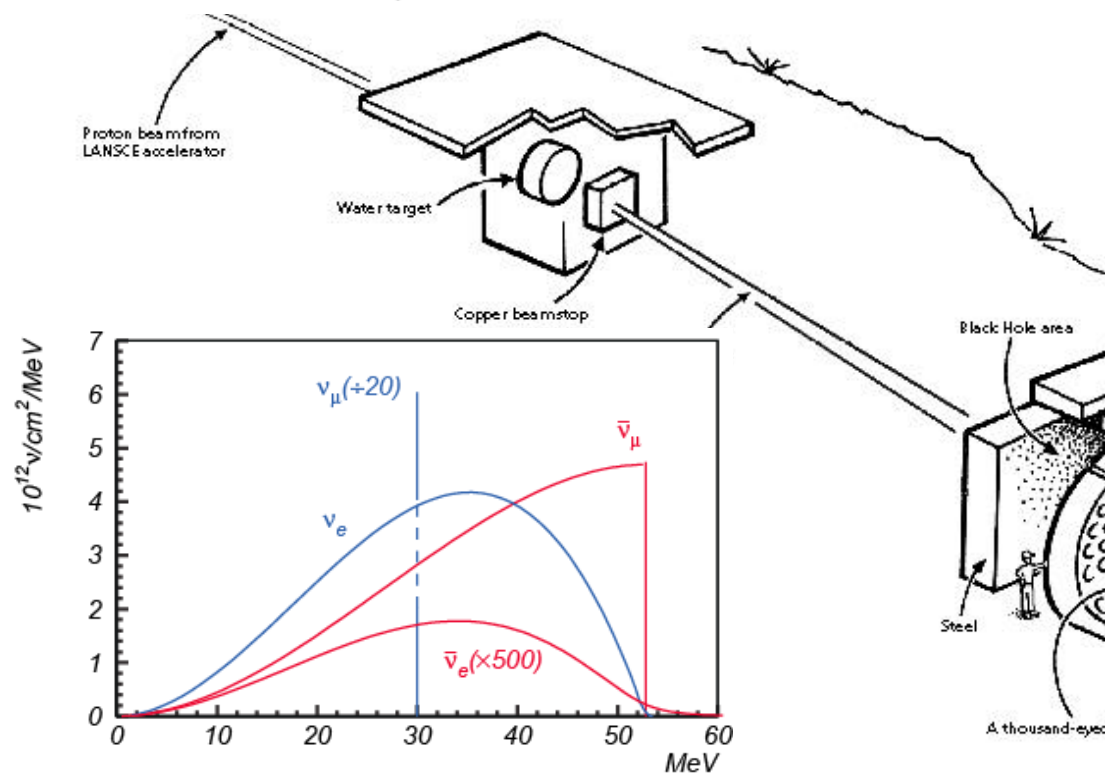
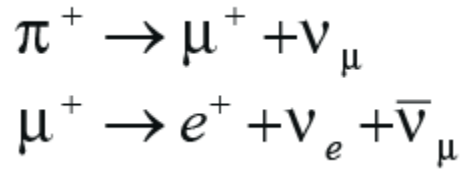
KamLAND won't  
allow it now.



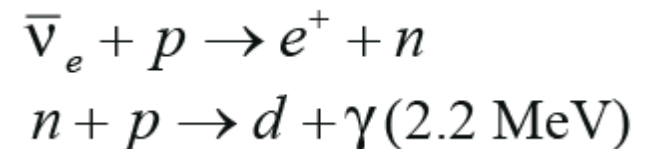
H. Murayama

stopped pion beam  $\Rightarrow$   
decay-at-rest spectra:

# LSND



- +/- Weakly significant ( $3.8\sigma$ )
- + No known defect
- Complementary experiment, KARMEN, sees no effect (+ but with less sensitivity)

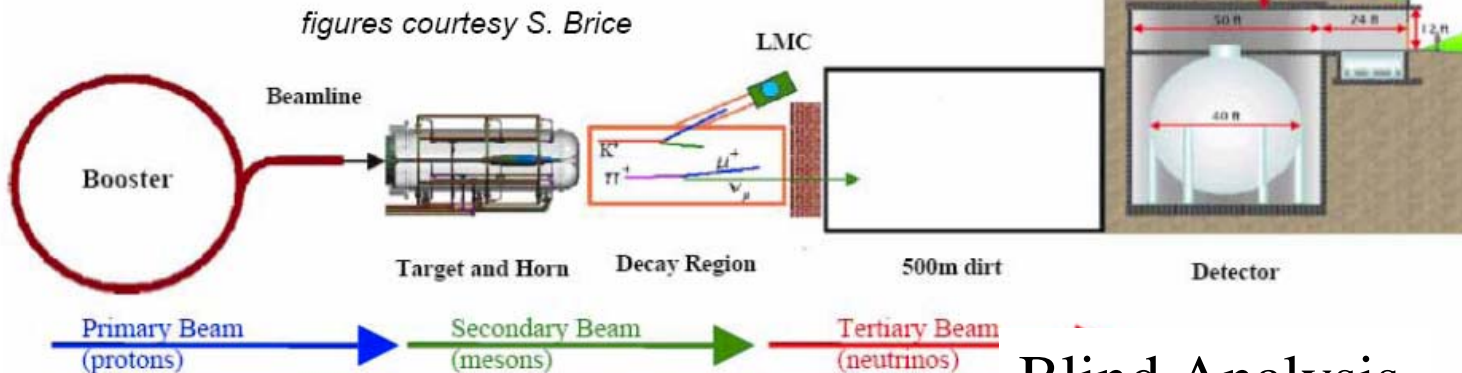


# MiniBooNE

$L = 540 \text{ m}$  ( $10 \times \text{LSND}$ )

$E = 500 \text{ MeV}$  ( $10 \times \text{LSND}$ )

$\nu_\mu$  not  $\bar{\nu}_\mu$

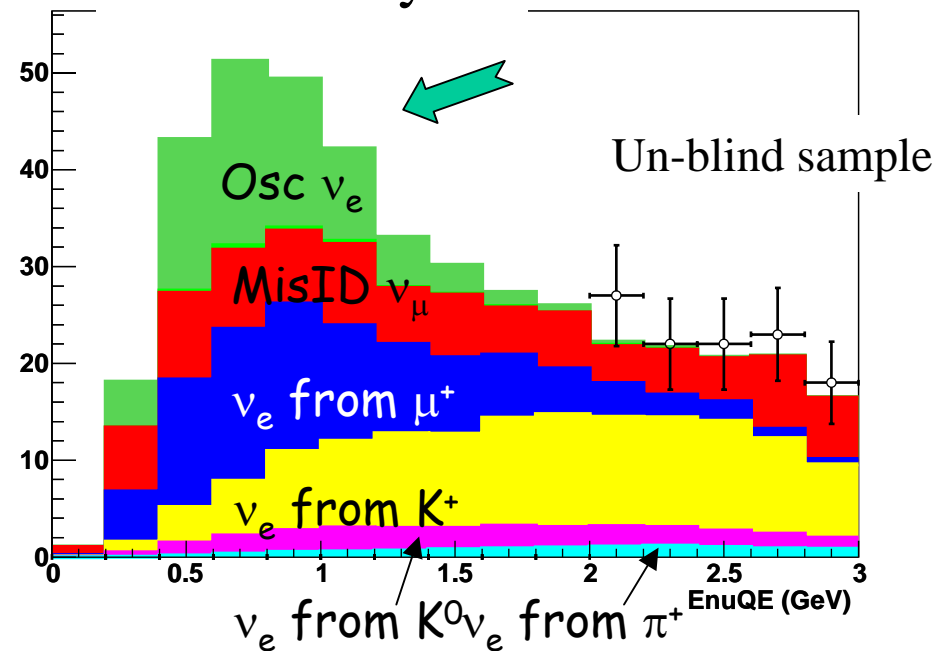


950 kl of pure mineral oil  
Cherenkov+scintillation  
1280 PMTs

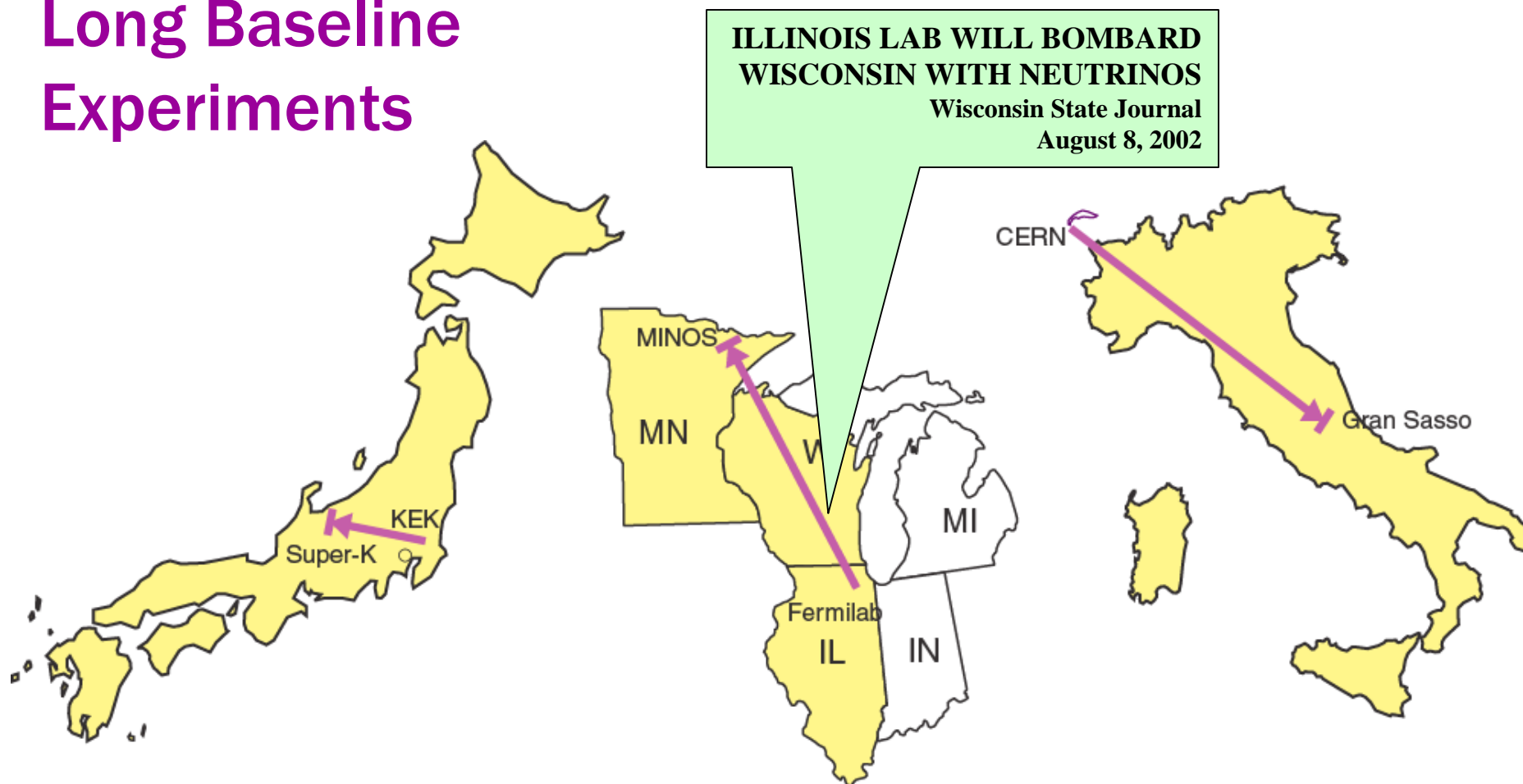
## STATUS:

- $7.2 \times 10^{20}$  pot
- anti- $\nu$  since Jan. 2006
- Expect result “real soon now”
- Important to be unambiguous and correct!

## Blind Analysis



# Long Baseline Experiments



**KEK - Kamioka (K2K)**  
~1 GeV neutrinos  
L=250 km  
1999-2004

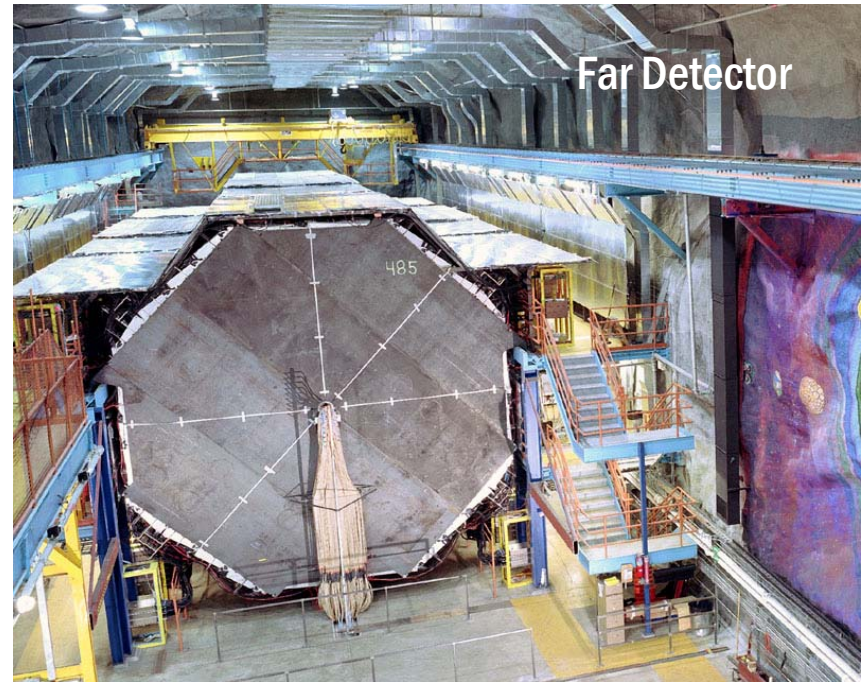
**Fermilab - Sudbury (MINOS)**  
~3 GeV neutrinos  
L=735 km  
Started 2005

**CERN - Gran Sasso (Opera/ICARUS)**  
~17 GeV neutrinos (broadband)  
L=732 km  
Starts in 2006



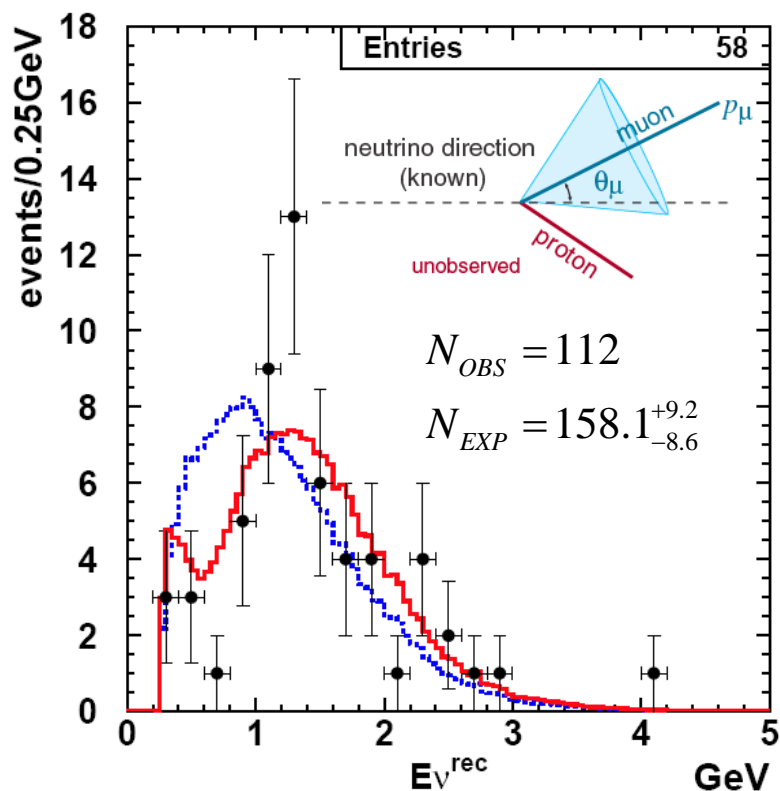
# MINOS

120 GeV protons,  $4 \times 10^{13}$  ppp, 1.87 s cycle  
0.4 MW beam power  
1 kton near detector  
5.4 kton far detector  
484 steel/scintillator planes  
1.2 T solenoidal magnetic field  
750 km baseline, peak energy  $\sim 3$  GeV  
 $92\% \nu_\mu$ ,  $1.5\% \nu_e/\nu_{\bar{e}}$



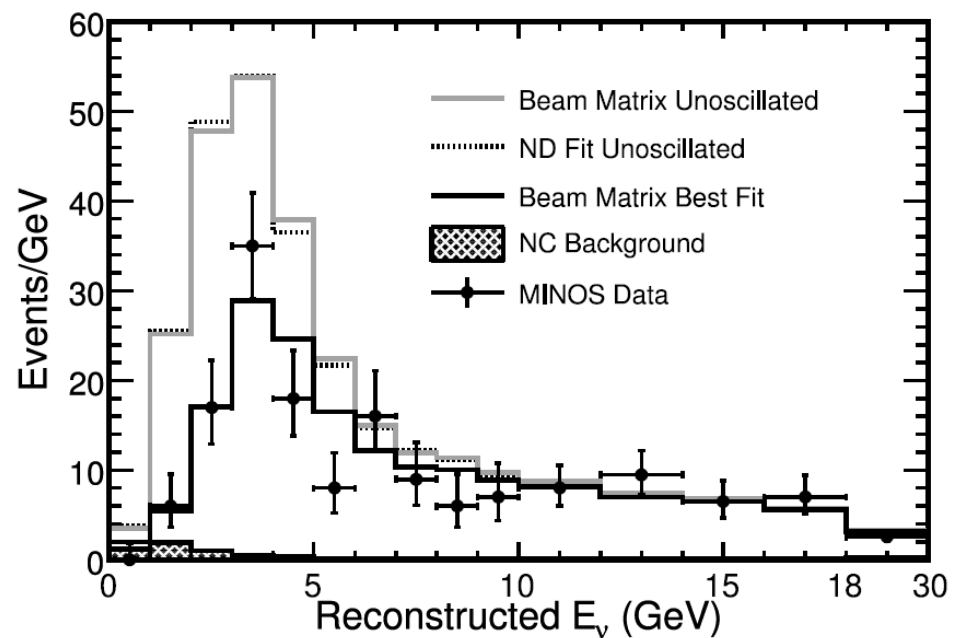


# Final results from K2K



> 4 $\sigma$  confirmation of atmospheric neutrino mixing

# First results from MINOS



$$\Delta m_{32}^2 = 2.74^{+0.44}_{-0.26} \times 10^{-3} \text{ eV}^2$$

$$\sin^2 2\theta_{23} > 0.87 \text{ (68\% CL)}$$

# $\theta_{13}$ – Gateway Parameter

$$\begin{aligned}
 P_{vac\pm}[\nu_\mu(\bar{\nu}_\mu) \rightarrow \nu_e(\bar{\nu}_e)] = & \sin^2 2\theta_{13} s_{23}^2 \sin^2 \left( \frac{\Delta m_{13}^2 L}{4E} \right) \\
 & - \frac{1}{2} s_{12}^2 \sin^2 2\theta_{13} s_{23}^2 \left( \frac{\Delta m_{12}^2 L}{2E} \right) \sin \left( \frac{\Delta m_{13}^2 L}{2E} \right) \\
 & + 2J_r \cos \delta \left( \frac{\Delta m_{12}^2 L}{2E} \right) \sin \left( \frac{\Delta m_{13}^2 L}{2E} \right) \\
 J_r = c_{12} s_{12} c_{13}^2 s_{13} c_{23} s_{23} \quad & \mp 4J_r \sin \delta \left( \frac{\Delta m_{12}^2 L}{2E} \right) \sin^2 \left( \frac{\Delta m_{13}^2 L}{4E} \right),
 \end{aligned}$$

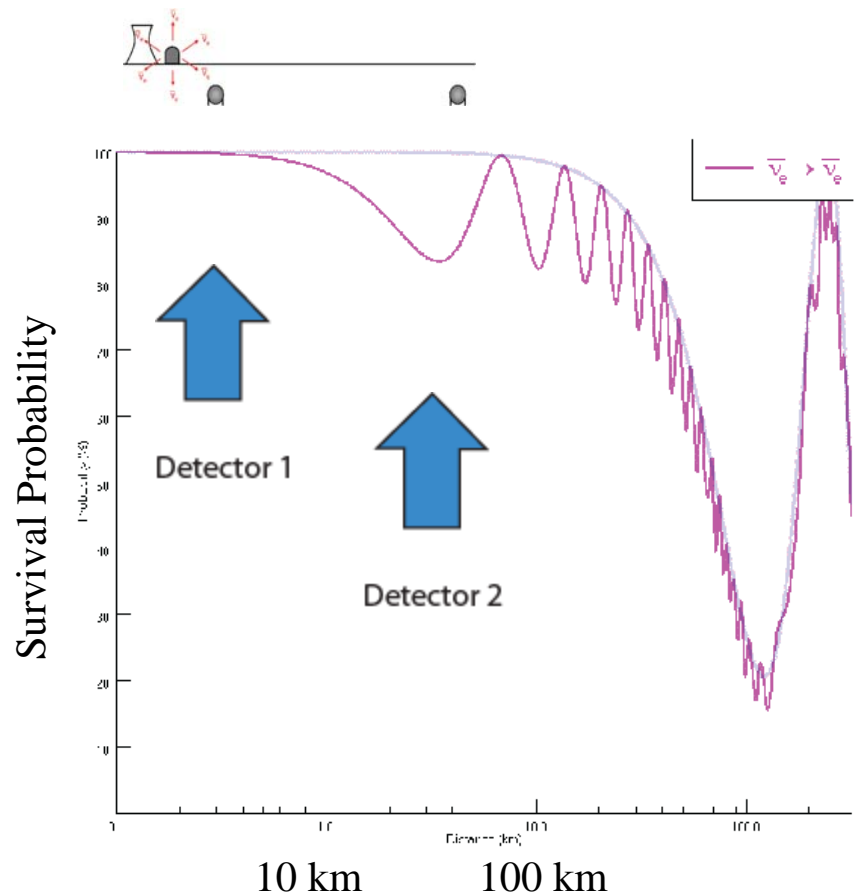


CP violating phase

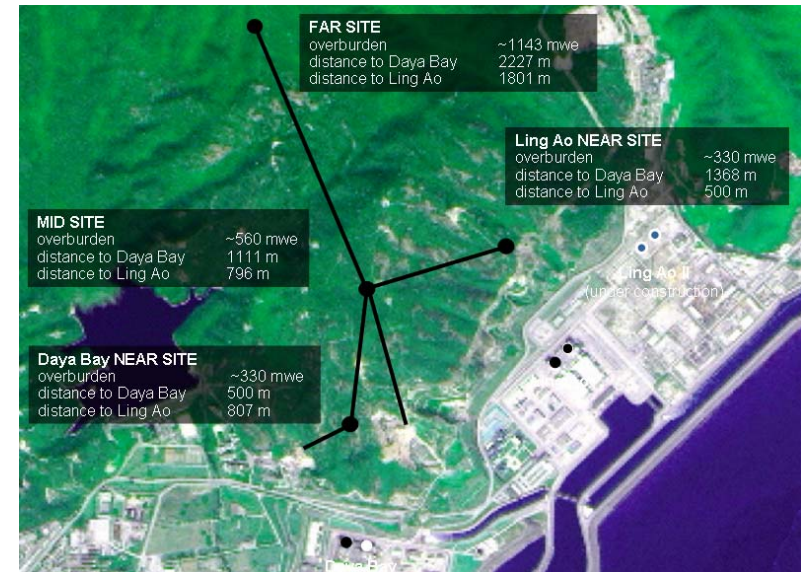
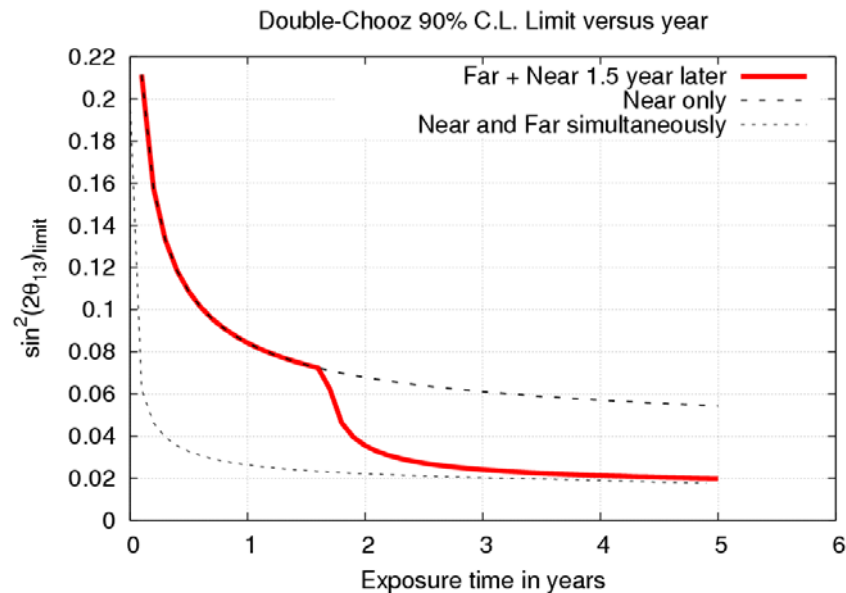
+ terms in matter effect

# Precision Reactor Experiments

$$P_{ee} \rightarrow 1 - \left( \sin^2 2\theta_{13} \sin^2 \frac{\Delta m_{31}^2 L}{4E} + \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \frac{\Delta m_{21}^2 L}{4E} \right)$$



- only depends on  $\theta_{13}$ , not  $\delta$  or hierarchy
- Requires careful control of systematics  $> 1\%$
- Require multiple detectors
- Require overburden to reduce background
- Can reach  $\sin^2 2\theta \sim 0.01$



## Double Chooz (France):

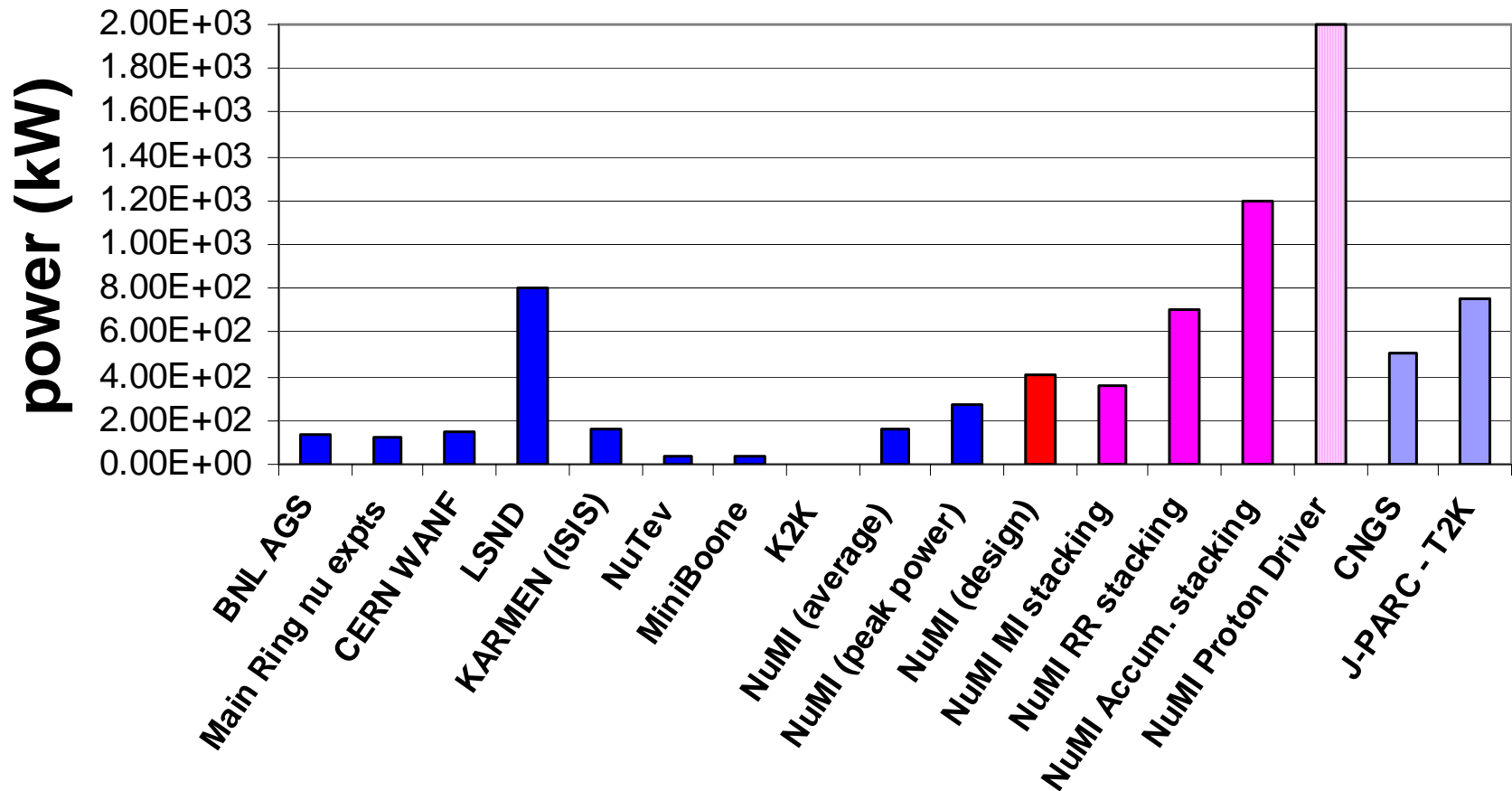
- 2 x 4 GW reactor cores
- 50-300 mwe overburden
- 0.3/1 km baseline
- Existing infrastructure – early start? (above)
- 2x10 ton modules – fixed
- Goal of 0.6% systematics
- Reach  $\sin^2 2\theta \sim 0.03$

## Daya Bay (Hong Kong):

- 6 reactor cores, 17 GW total
- 200-1000 mwe overburden
- 0.3/1.8-2.2 km baseline
- Construct tunnels and labs (above)
- 8x20 ton modules – moveable
- Goal of 0.36% systematics
- Reach  $\sin^2 2\theta \sim 0.01$

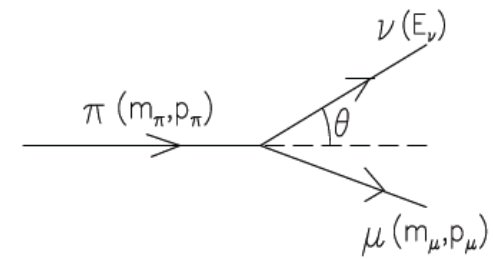
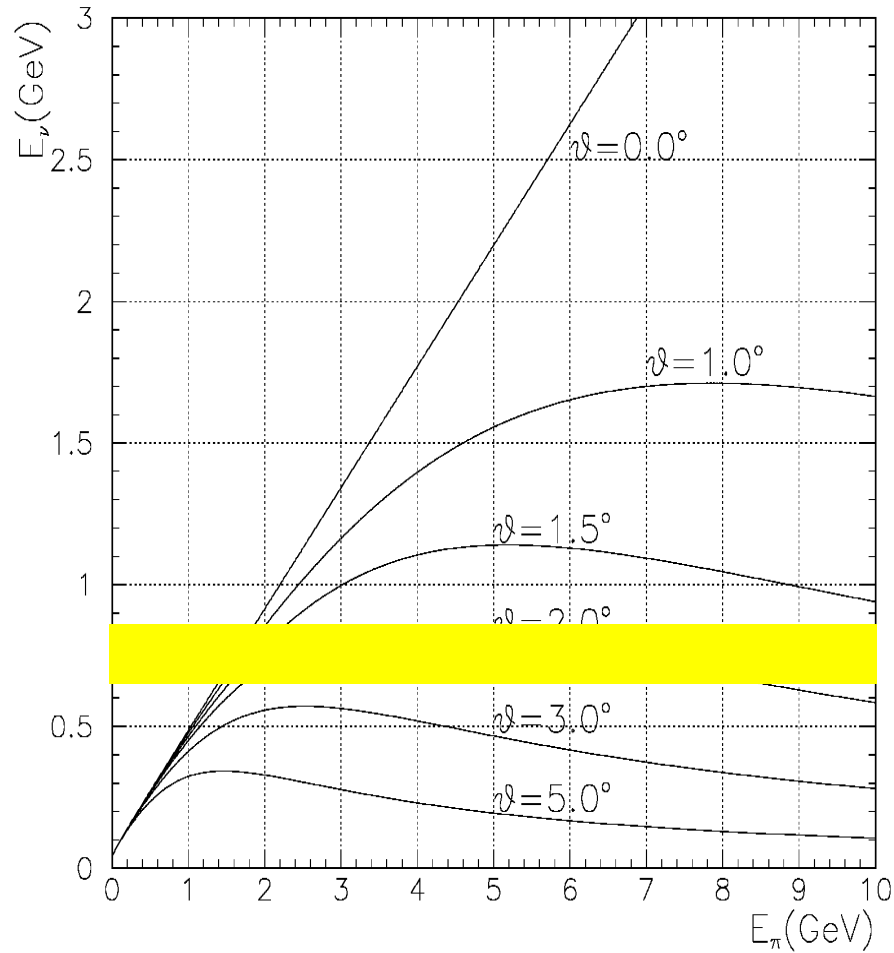
Neutrino flux is roughly proportional to proton beam power.

## Neutrino beams power

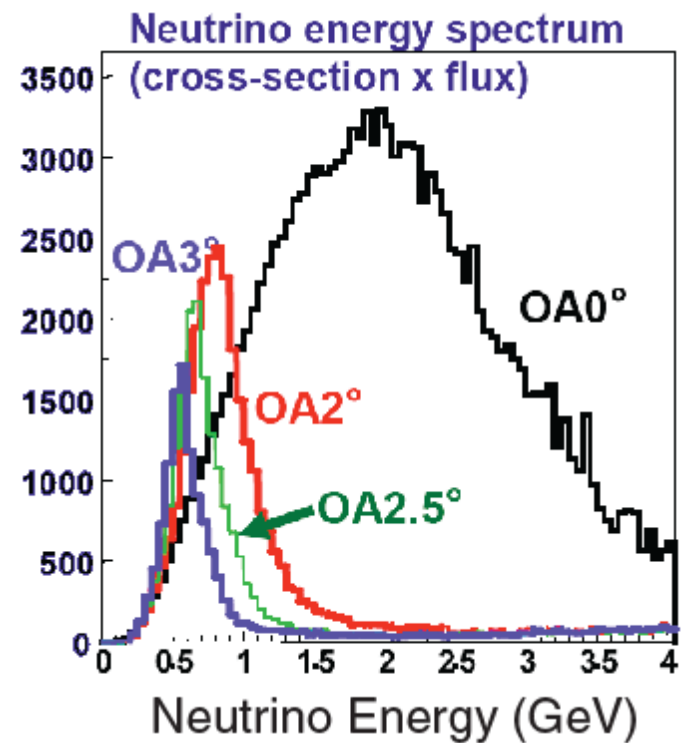


Power[W]=(protons/pulse) $\times$ (energy[eV]) $\times$ (repetition rate[Hz]) $\times$ ( $1.6 \times 10^{-19}$  [C/proton])  
or if available: Power[W]=(beam current[A]) $\times$ (beam energy[eV])

# Off-Axis Technique

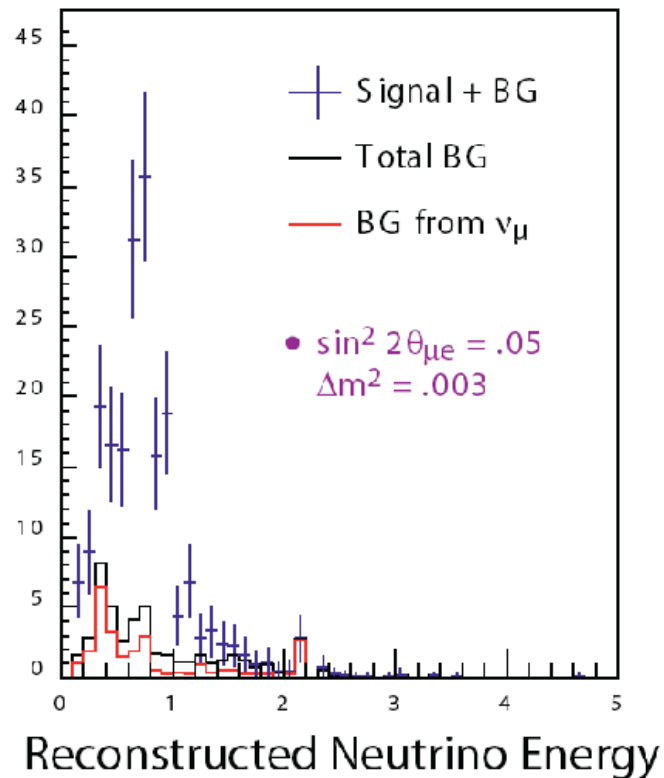


$$E_\nu = \frac{m_\pi^2 - m_\mu^2}{2(E_\pi - p_\pi \cos \theta)}$$

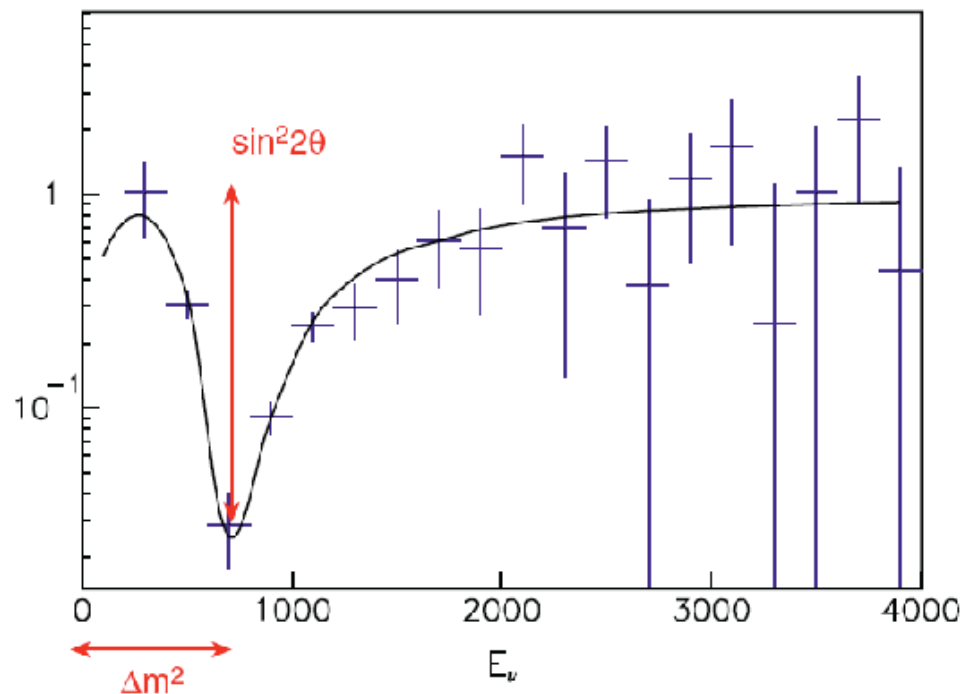


# Physics Goals

Discover  $\nu_e$  appearance (first such result barring LSND/MiniBooNE),  
measuring non-zero  $\theta_{13}$

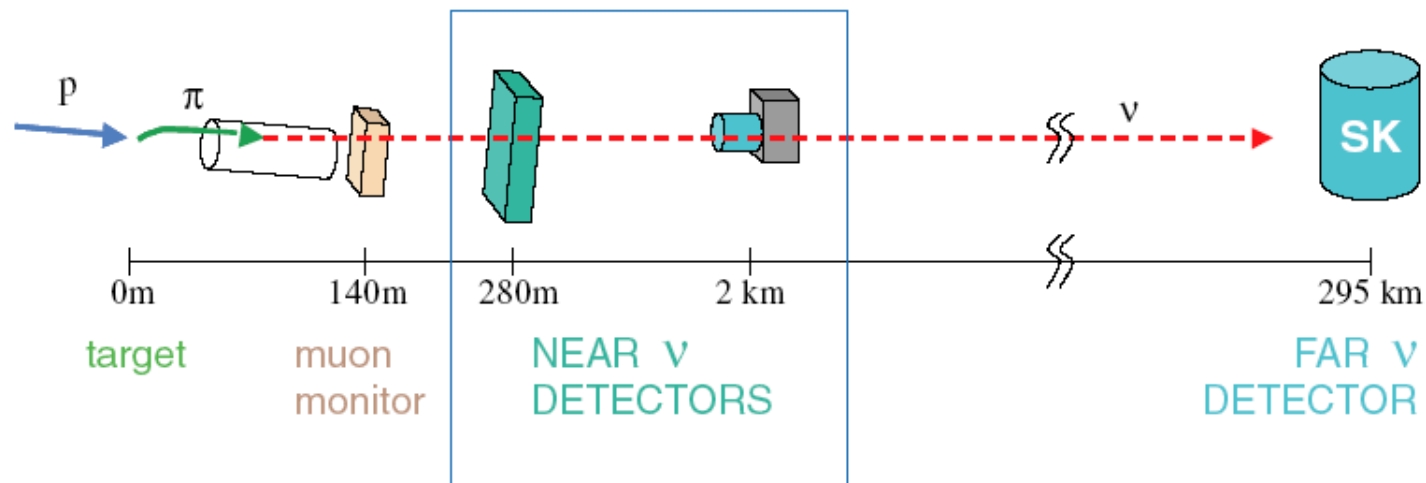


Resolve if  $\theta_{23}$  is non-maximal  
More precisely measure  $\Delta m_{23}^2$





## Phase I: 0.75 MW and Super-Kamiokande

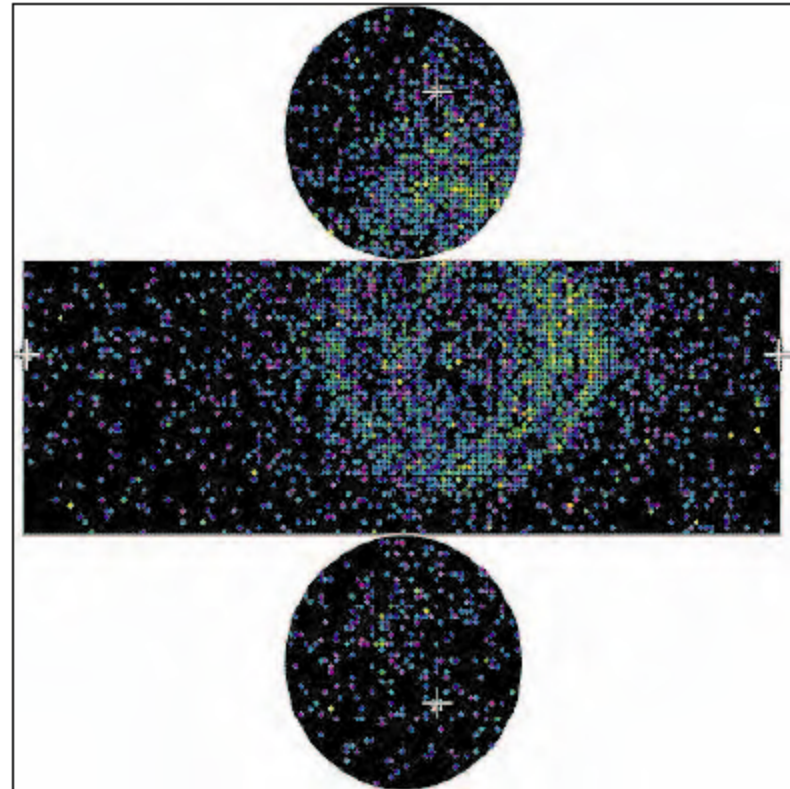
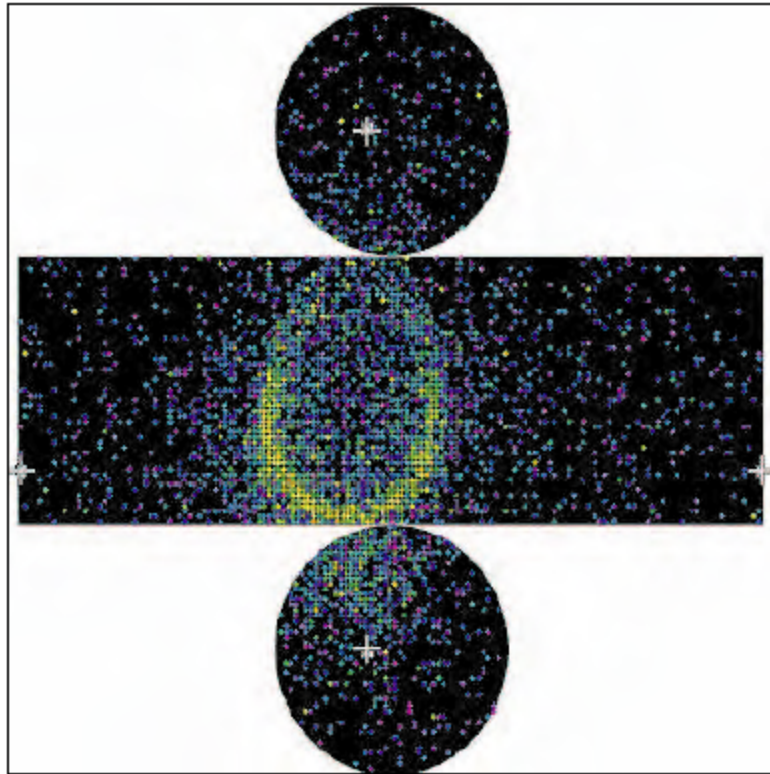




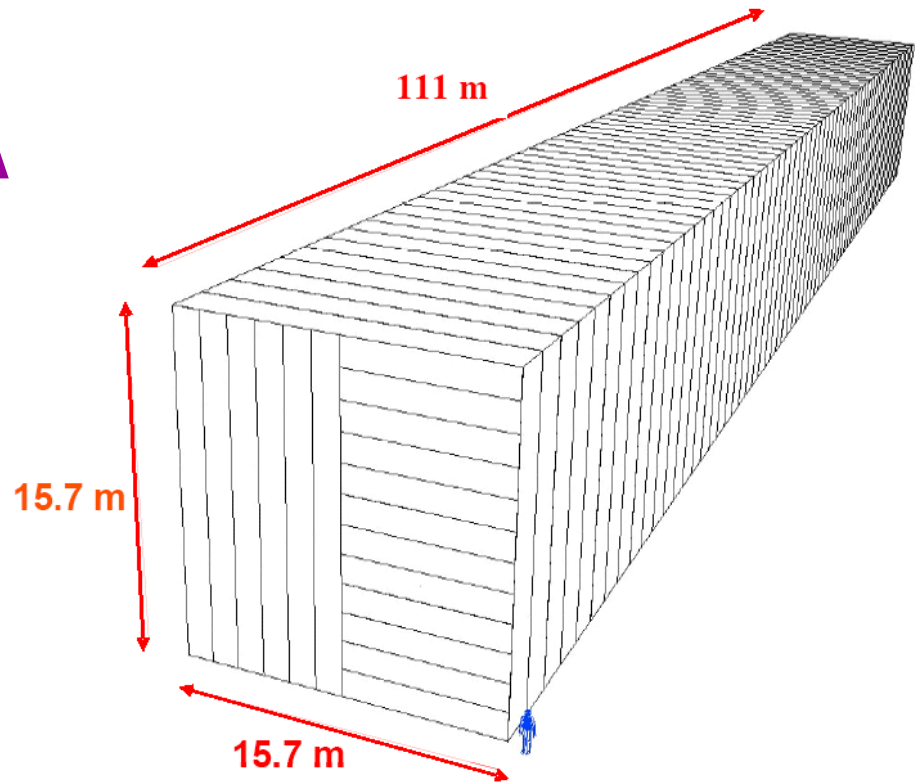
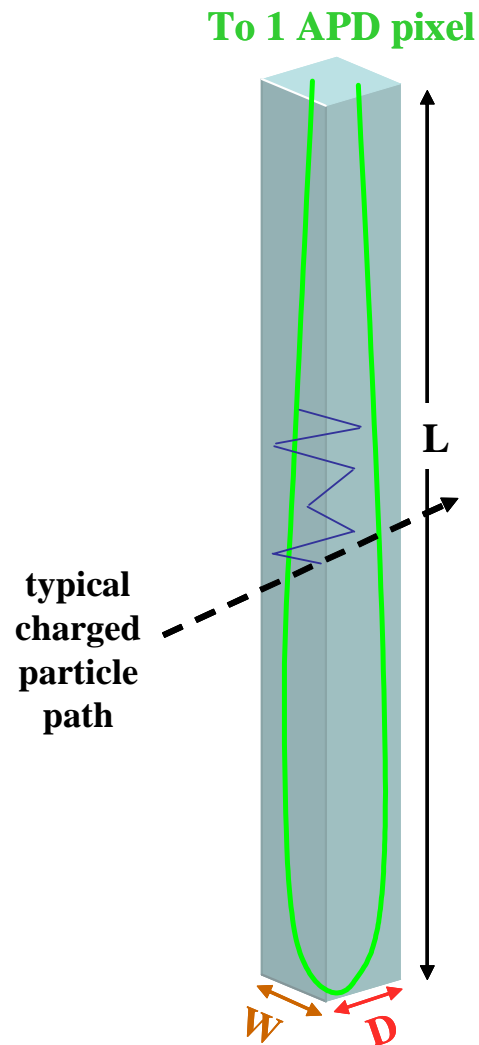
# One is signal, one is background

$$\nu_e + n \rightarrow e^- + p$$

$$\nu_\mu + p \rightarrow \nu_\mu + p + \pi^0$$



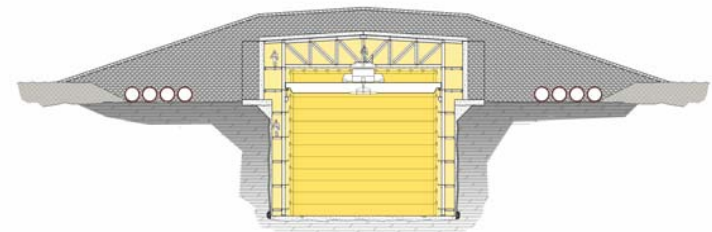
# NOvA



30 (25) kton totally active detector

Planes of liquid scintillator (mineral oil) read by WLS fiber and APD

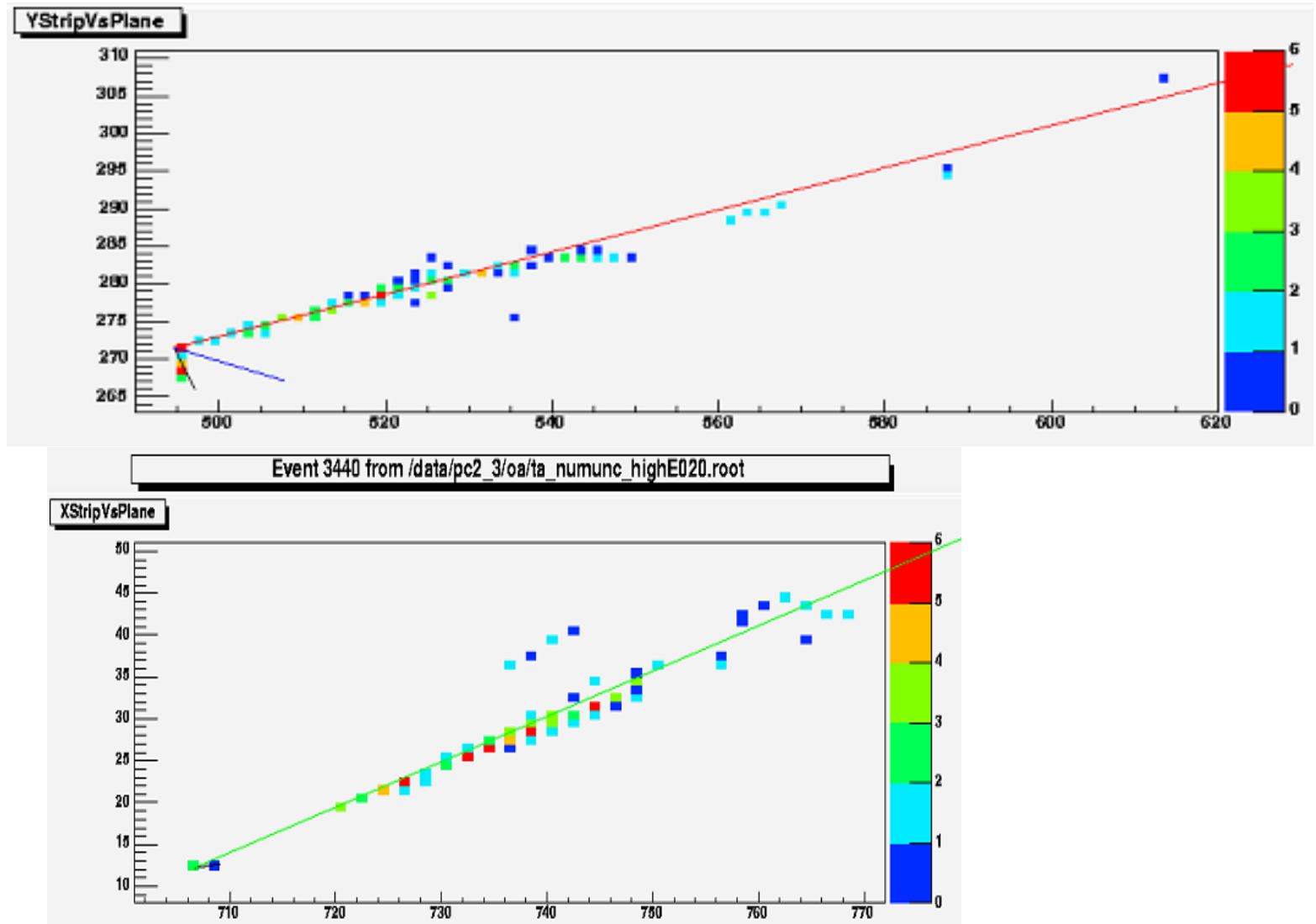
Surface detector with s overburden (right)



# One is signal, one is background

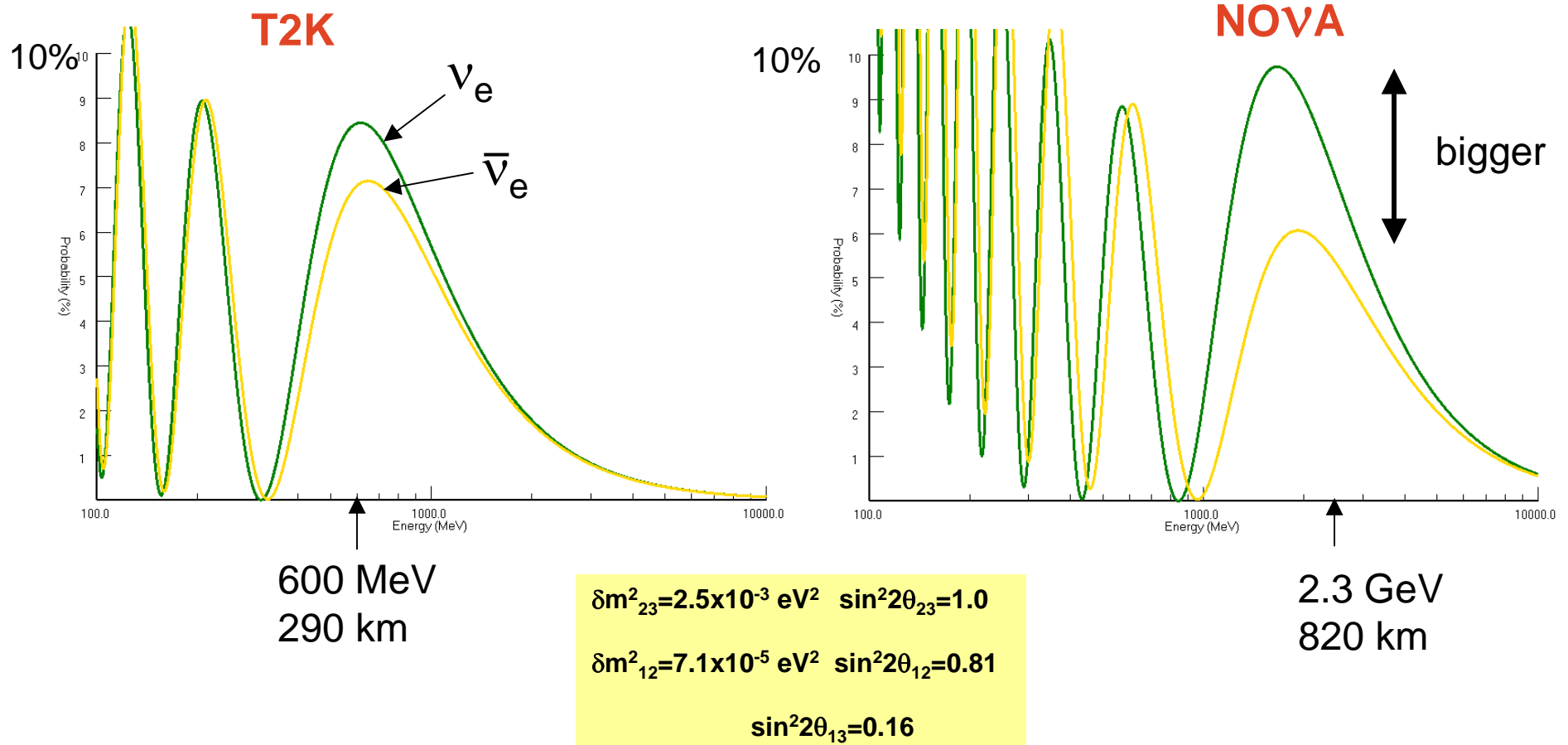
$$\nu_e + p \rightarrow e^- + p + \pi^+$$

$$\nu_\mu + N \rightarrow \nu_\mu + p + \pi^0$$



# Resolving the Mass Hierarchy

Matter effect enhances  $\nu_e$  appearance for normal hierarchy  
 Effect is reversed (enhanced anti- $\nu_e$ ) for inverted hierarchy





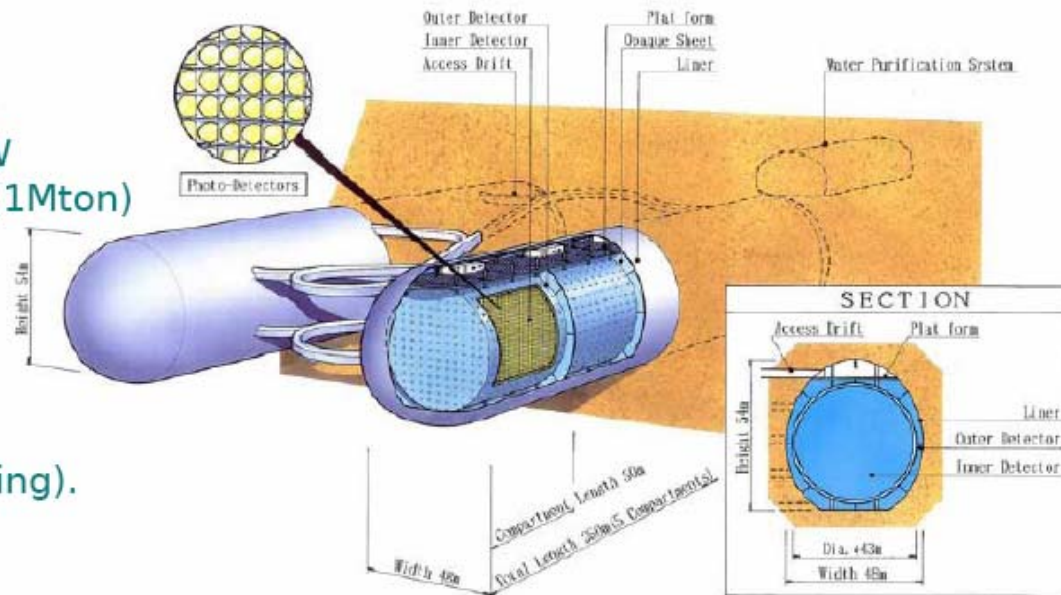
# Beyond T2K and NOvA

## T2K PHASE-II

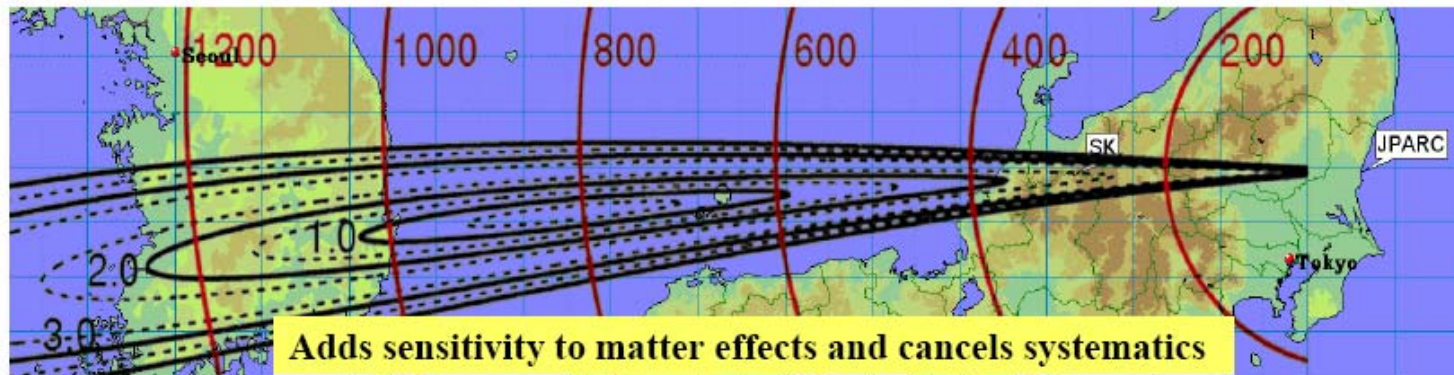
JPARC .77 MW  $\rightarrow$  4MW  
SK (50kT)  $\rightarrow$  Hyper-K(1Mton)

## GOAL:

Measure CP Violation  
(use  $\nu$  and anti- $\nu$  running).

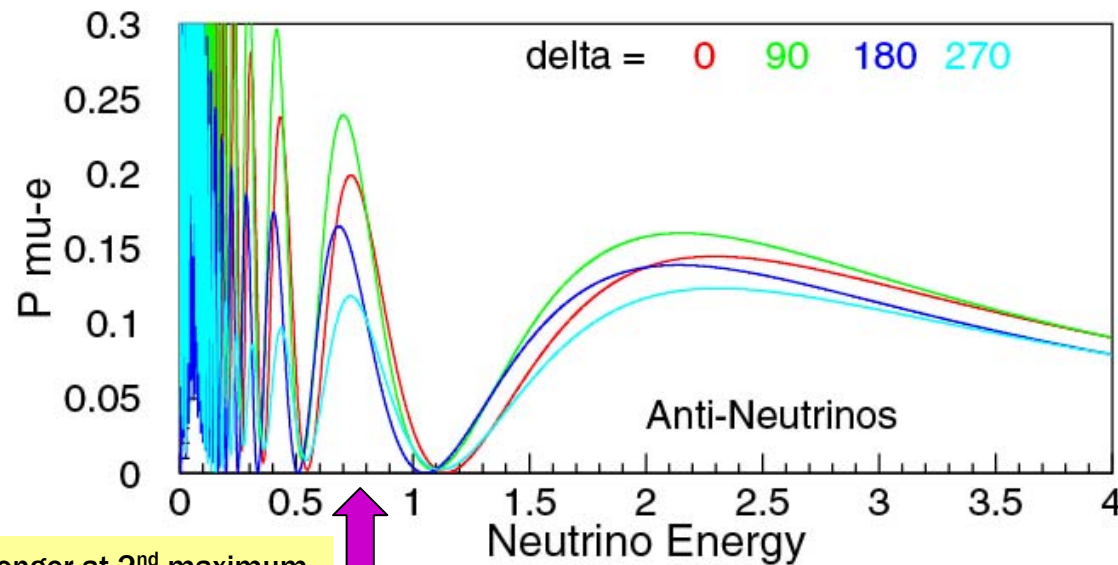
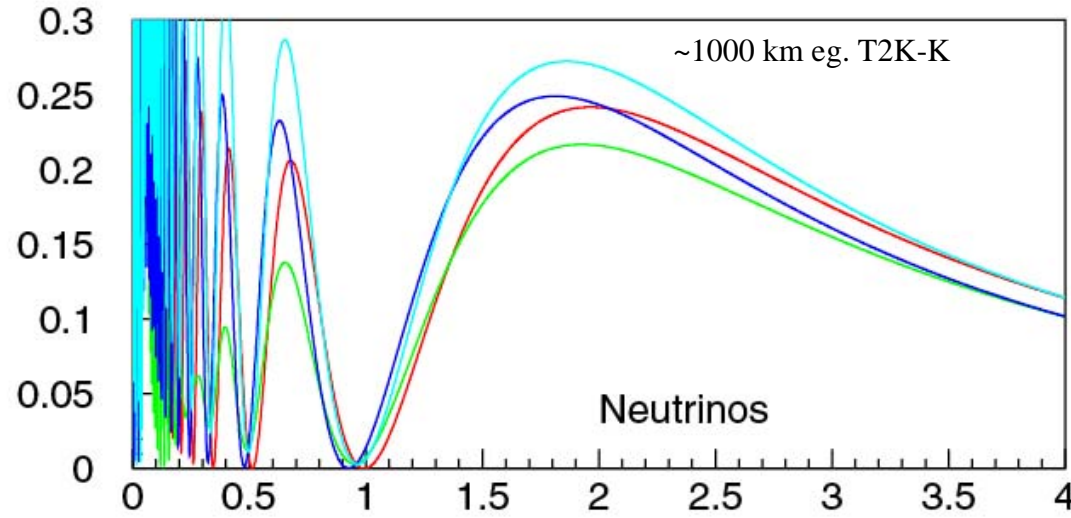


**Idea under study: Put  $\frac{1}{2}$  of Hyper-K in Korea.**



$$P(\nu_{\mu} \rightarrow \nu_e) \neq P(\bar{\nu}_{\mu} \rightarrow \bar{\nu}_e)$$

**A.K.A.  
CP  
Violation**



CP Asymmetry stronger at 2<sup>nd</sup> maximum

# To do list:

- Are there only three neutrino states? (LSND)
  - mini-BooNE Real soon- 2006?!
- Can we really make an appearance experiment?
  - CNGS, SK? ( $\tau$ ); T2K, NOvA ( $e$ )
- What is the absolute mass scale?
  - KATRIN,  $0\nu\beta\beta$ , precision cosmology?
- Are neutrinos their own antiparticle? (Majorana)
  - Numerous  $0\nu\beta\beta$  experiments being proposed
- What is the sign of the large  $\Delta m^2$ ? (heirarchy  $\overline{\overline{=}}$  or  $\overline{=}$  )
  - NOvA + T2K
- What is the value of  $\theta_{23}$ ? Is it truly maximal?
  - NOvA, T2K
- What is the value of  $\theta_{13}$ ? Is it really zero?
  - NOvA, T2K, new reactor experiment
- What is the value of  $\delta$ ?
  - upgraded off-axis experiments (eg. Hyper-K+4MW beam)



There was something unusual about this neutrino talk compared to many other neutrino talks you may have seen. Did you discern it?

### No contours!

This is not because contours (confidence intervals) are bad. They are generally a very appropriate way to present a final result, and a very good way of comparing results (i.e. by overlaying them). But contours are fully digested final answers... there is no way to evaluate the character or quality of the **data**. As was mentioned: when reading a paper or proposal, try to find the important plot that characterizes the result, not simply states it. I recently seem to see many talks that seem to show only the contours. It's like seeing a talk that reports only the final numbers (with  $\pm$  errors), and no other details. I imagine 90% of all neutrino physicists can sketch the Chooz contour for  $\sin^2\theta_{23}$ , but many fewer can sketch the data and fit that produced it.

So as an exercise for myself, I made this lecture without contours.

Caveat: one set snuck in- can you find it?