

# Oscillation

Review of neutrino physics - historical trajectory

Quantum mechanics of neutrino oscillation

Positive results from four current experiments

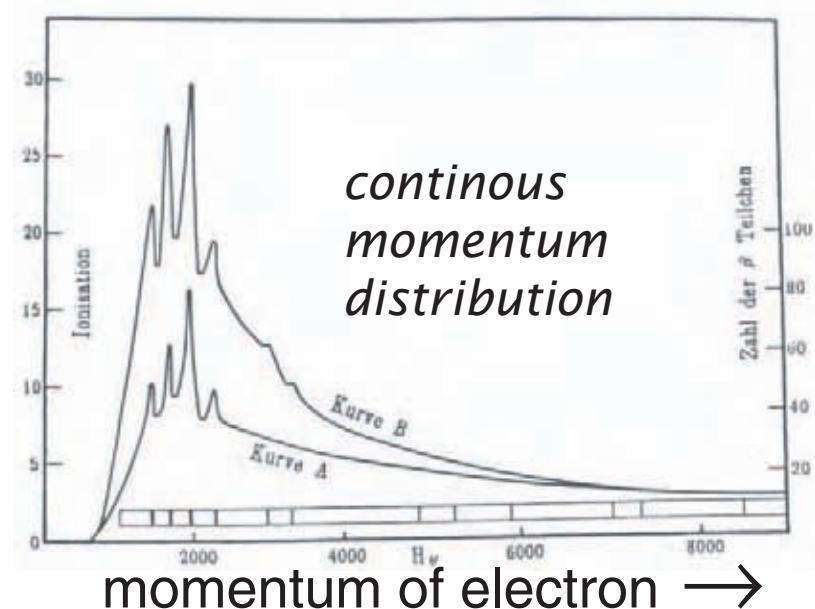
What we know and what we don't know

Your neutrino future

# Pauli's Desperate Remedy

$$n \rightarrow p + e^-$$

*a two-body decay:  
should result in a single  
fixed momentum of the electron*



Abschrift/15.12.56

Offener Brief an die Gruppe der Radioaktiven bei der  
Gauvereins-Tagung zu Tübingen.

Abschrift

Physikalisches Institut  
der Eidg. Technischen Hochschule  
Zürich

Zürich, 4. Dez. 1930  
Gloriastrasse

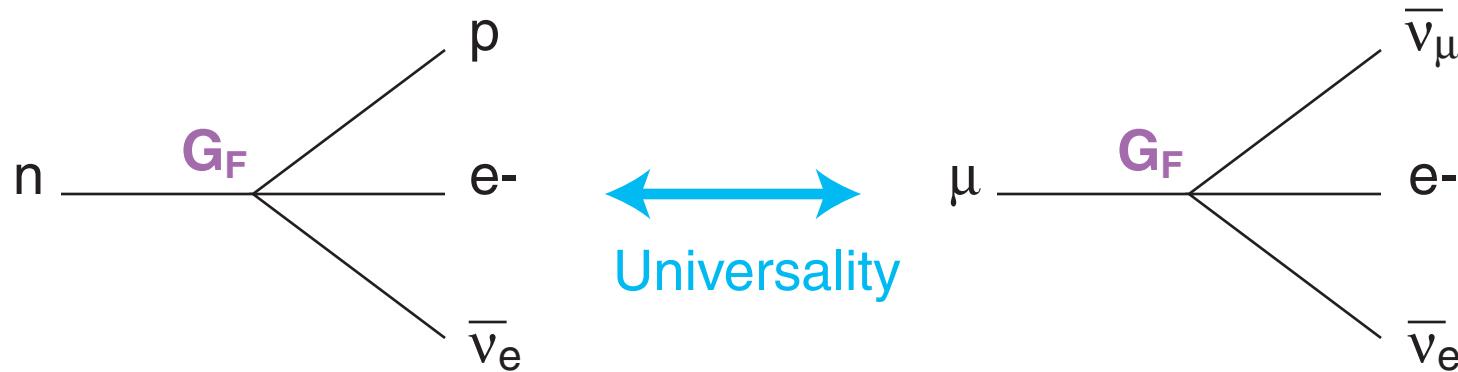
Liebe Radioaktive Damen und Herren,

$$n \rightarrow p + e^- + \nu$$

*Pauli's lightweight neutrino can share energy with  
the electron and explain the continuous distribution.*

# Fermi Coupling Constant

$$G_F = 1.167 \times 10^{-5} \text{ GeV}^{-2}$$



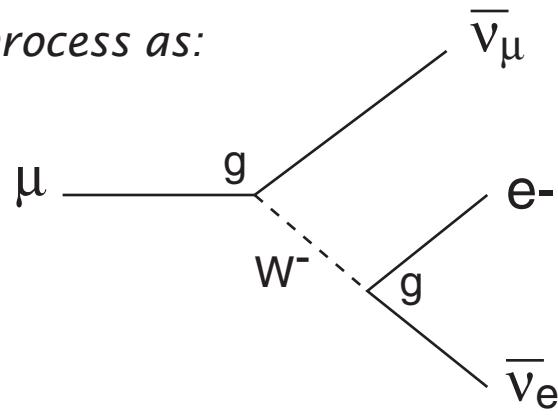
$$\sigma \propto (G_F)^2 [\text{energy}]^2$$

$$s = \sqrt{2M E_\nu}$$

$$\Rightarrow \sigma \propto (G_F)^2 M E_\nu \sim 10^{-38} \text{ cm}^2$$

very small!

*today, we understand the process as:*



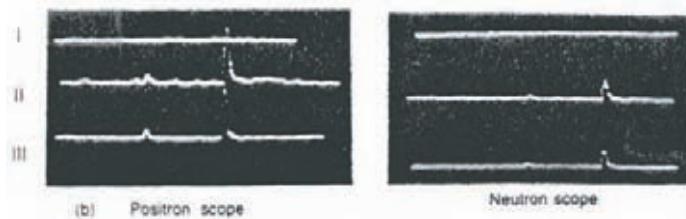
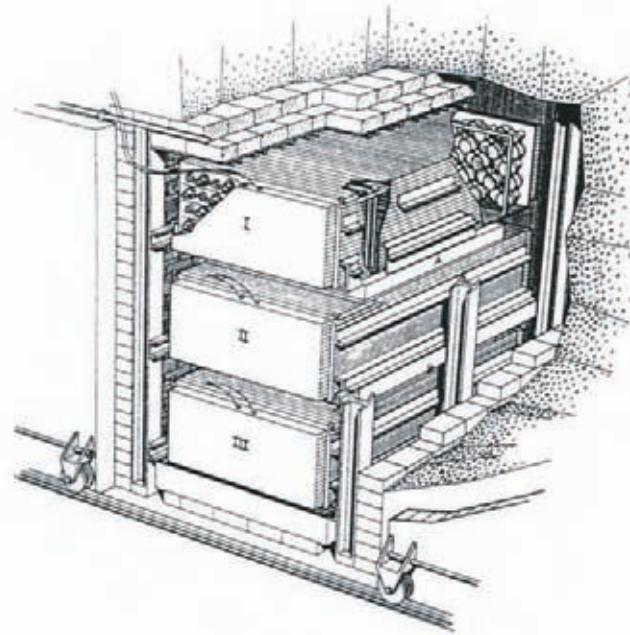
$$G_F = \frac{g^2}{M_W^2}$$

$$\alpha_{\text{weak}} = \frac{g^2}{4\pi}$$

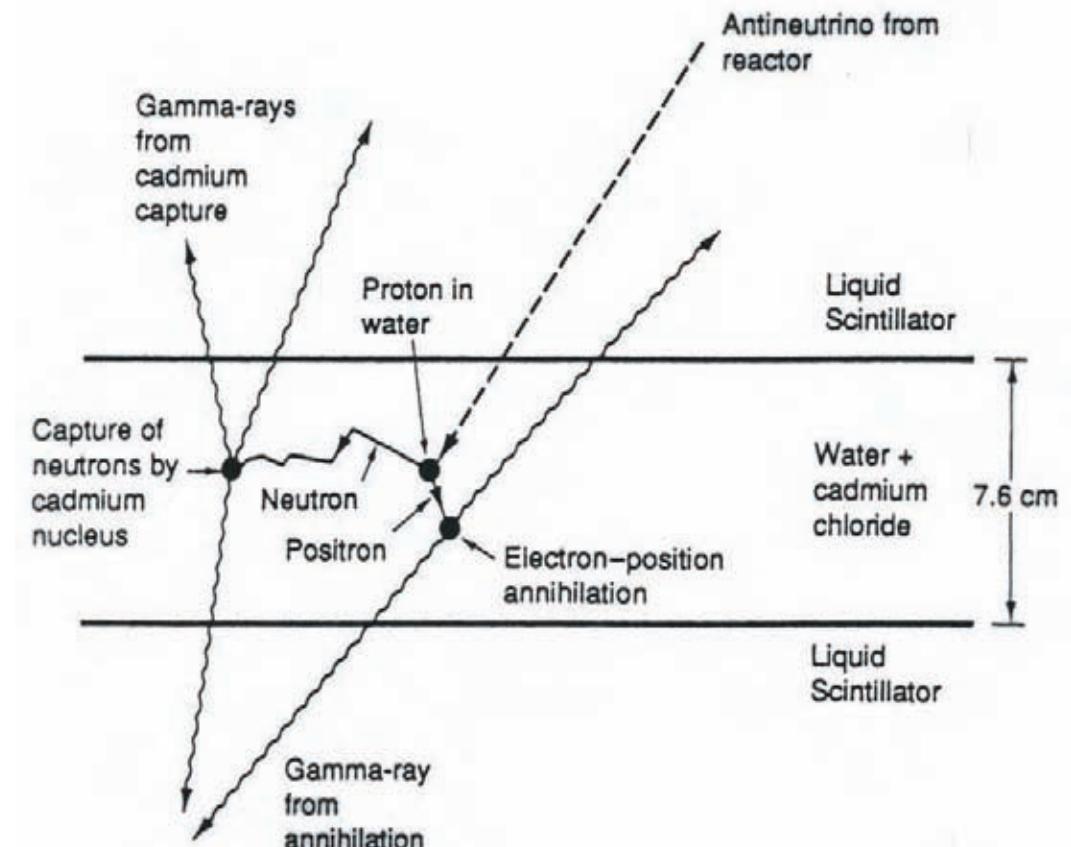
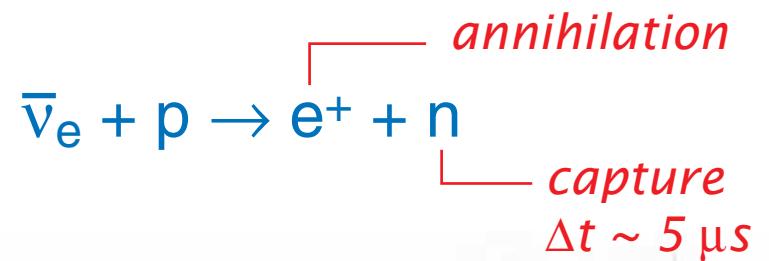
$$\sim 1/29$$

# First Detection of Neutrinos

Reines & Cowen 1956  
Savannah River nuclear reactor



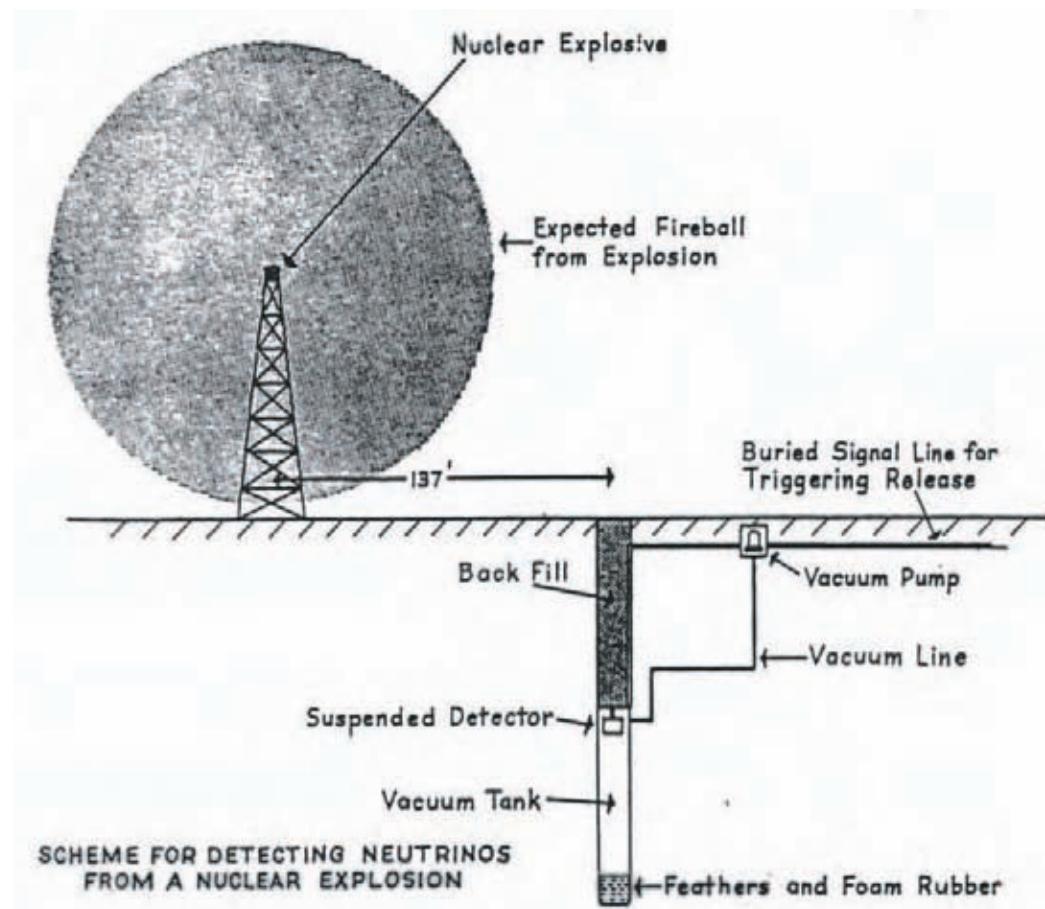
*data recorded by  
oscilloscopes and counters*



*Fred Reines  
1995 Nobel Prize in Physics*

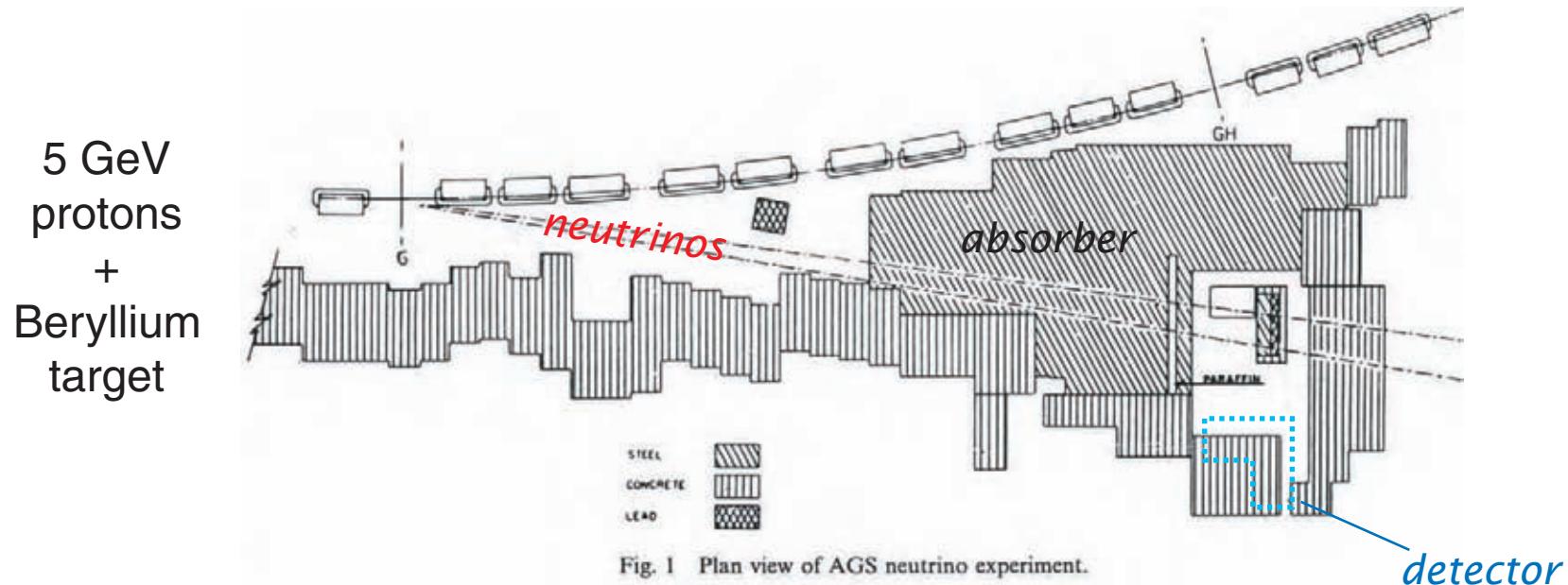
# First Detection of Neutrinos (Proposed)

*Reines & Cowen 1950*



# “Two Neutrino Experiment”

(mostly) muons detected in a beam of (mostly) muon neutrinos

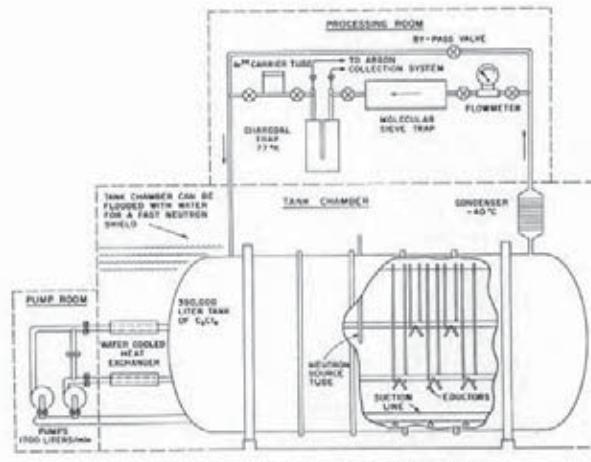


**beam:** *decay products of  $p$ ,  $K$   
(known to decay mostly to muons rather than electrons)*

**detected:** *34 muons ( $p > 300 \text{ MeV}/c$ )  
6 EM showers ( $n$ ,  $ne$ )*

Lederman, Schwartz, Steinberger  
1988 Nobel Prize in Physics

# Homestake Mine Solar Neutrino Experiment

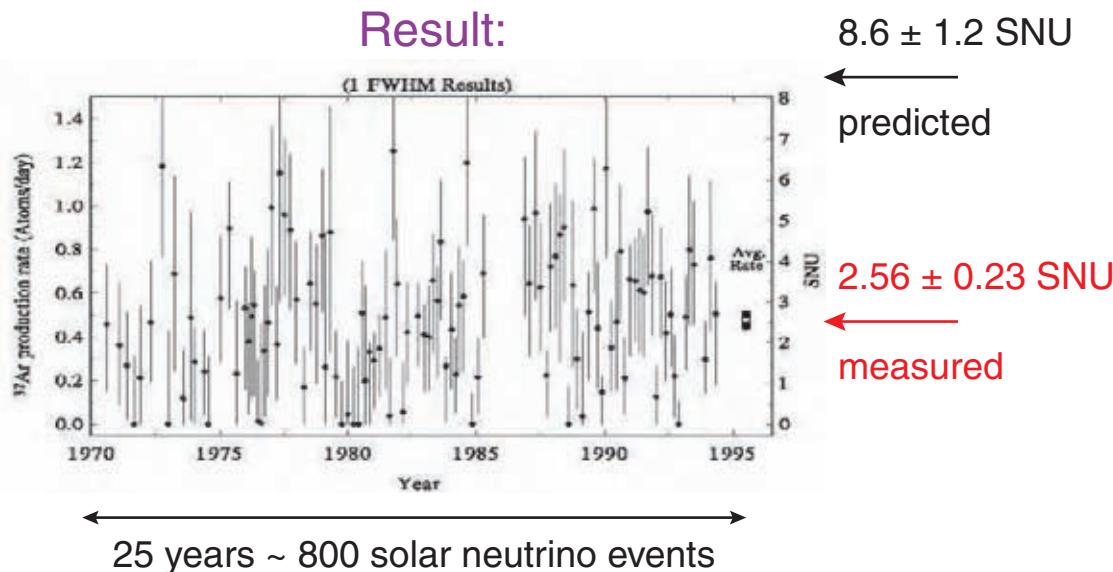


615 tons of  $\text{C}_2\text{Cl}_4$   
(dry cleaning fluid)

1500 meters depth

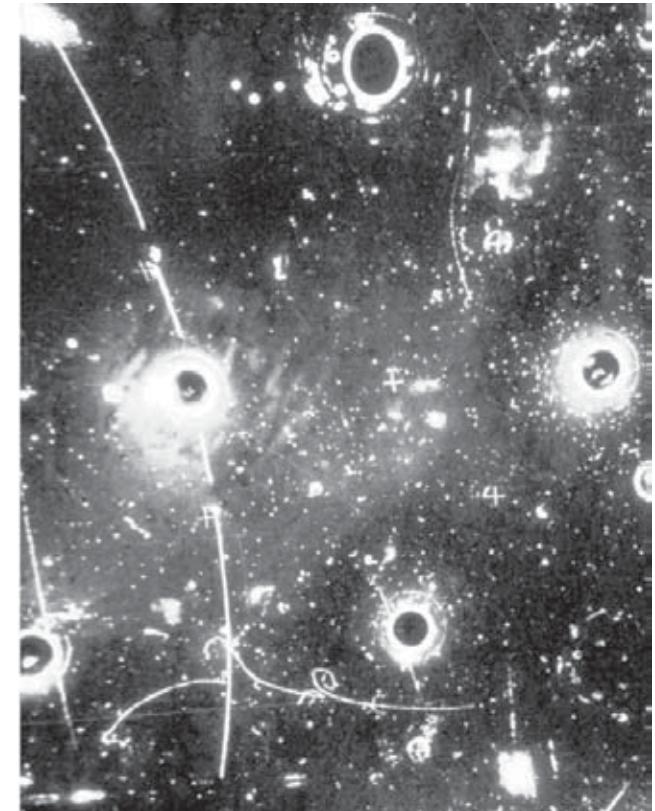
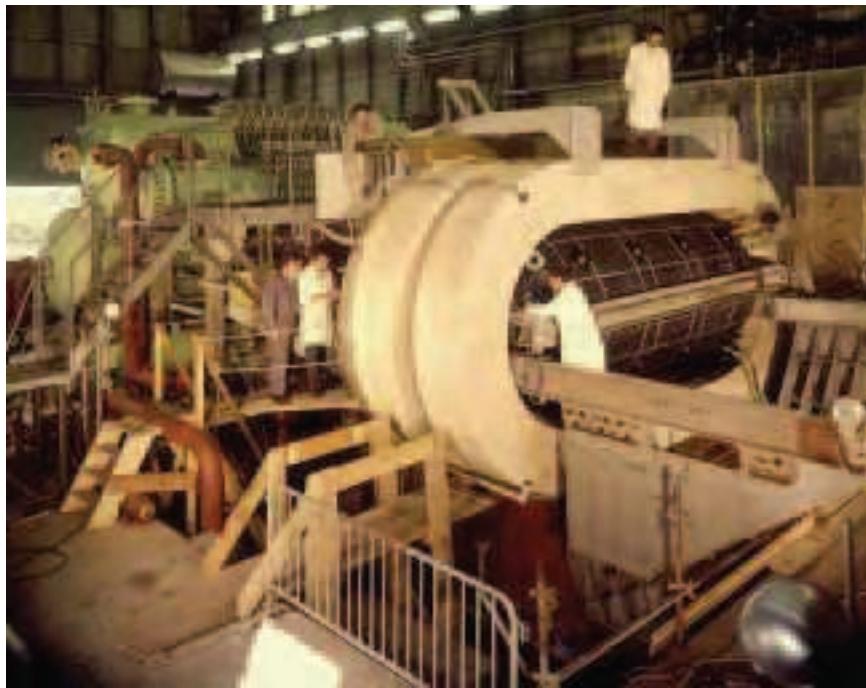
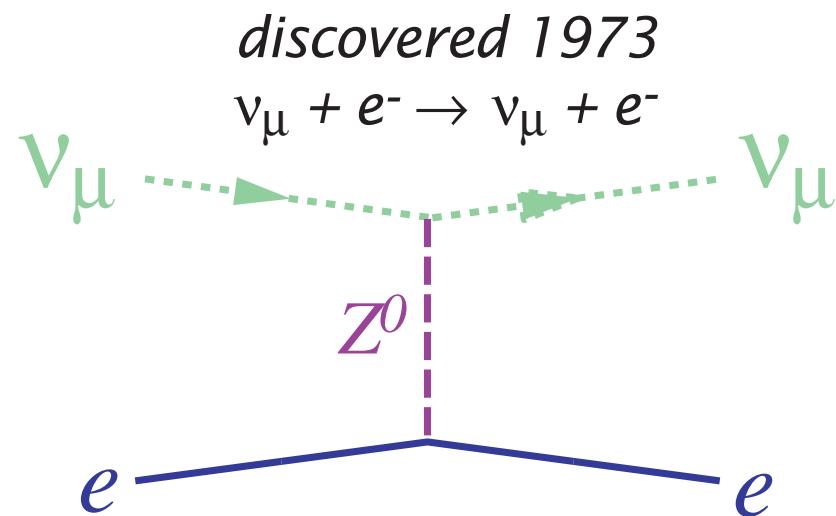
Individual Ar atoms  
extracted and counted  
by radioactive  
decay ( $\tau \sim 35$  days)

note:  
extraction rate  
less than  
1 atom per day!



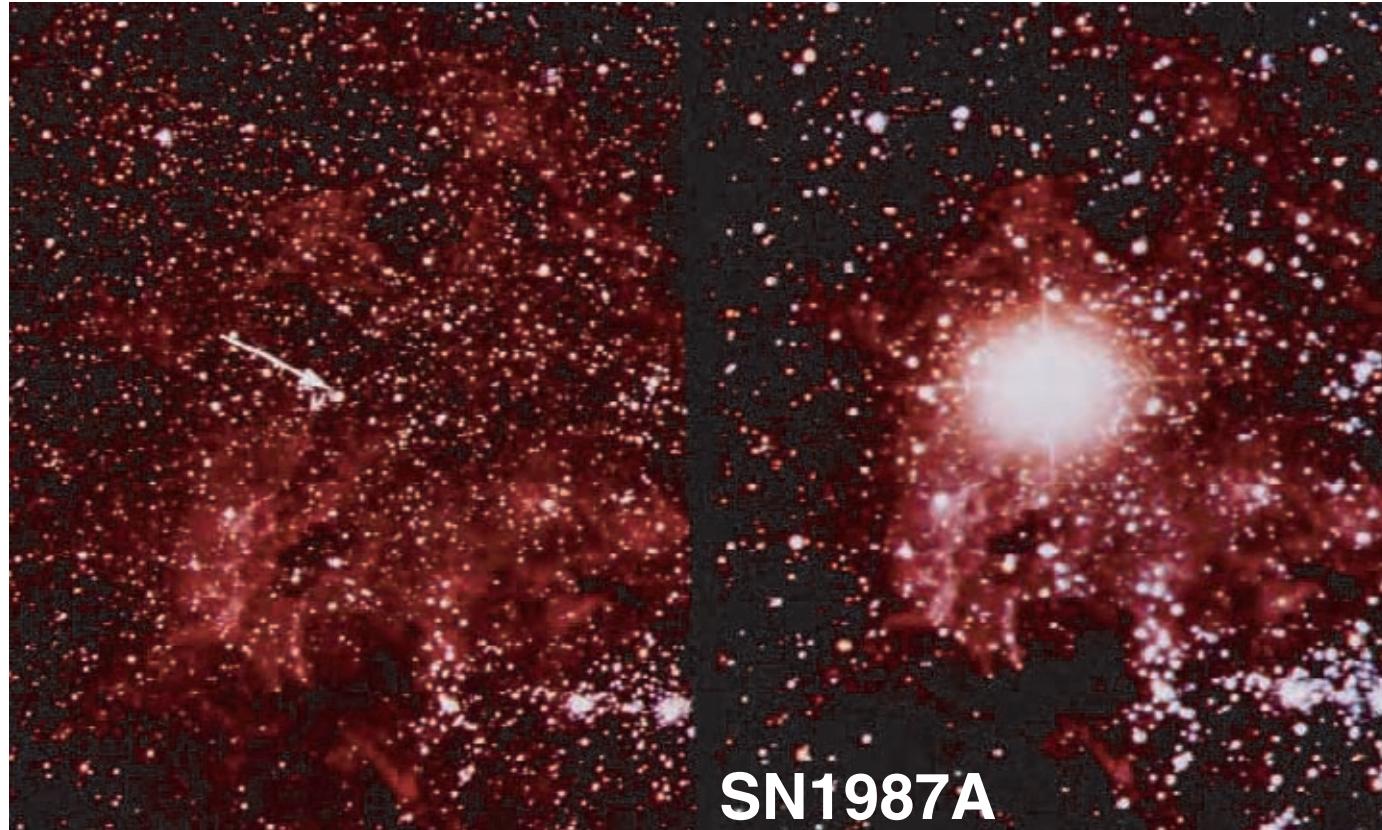
Ray Davis Jr.  
2002 Nobel Prize  
in Physics

# Neutral Currents and Neutrinos

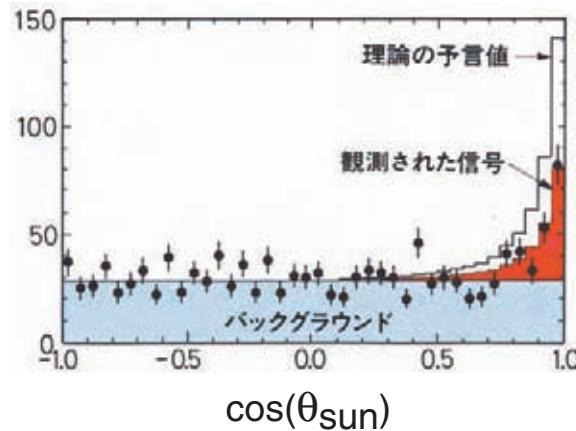




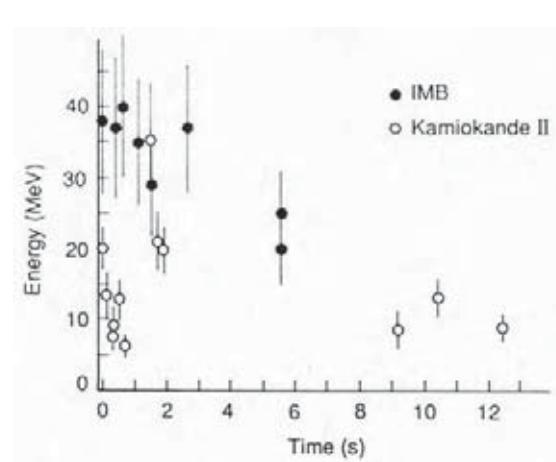
# Neutrino Astronomy



Kamiokande Solar Neutrino Result

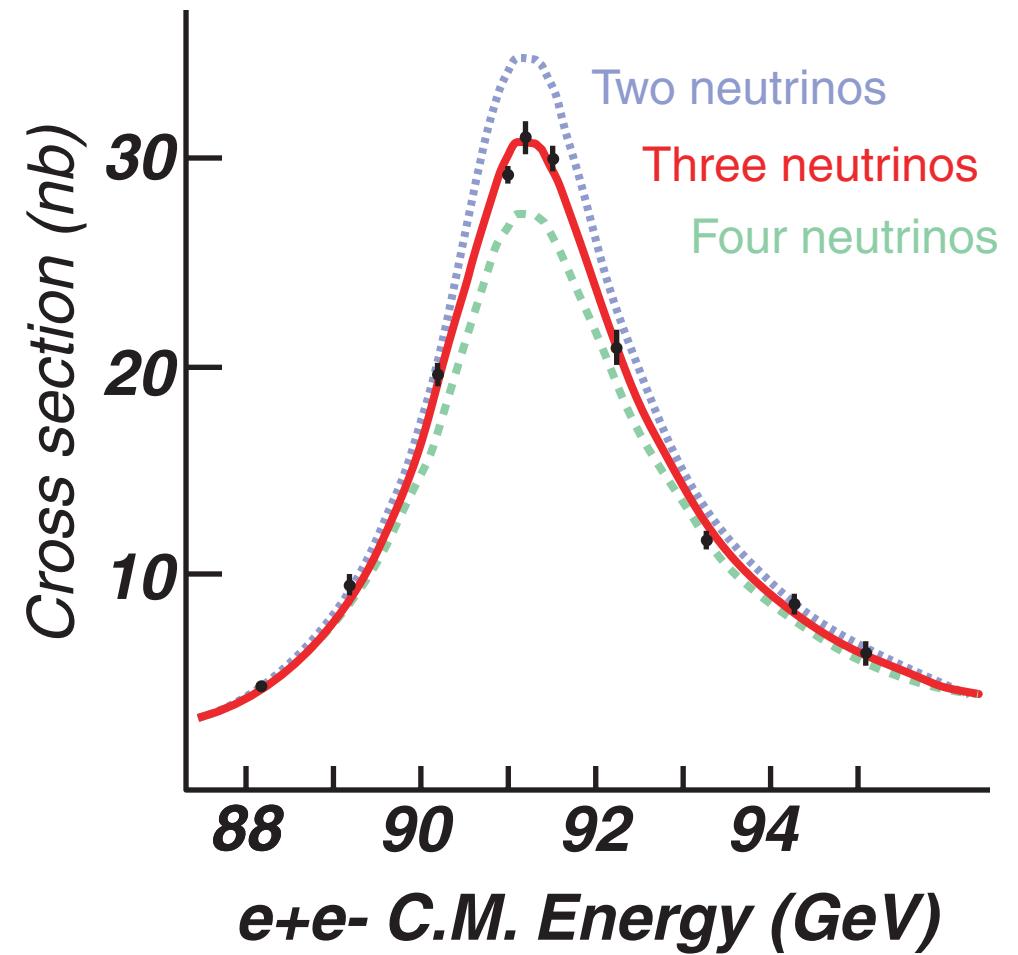
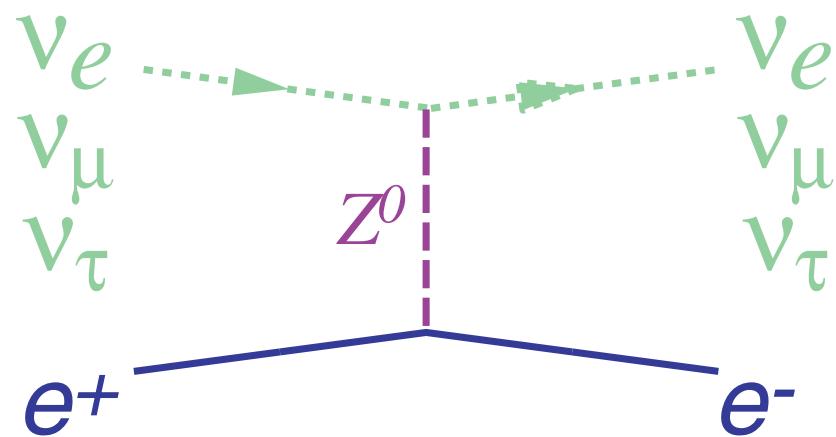


Result:  
 $46\% \pm 15\%$   
of predicted flux



Masatoshi  
Koshiba  
2002 Nobel Prize  
in Physics

# Three Neutrinos



*results from LEP experiments  
at CERN (1990's)*

# Neutrino Oscillations

First proposed by Bruno Pontecorvo in 1957 in analogy to  $K^0-\bar{K}^0$  mixing.

Recently the question was discussed whether there exist other mixed neutral particles beside the  $K^0$  mesons, i.e. particles that differ from the corresponding antiparticles, with the transitions between particle and antiparticle states not being strictly forbidden. It was noted that neutrino might be such a mixed particle, and consequently there exists the possibility of real **neutrino-antineutrino** transitions in vacuum, provided that lepton (neutrino) charge is not conserved.

- before the two-neutrino experiment, later extended to  $\nu_e - \nu_\mu$
- a consequence of interference of the mass states of a propagating neutrino
- requires non-zero mass and finite mixing of neutrino flavors

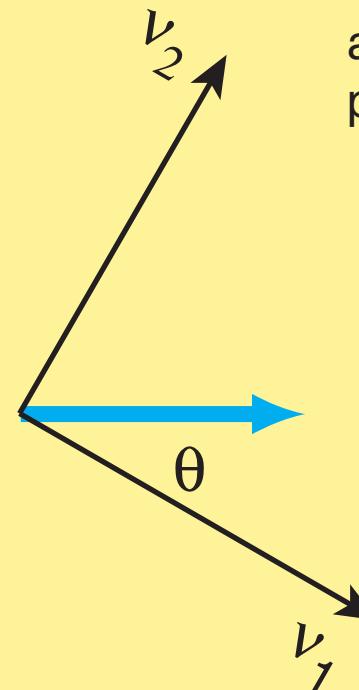
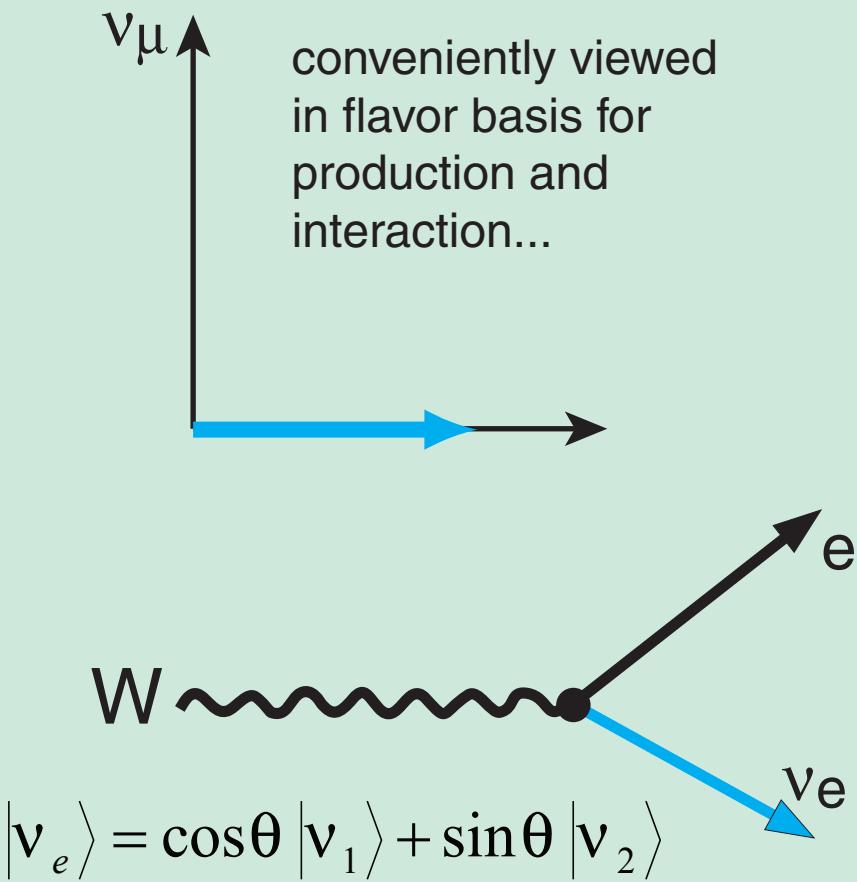
# Neutrino Mixing

Consider the neutrino as a two-state system (we will extend to 3-states shortly),

*flavor*  
 $\alpha = e, \mu, \tau$

$$\begin{pmatrix} v_e \\ v_\mu \end{pmatrix} = \begin{pmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{pmatrix} \begin{pmatrix} v_1 \\ v_2 \end{pmatrix}$$

*mass*  
 $i = 1, 2, 3$



and in mass basis for propagation and evolution.

*Schroedinger Equation:*

$$i \frac{\partial}{\partial t_1} |v_1\rangle = m_1 |v_1(t_1)\rangle$$

solved by:

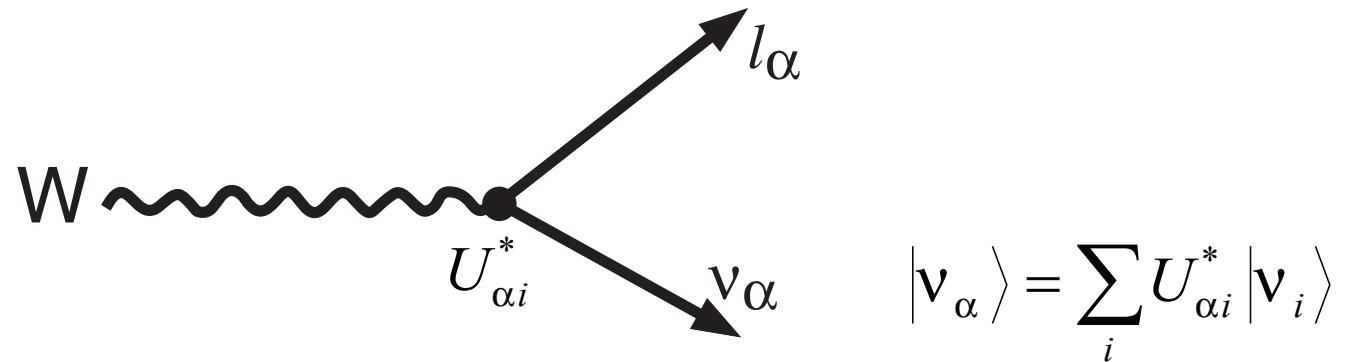
$$|v_1(t)\rangle = e^{-im_1 t} |v_1(0)\rangle$$

# Mixing with Three Flavors

$$\begin{pmatrix} \mathbf{v}_e \\ \mathbf{v}_\mu \\ \mathbf{v}_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{pmatrix} \begin{pmatrix} \mathbf{v}_1 \\ \mathbf{v}_2 \\ \mathbf{v}_3 \end{pmatrix}$$

three angles plus  
one complex phase

Pontecorvo-Maki-Nakagawa-Sakata Matrix (PMNS or MNS)



$$|\langle \mathbf{v}_\alpha | \mathbf{v}_i \rangle|^2 = |U_{\alpha i}|^2 \quad \text{flavor fraction of } \alpha \text{ in mass state } i$$

# Propagation in the Mass Basis

Amplitude for evolving for proper time  $\tau$ :

$$\langle \mathbf{v}_i(0) | \mathbf{v}_i(\tau_i) \rangle = e^{im_i\tau_i}$$

In laboratory frame variables, requiring Lorentz invariance, and  $v \sim c$ :



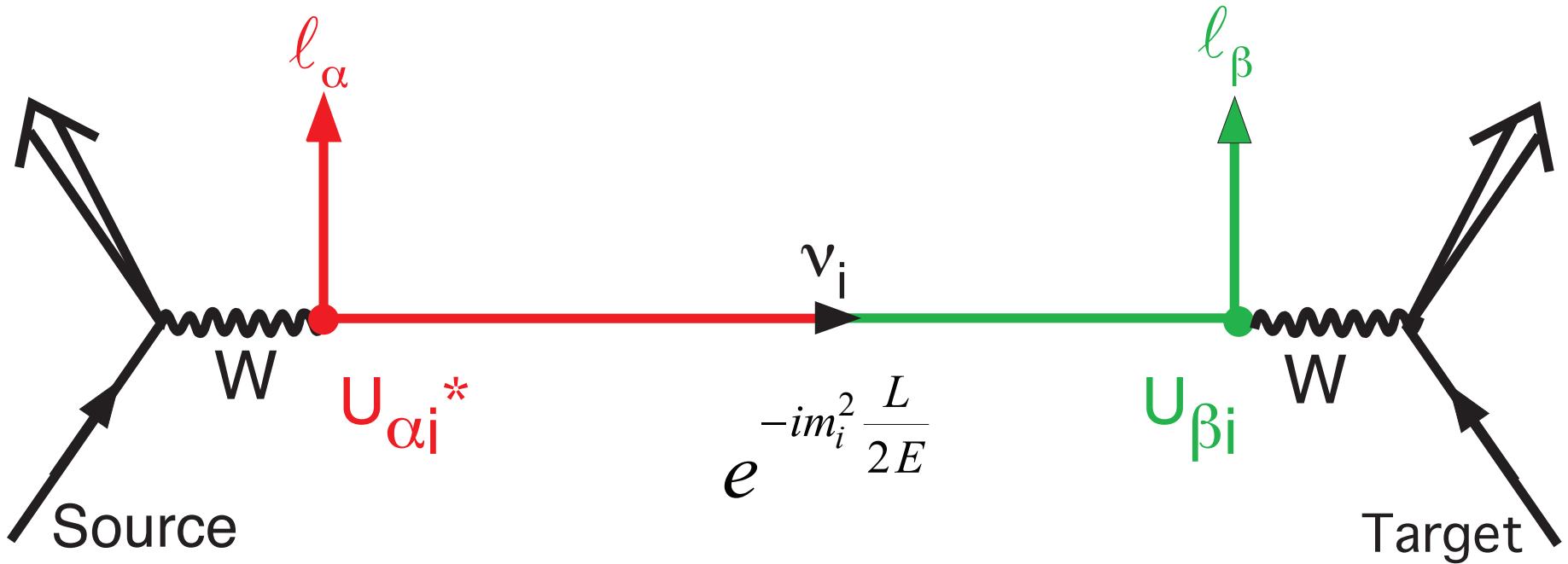
$$m_i\tau_i = E_i t - p_i L \quad p_i = \sqrt{E^2 - m_i^2} \approx E - \frac{m_i^2}{2E}$$

For components with common energy  $E$  that coherently interfere:

$$m_i\tau_i \approx E(t - L) + \frac{m_i^2}{2E} L$$

$$\langle \mathbf{v}_i(0) | \mathbf{v}_i(\tau_i) \rangle = e^{-im_i^2 \frac{L}{2E}} \quad \dots \text{ignoring common phase } E(t-L)$$

# Putting it all together...



$$P(\nu_\alpha \rightarrow \nu_\beta) = \delta_{\alpha\beta} - 4 \sum_{i>j} \text{Re}[U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*] \sin^2 \left( \Delta m_{ij}^2 \frac{L}{4E} \right)$$

- sign for antineutrinos

$$\pm 2 \sum_{i>j} \text{Im}[U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*] \sin \left( \Delta m_{ij}^2 \frac{L}{4E} \right)$$

$$\Delta m_{ij}^2 \equiv m_i^2 - m_j^2$$

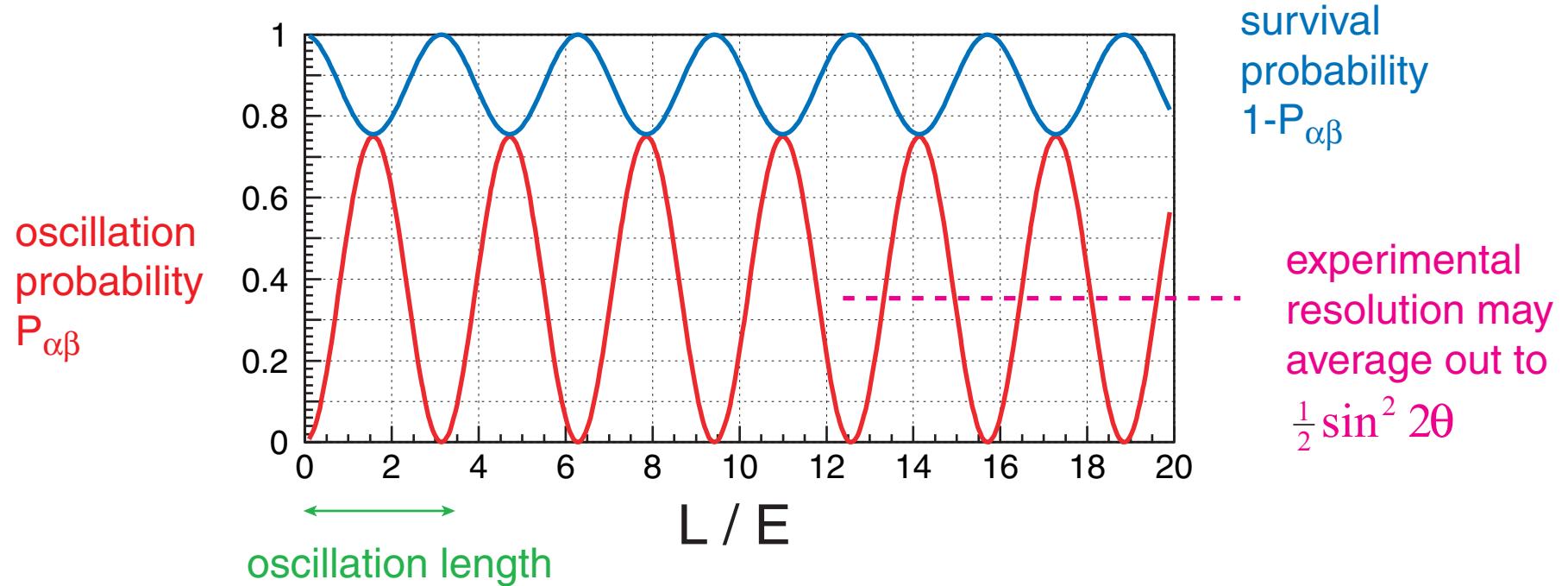
$$\Delta m_{ij}^2 \frac{L}{4E} = 1.27 \Delta m_{ij}^2 (\text{eV}^2) \frac{L(\text{km})}{E(\text{GeV})}$$

with  $\hbar, c \neq 1$

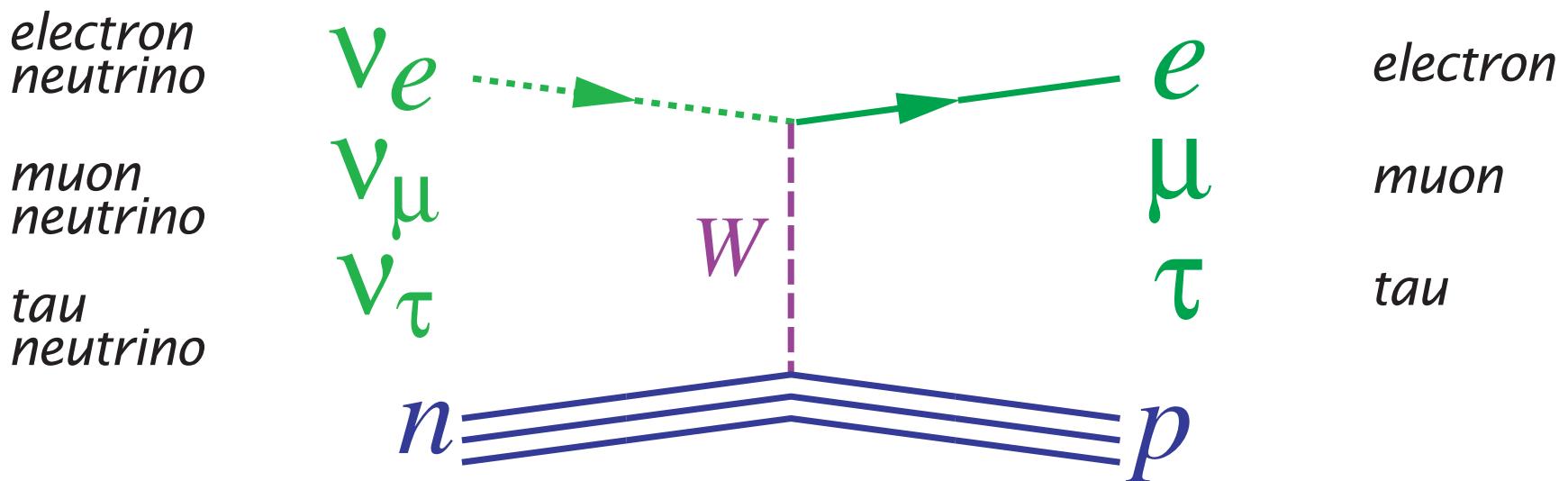
# Back to Two Neutrinos

- often the case: one of the oscillatory terms remains zero under the experimental conditions (i.e.  $L$  too short,  $E$  too large etc.)

$$P(\nu_\alpha \rightarrow \nu_\beta) = \sin^2 2\theta \sin^2 \left( 1.27 \Delta m_{ij}^2 \frac{L}{E} \right)$$



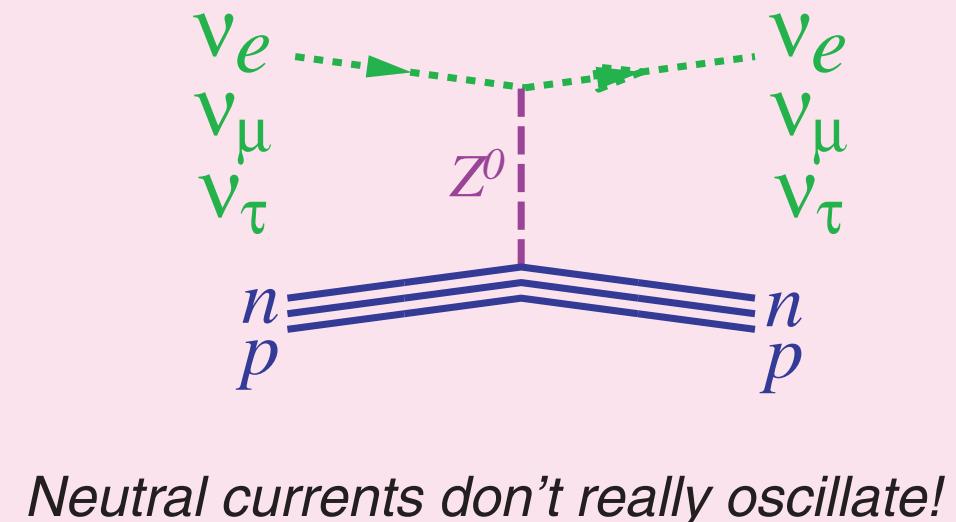
# Appearance and Disappearance



## Reaction Threshold

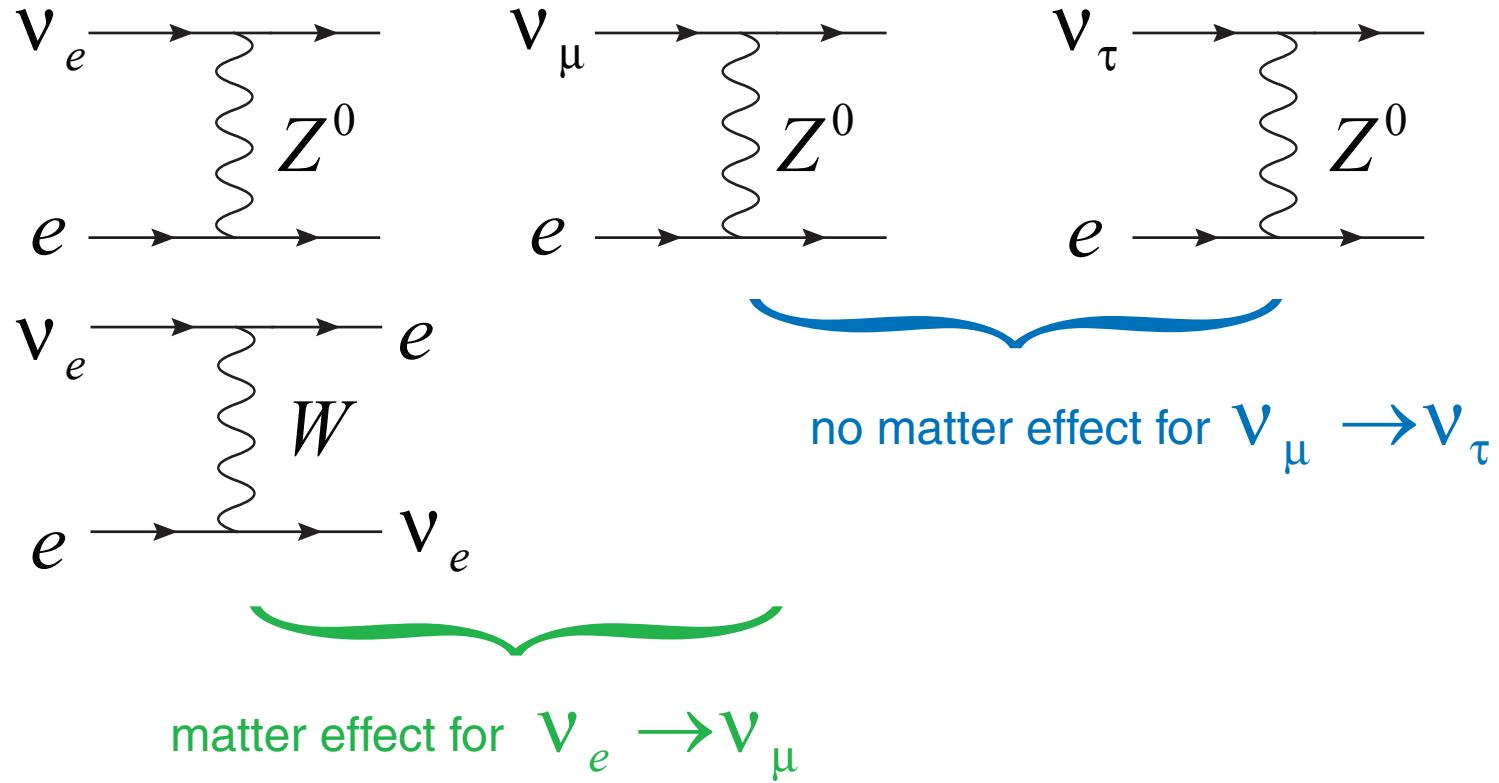
$e$	$E_V > 1.5 \text{ MeV}$
$\mu$	$E_V > 110 \text{ MeV}$
$\tau$	$E_V > 3500 \text{ MeV}$

often, an experiment produces the beam neutrino below the threshold of for the production of a new flavor lepton



# Matter Effects

due to coherent forward scattering



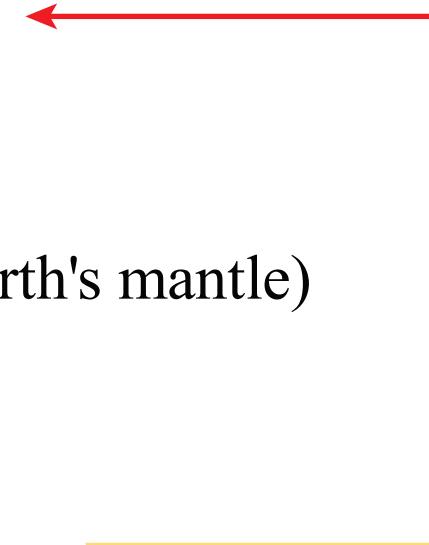
extra interaction potential  $V = \sqrt{2}G_F N_e$   
(- sign for anti- $\nu_e$ )

if  $m_2^2 - m_1^2 < 0$  then  $V$  also changes sign

# Matter Effects (continued)

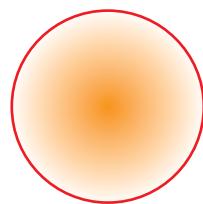
$$\Delta m_M^2 = \Delta m^2 \sqrt{\sin^2 2\theta + (\cos 2\theta - x)^2}$$

$$\sin^2 2\theta_M = \frac{\sin^2 2\theta}{\sin^2 2\theta + (\cos 2\theta - x)^2}$$



$$x = \frac{V/2}{\Delta m^2 / 4E} = \frac{2\sqrt{2}G_F N_e E}{\Delta m^2} \sim \frac{E}{12 GeV} \text{ (in earth's mantle)}$$

Mikheyev-Smirnov-Wolfenstein (MSW effect)



neutrinos produced in Sun's center would encounter critical density at some point on the way out regardless of how small the mixing angle

*if  $\sin^2 2\theta$  is small it can become large in matter under the right energy and density conditions*

# Neutrino Oscillation Experiments

## *solar neutrinos*



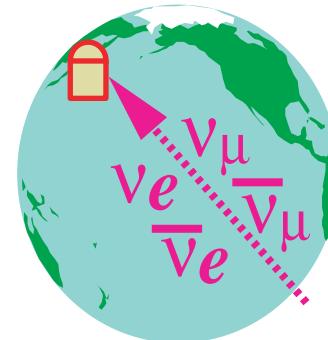
$$L = 10^{11} \text{ m}$$

$$E = 0.1 \text{ to } 15 \text{ MeV}$$

$$\Delta m^2 \sim 10^{-10} \text{ to } 10^{-12} \text{ eV}^2 \text{ (vacuum)}$$

$$\Delta m^2 \sim 10^{-4} \text{ to } 10^{-10} \text{ eV}^2 \text{ (matter effects)}$$

## *atmospheric neutrinos*

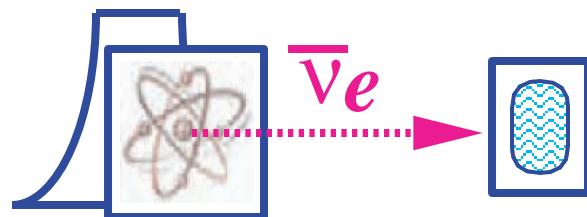


$$L = 10 \text{ to } 10000 \text{ km}$$

$$E = 0.1 \text{ to } 10 \text{ GeV}$$

$$\Delta m^2 \sim 10^{-1} \text{ to } 10^{-5} \text{ eV}^2$$

## *reactor neutrinos*

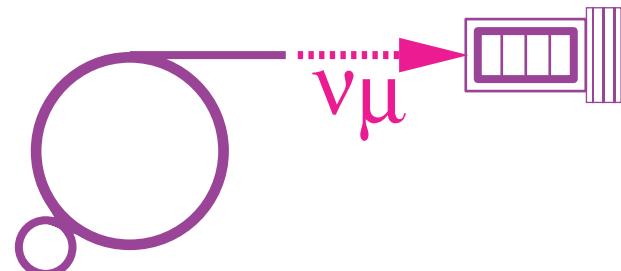


$$L = 100 \text{ to } 10000 \text{ m}$$

$$E = 3 \text{ MeV}$$

$$\Delta m^2 \sim 10^{-2} \text{ to } 10^{-5} \text{ eV}^2$$

## *accelerator neutrinos*

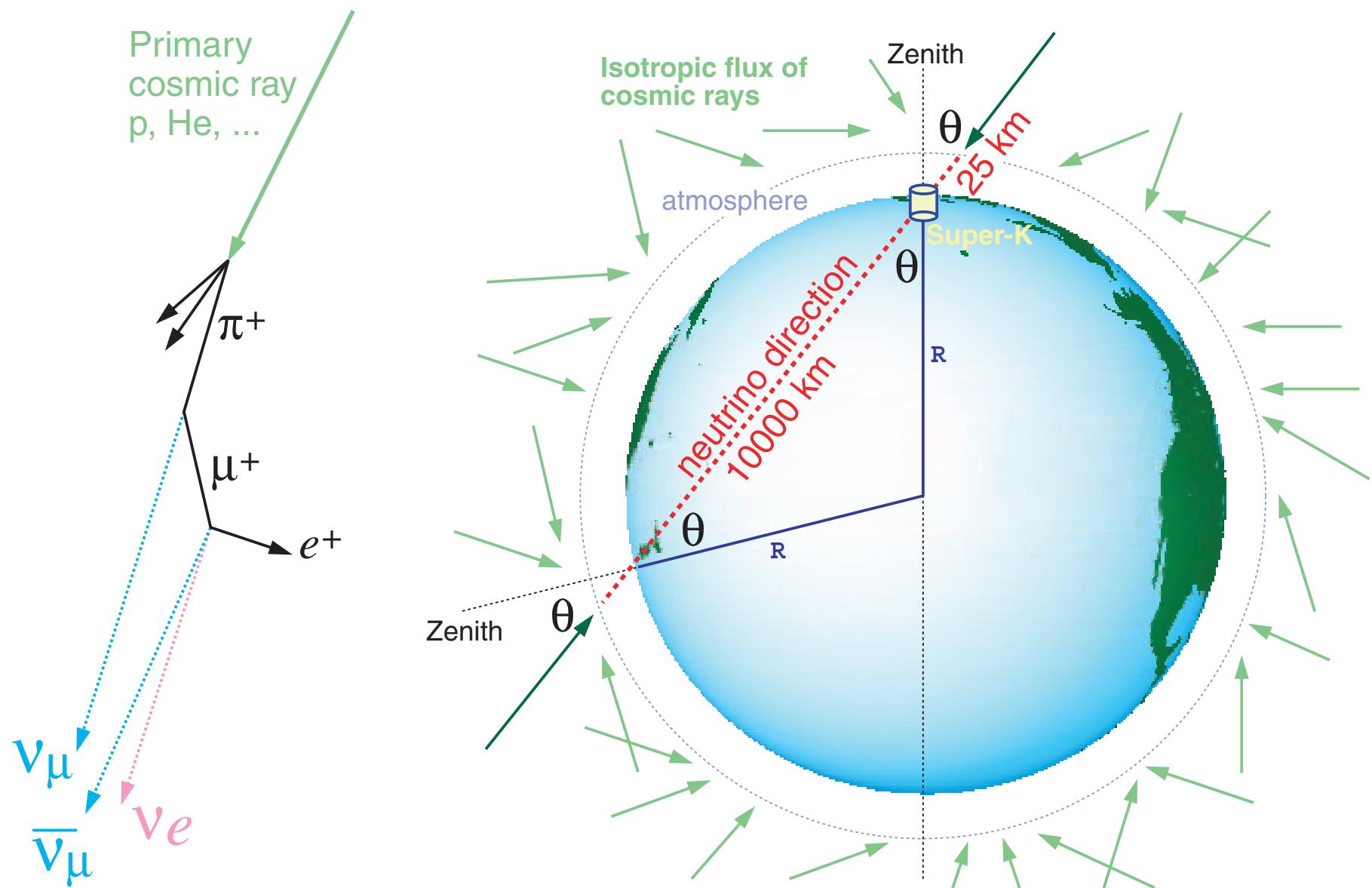


$$L = 0.1 \text{ to } 1000 \text{ km}$$

$$E = 1-10 \text{ GeV}$$

$$\Delta m^2 \sim 10^0 \text{ to } 10^{-4} \text{ eV}^2$$

# Atmospheric Neutrinos



**Ratio of  $\nu_\mu/\nu_e \sim 2$**   
(for  $E_\nu < \text{few GeV}$ )

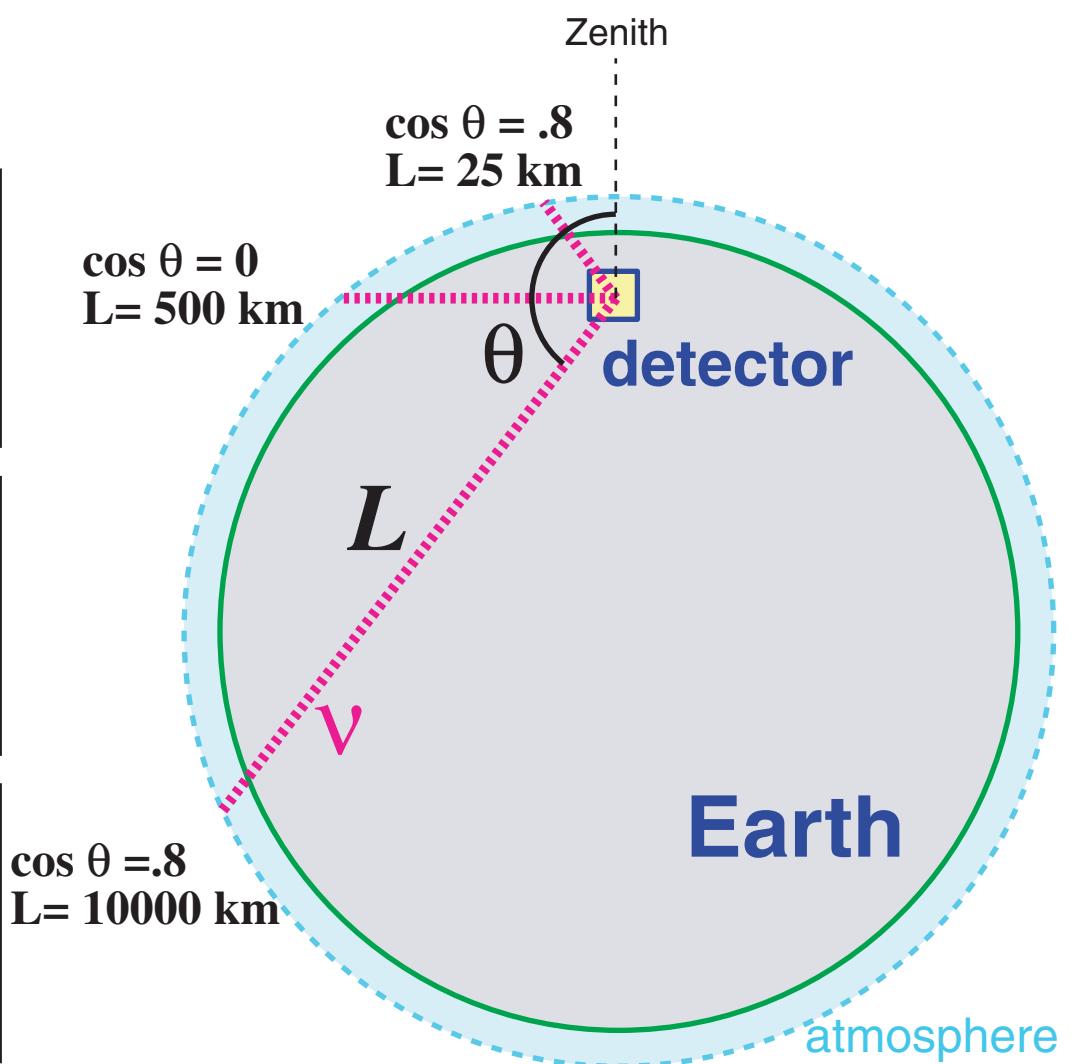
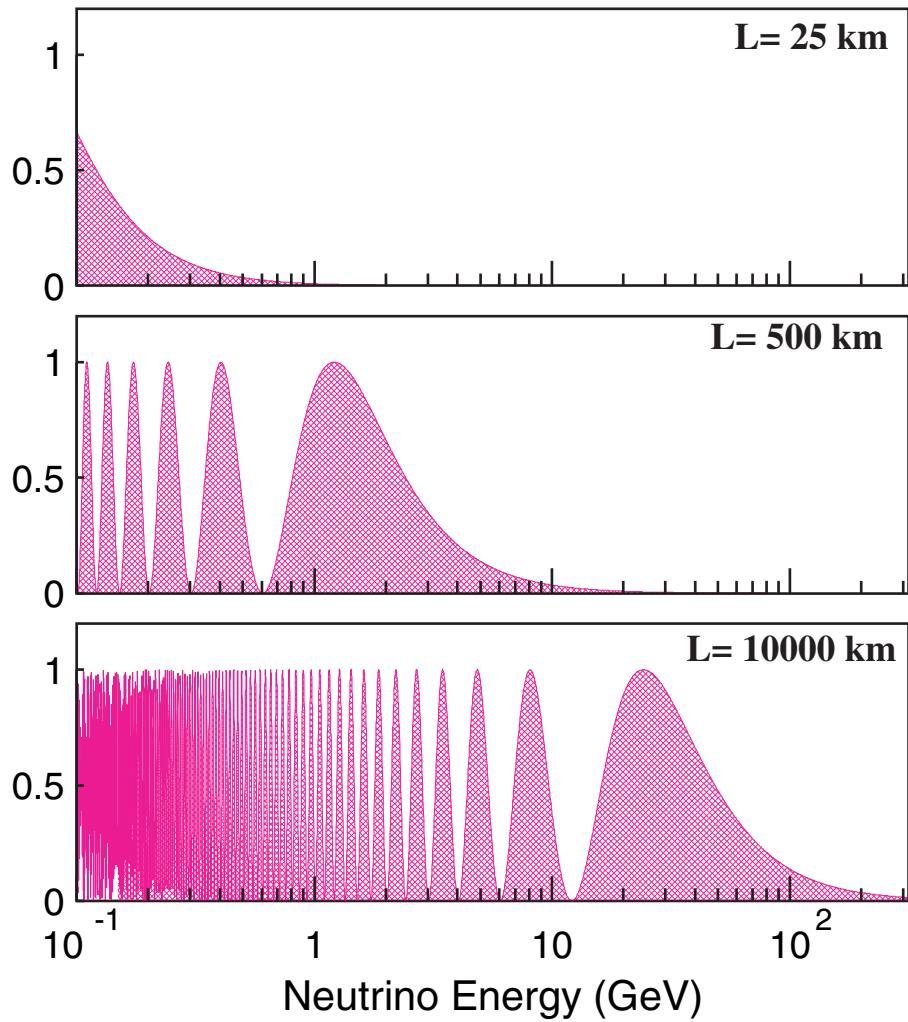
**Up/Down Symmetric Flux**  
(for  $E_\nu > \text{few GeV}$ )

# Atmospheric Neutrino Oscillation

$$P_{\nu\nu'} = \sin^2 2\theta \sin^2 \frac{1.27 \Delta m^2 L}{E}$$

$$\sin 2\theta = 1$$

$$m^2 = .003 \text{ eV}$$



# Super-Kamiokande Experiment

## Inner detector

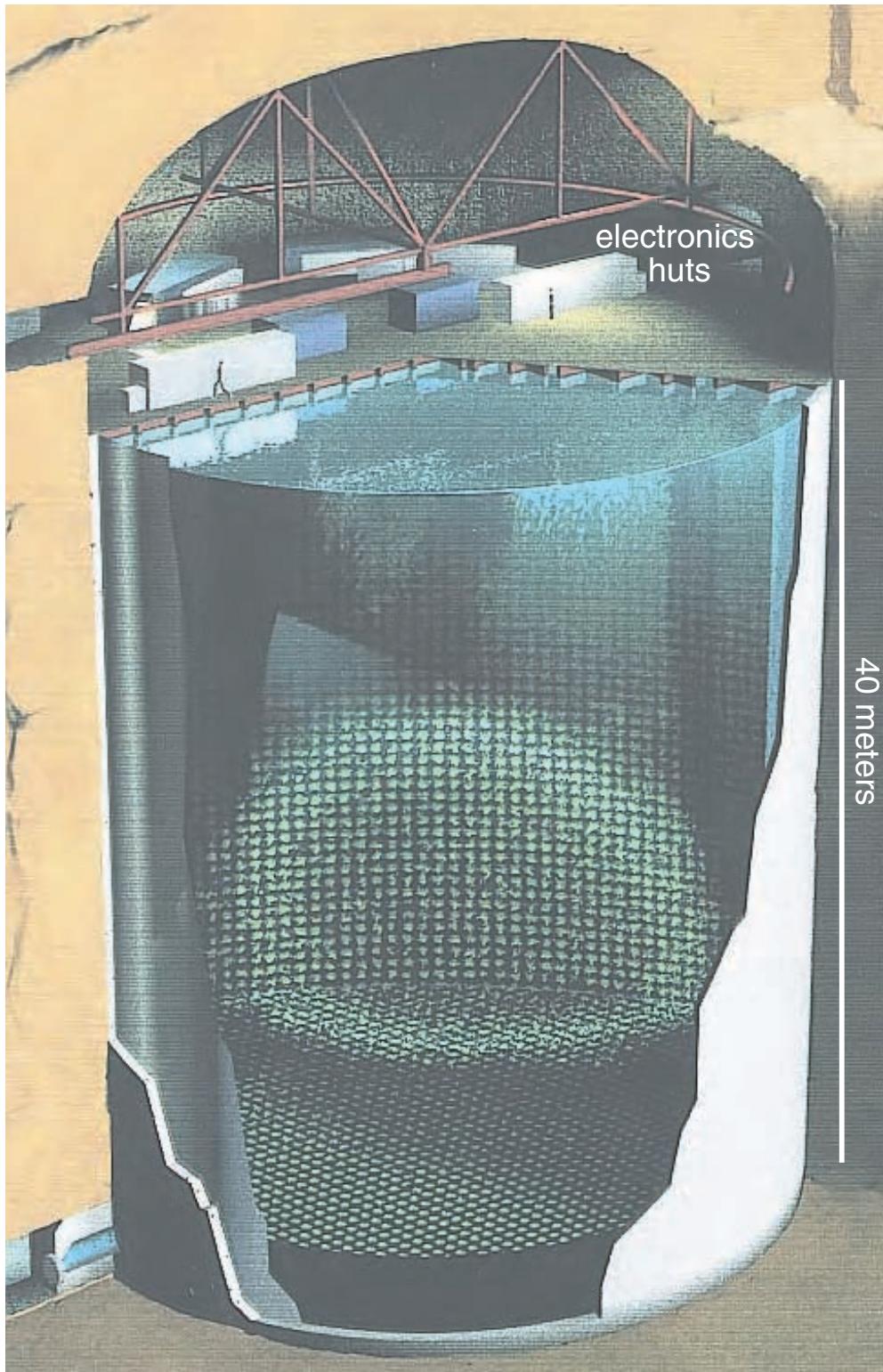
**22.5 kton fiducial mass**  
**11134 50cm photomultiplier tubes**  
**40% photocathode coverage**  
**~2 ns PMT timing resolution**  
**~85 m water attenuation length**

## Outer detector

**optically isolated veto and shield**  
**1800 20cm pmts recovered from IMB**

## Location

**Kamioka zinc mine, Japan**  
**1 km under mountain (2700 m.w.e.)**



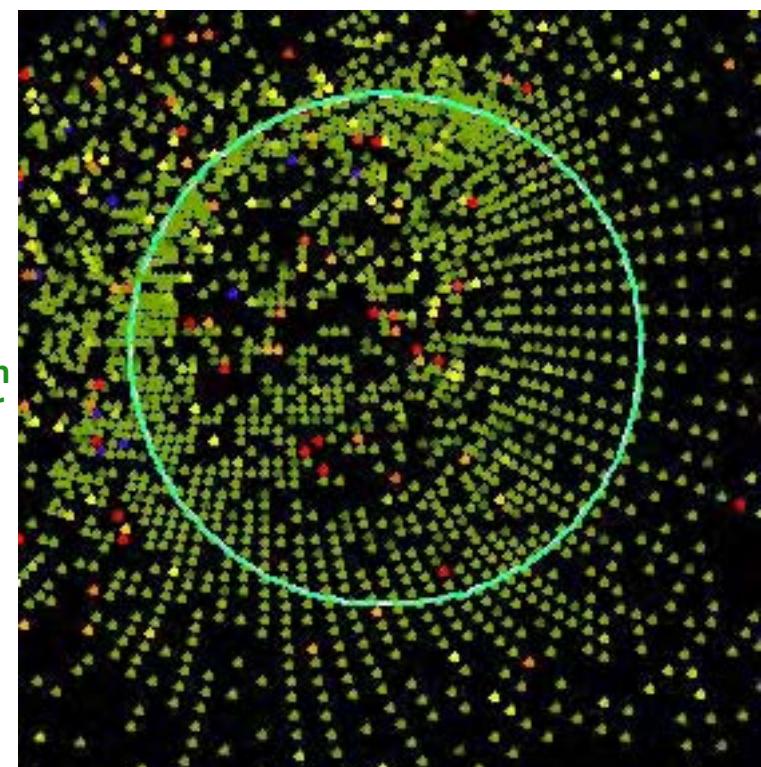
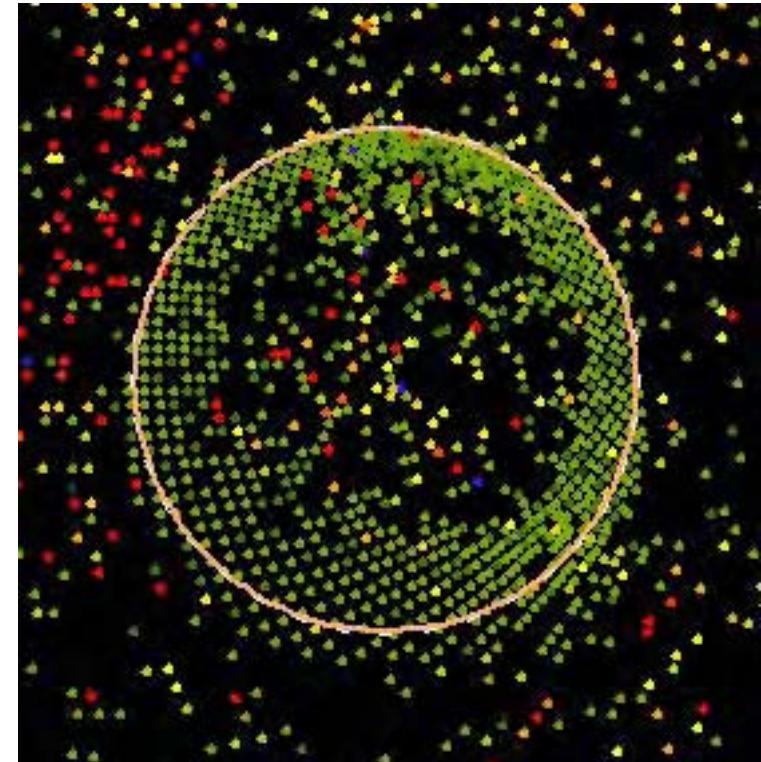
# How to distinguish muon neutrinos from electron neutrinos

MUON  
NEUTRINO

muon

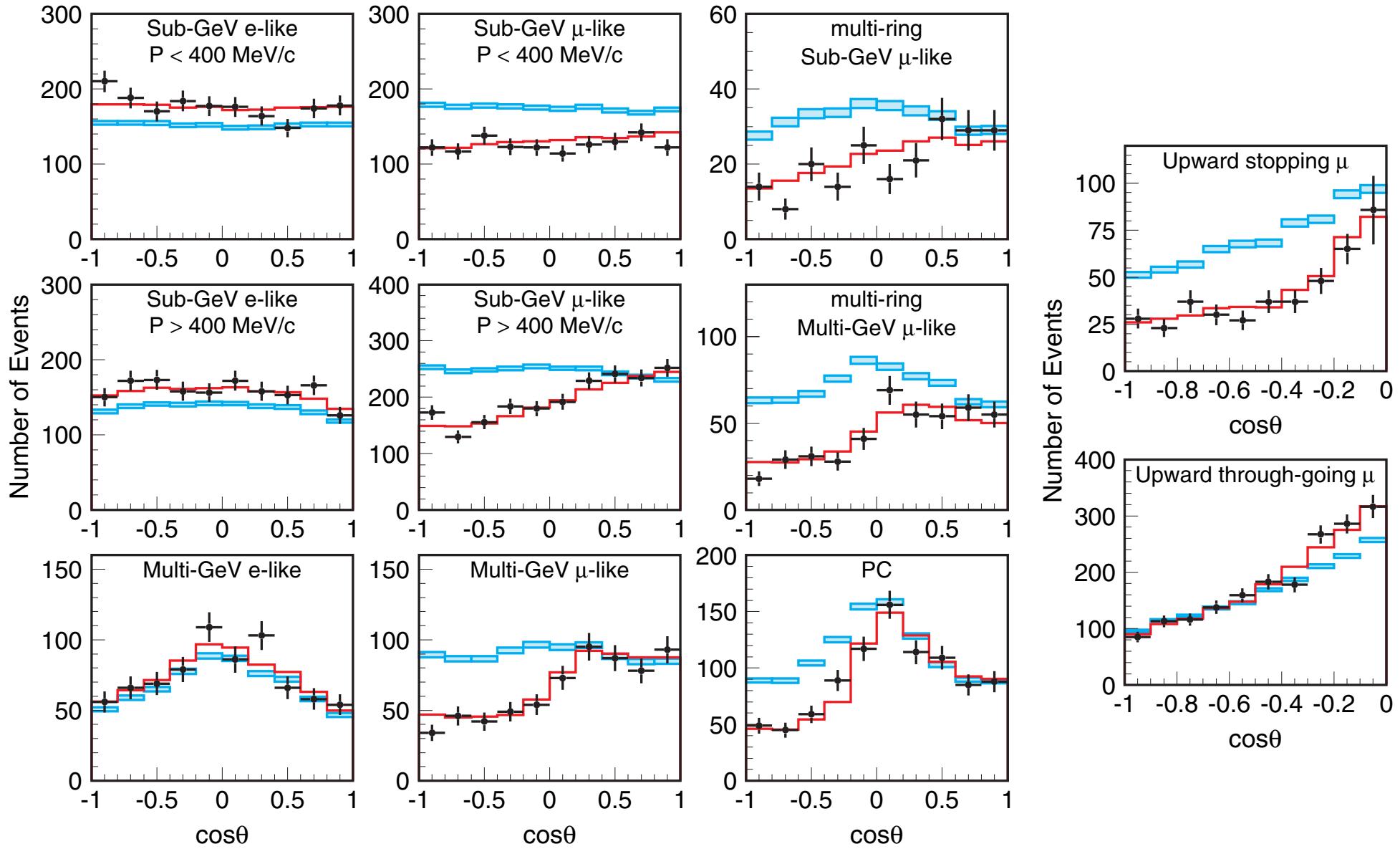
ELECTRON  
NEUTRINO

electron  
shower

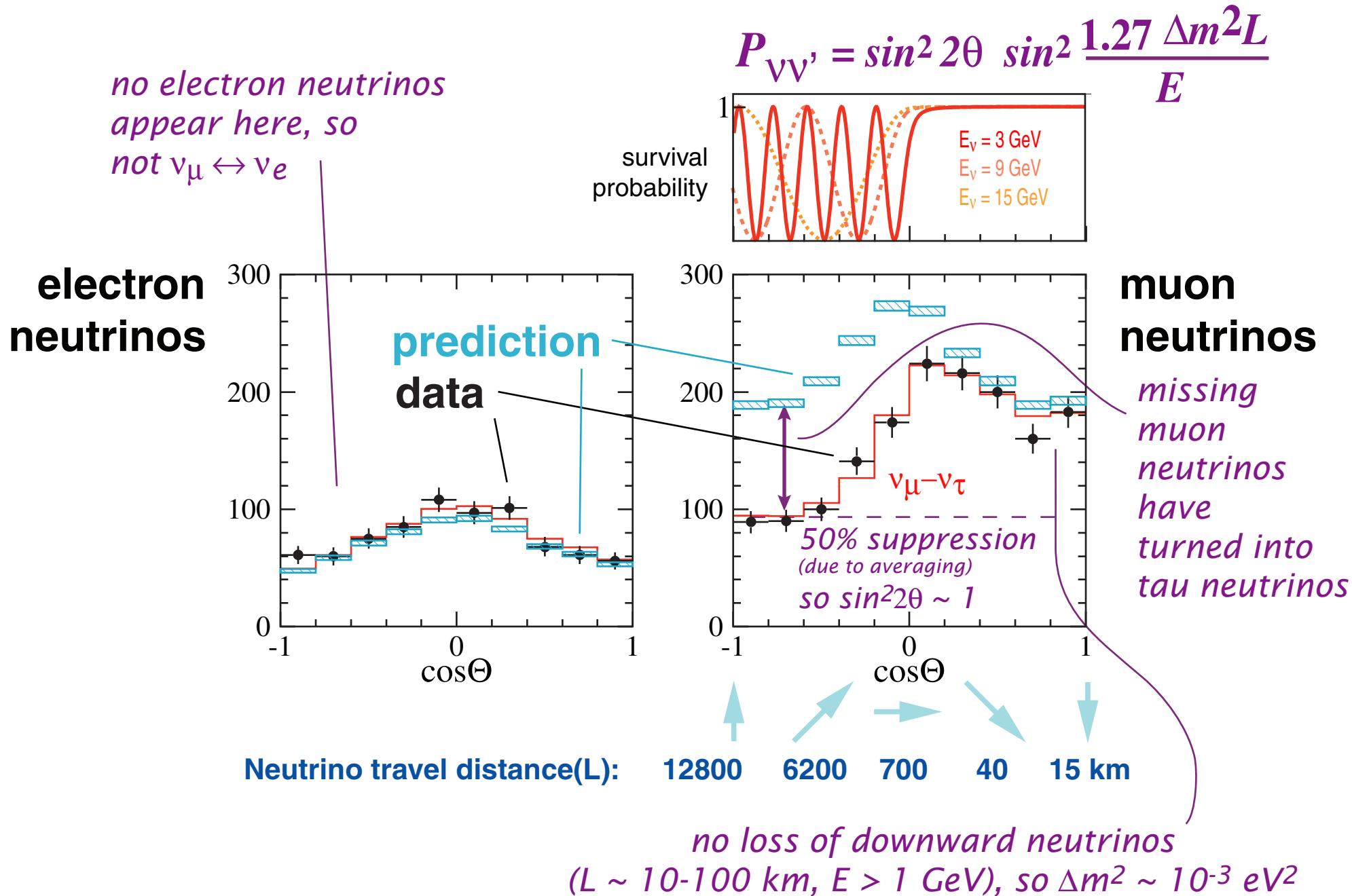


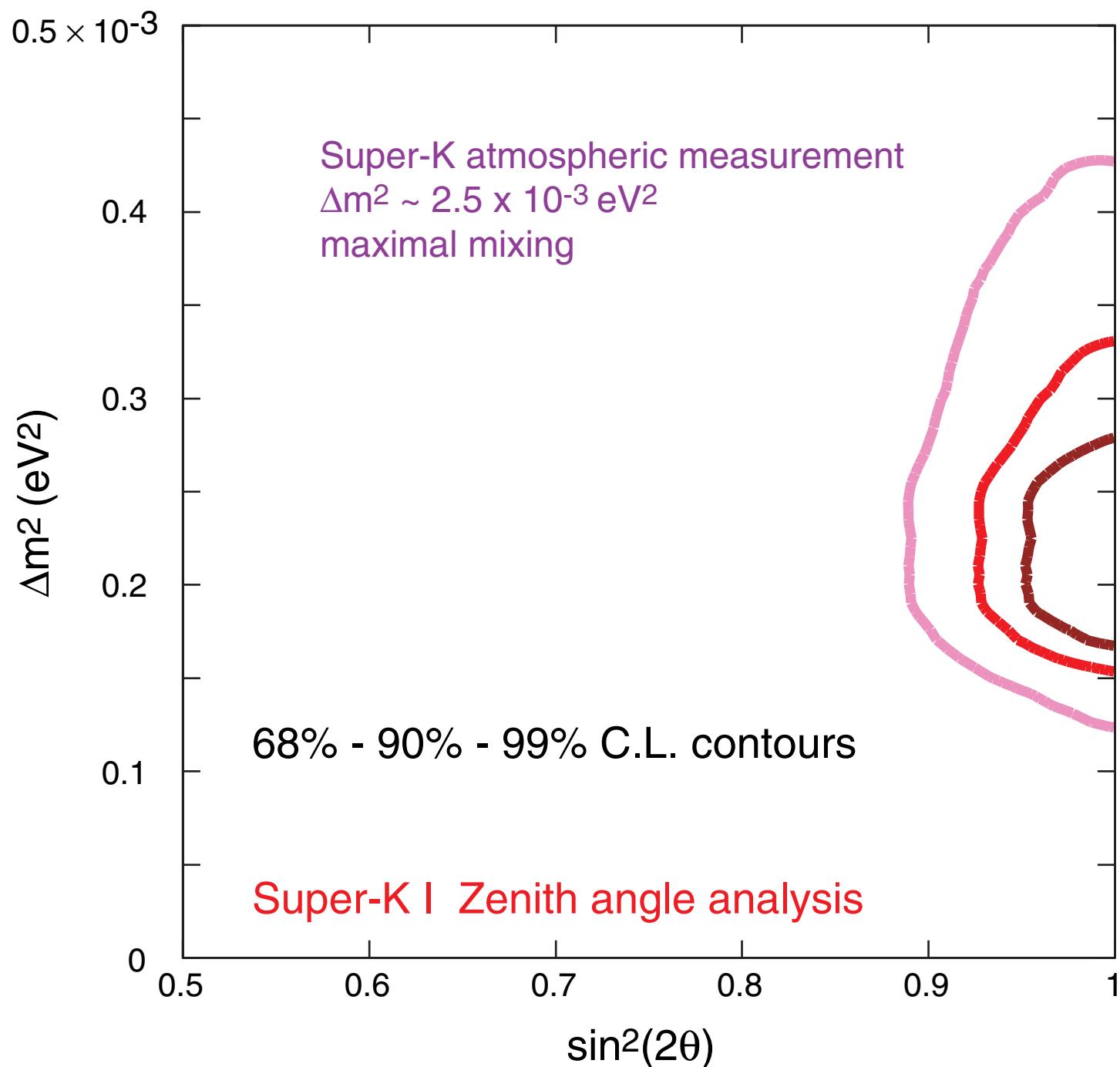
# Super-K Atmospheric Neutrino Data

## Zenith Angle Distributions



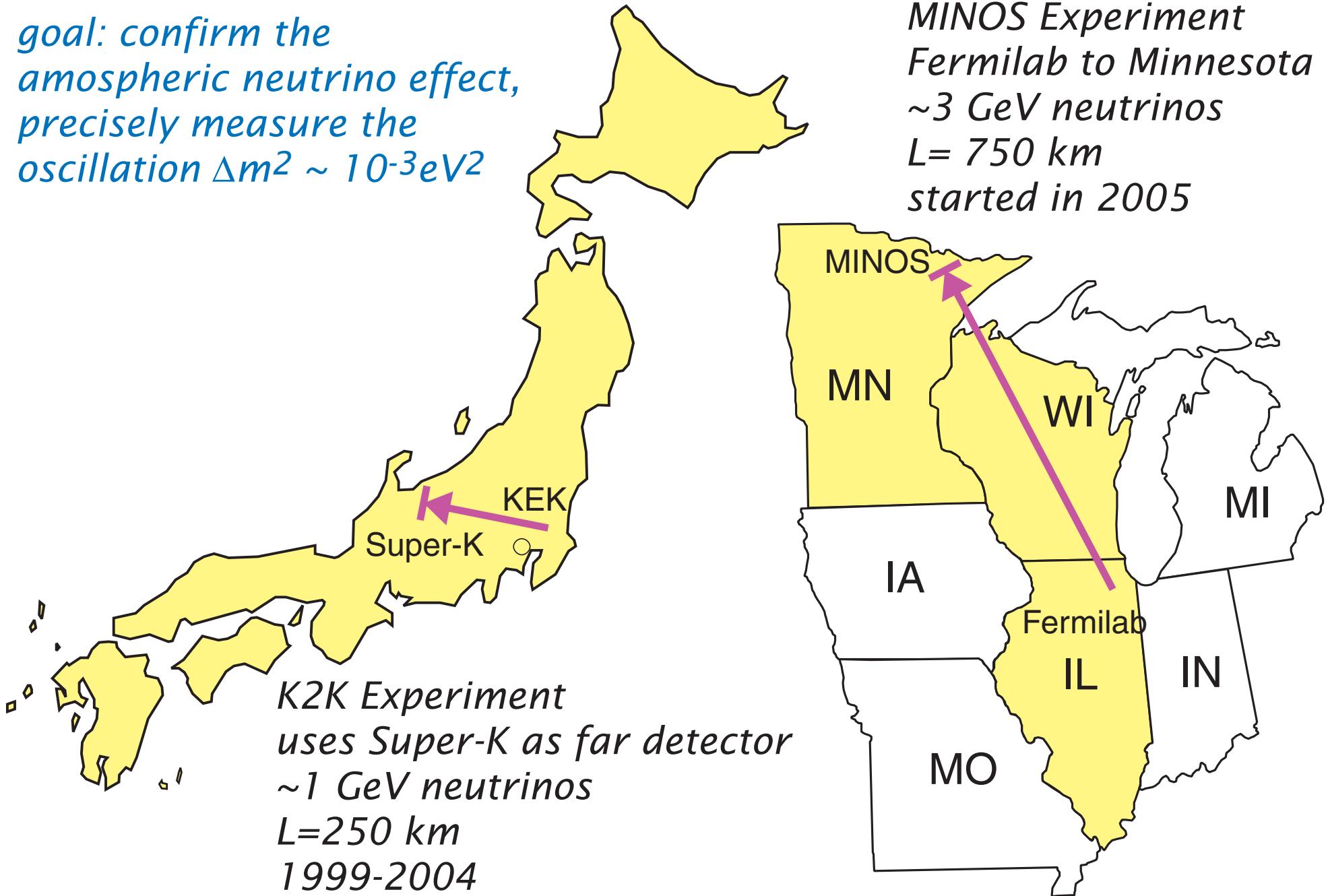
# How is this Neutrino Oscillation?

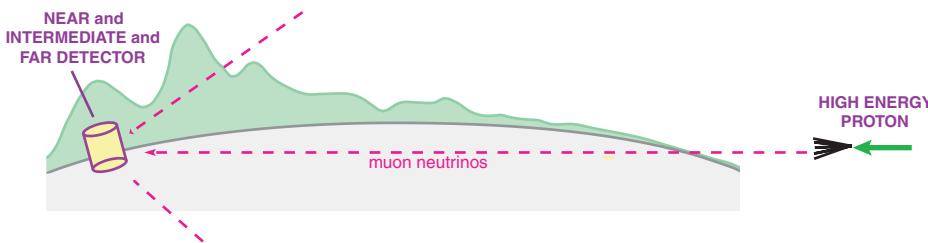




# Long Baseline Neutrino Oscillation Experiments

*goal: confirm the atmospheric neutrino effect, precisely measure the oscillation  $\Delta m^2 \sim 10^{-3} \text{eV}^2$*





## Atmospheric Neutrinos

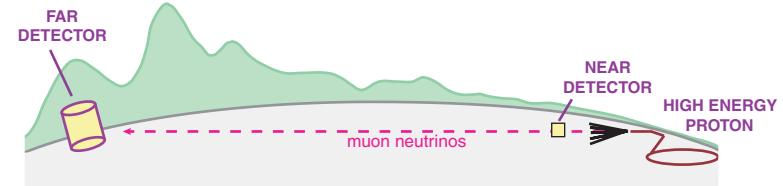
mixed beam of  $\nu_\mu \bar{\nu}_\mu \nu_e \bar{\nu}_e$

wide energy band 200 MeV - 1 TeV

continuous flux - free

multiple baselines 10 km - 13000 km

neutrino direction unknown



## Long Baseline Neutrinos

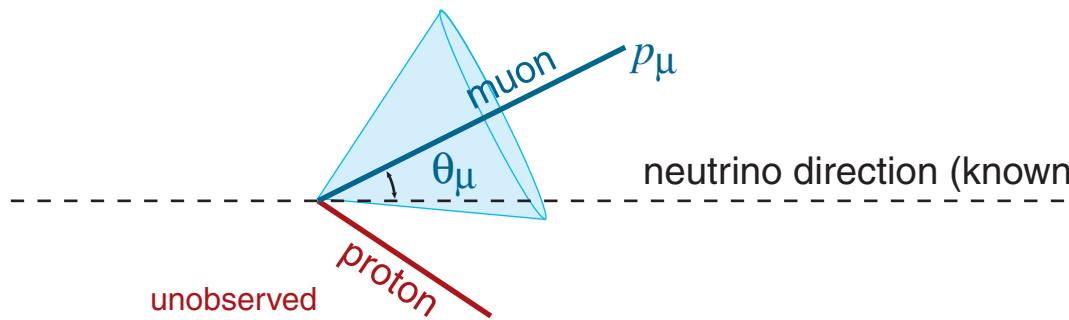
nearly pure beam of  $\nu_\mu$

narrow energy band, adjustable

pulsed flux - expensive

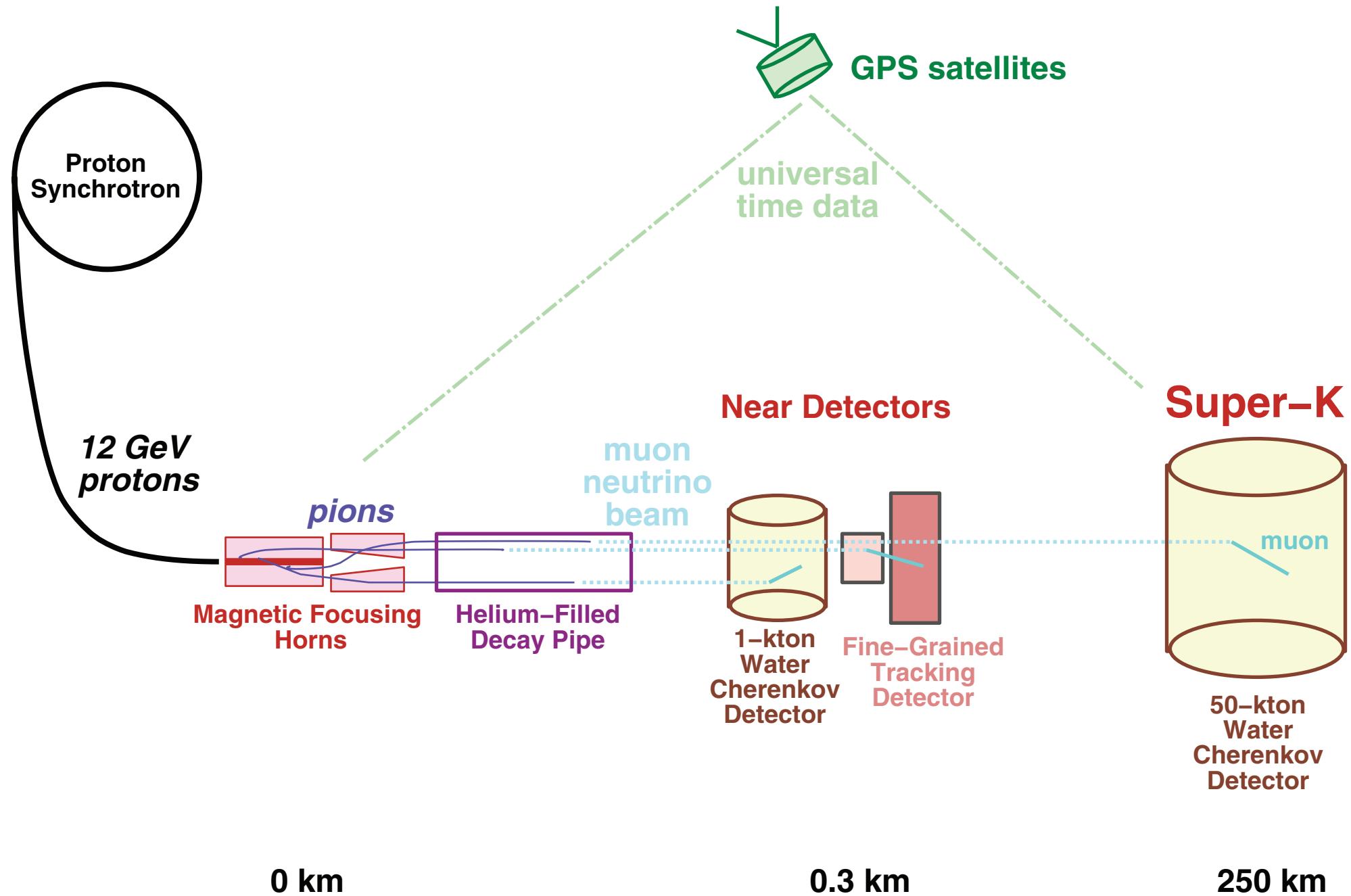
fixed baseline 250 / 750 km so far

neutrino direction known

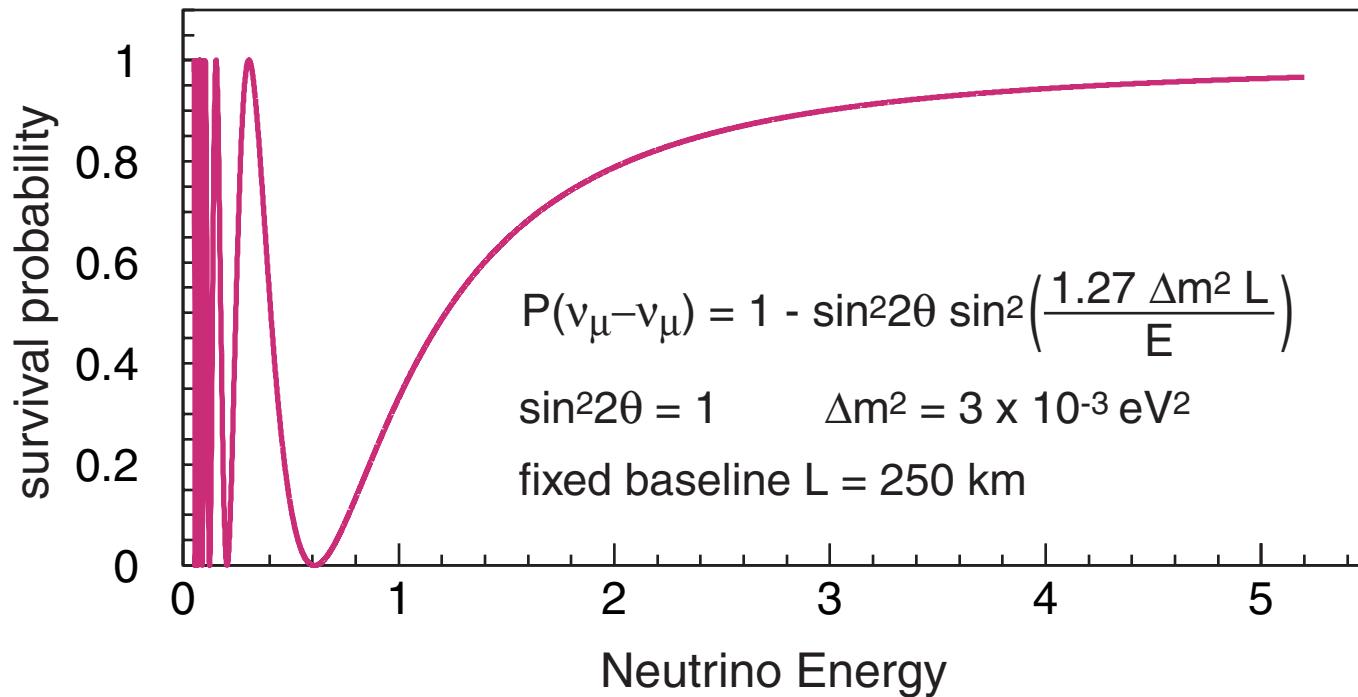


$$E_{\nu} = \frac{M_n E_\mu - m_\mu^2/2}{M_n - E_\mu + p_\mu \cos \theta_\mu}$$

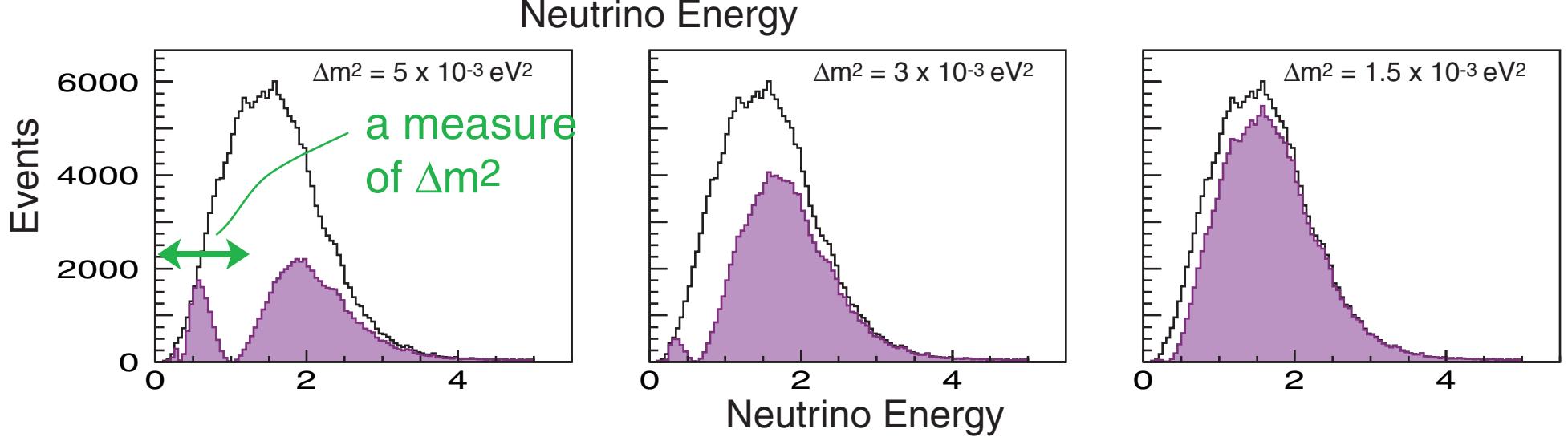
useful for quasi-elastic events (prevalent at low energies ~1 GeV)



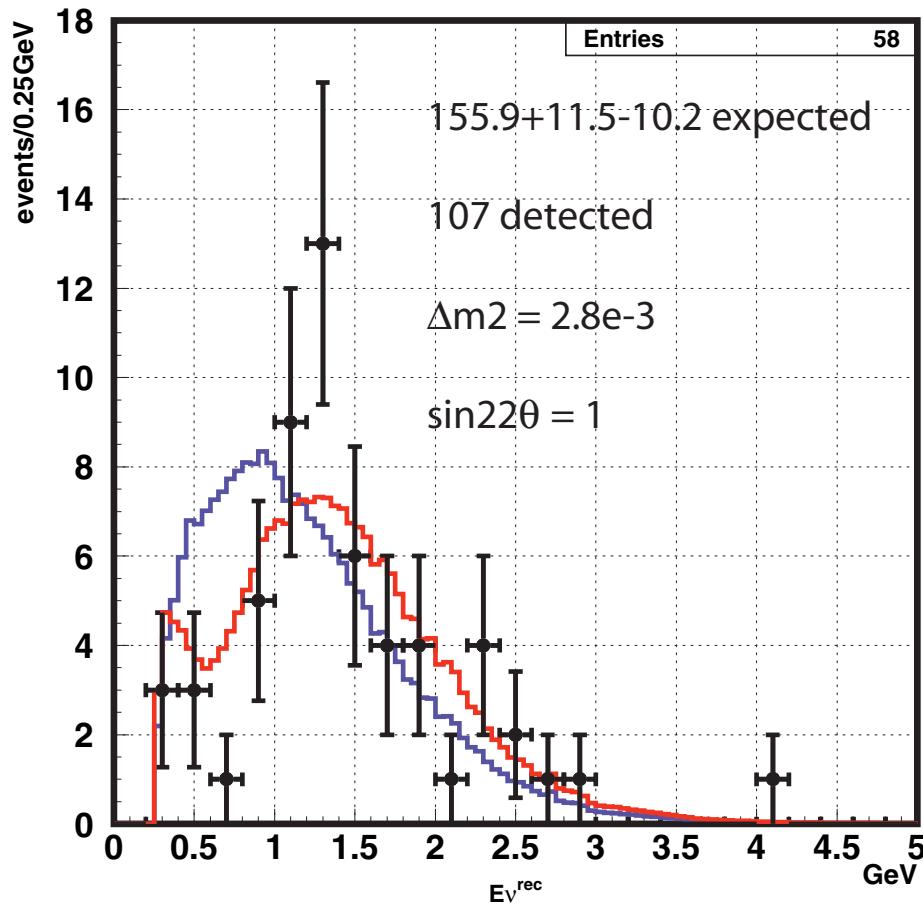
# Principle of Long Baseline Experiments



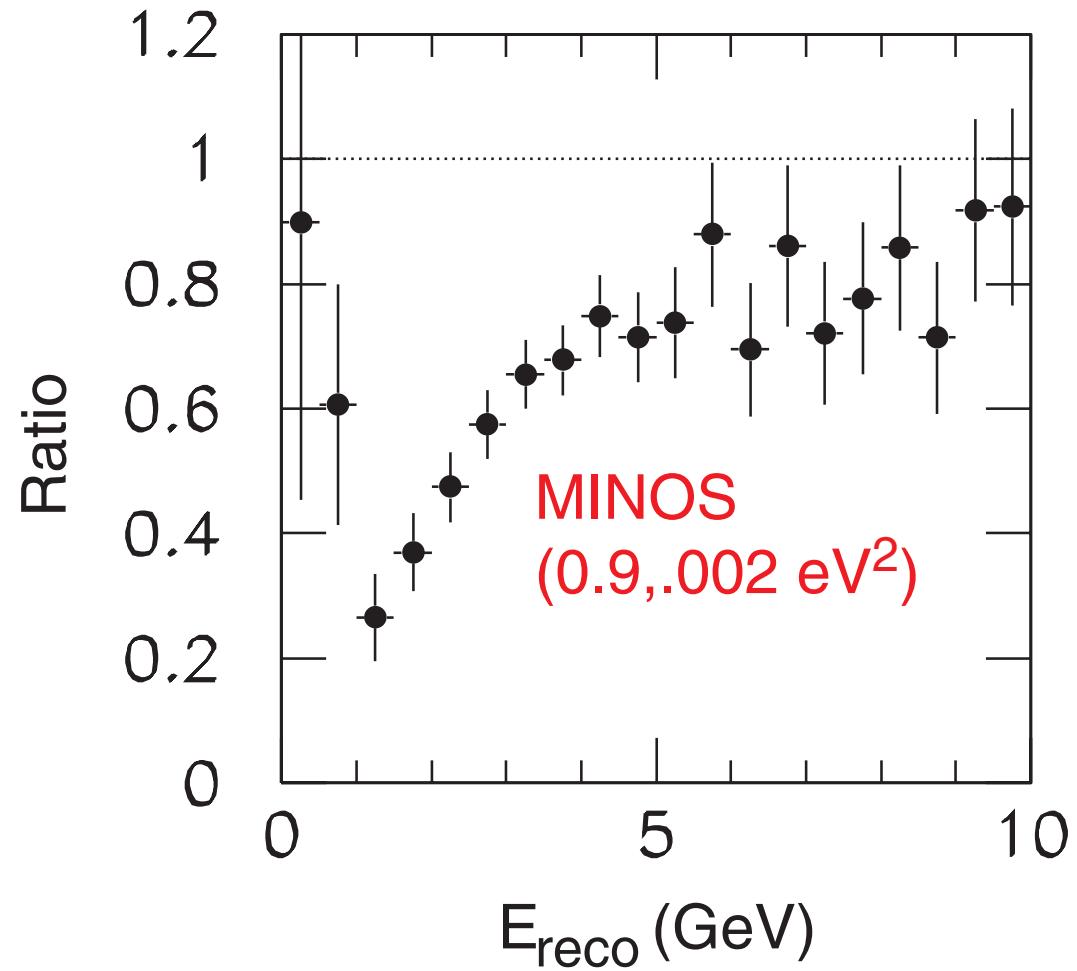
- distortion in the neutrino energy spectrum
- reduction in the number of events

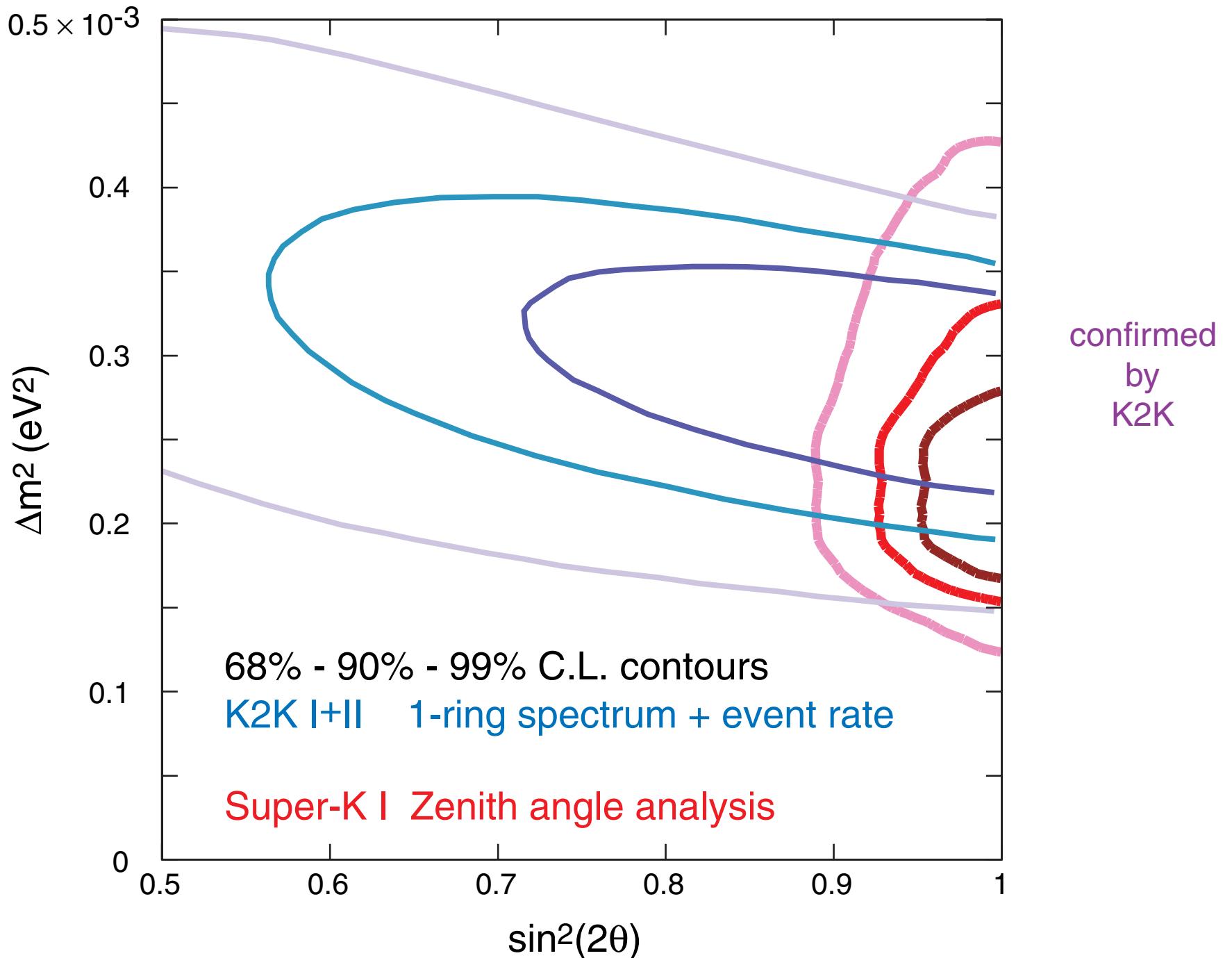


# K2K results

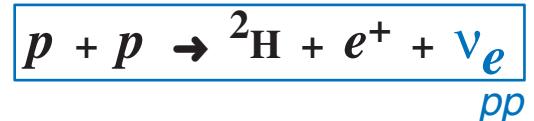
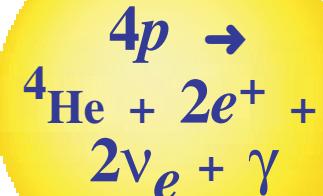
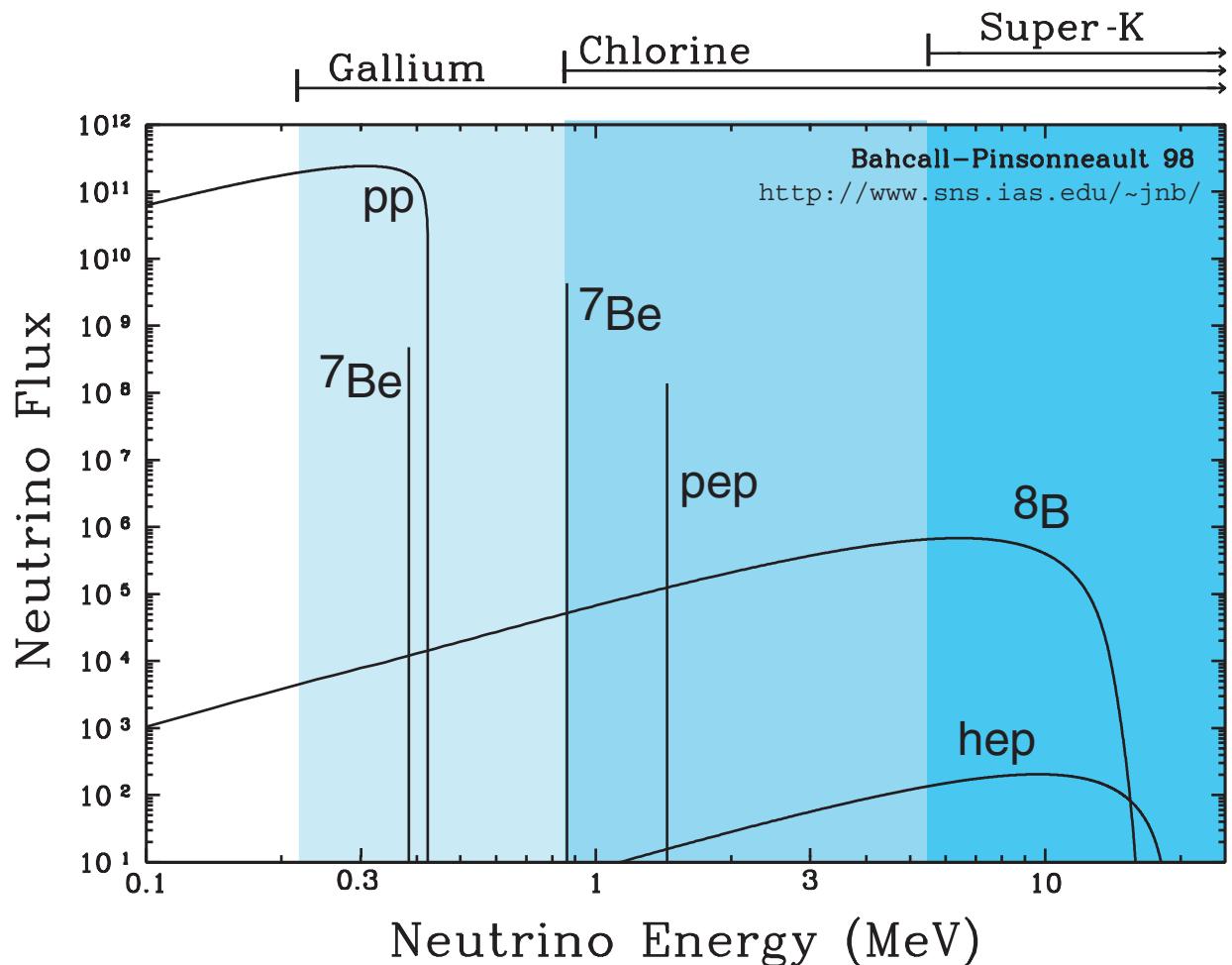


# MINOS expectation

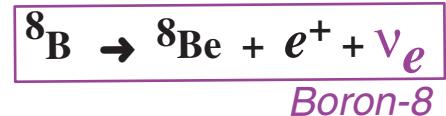




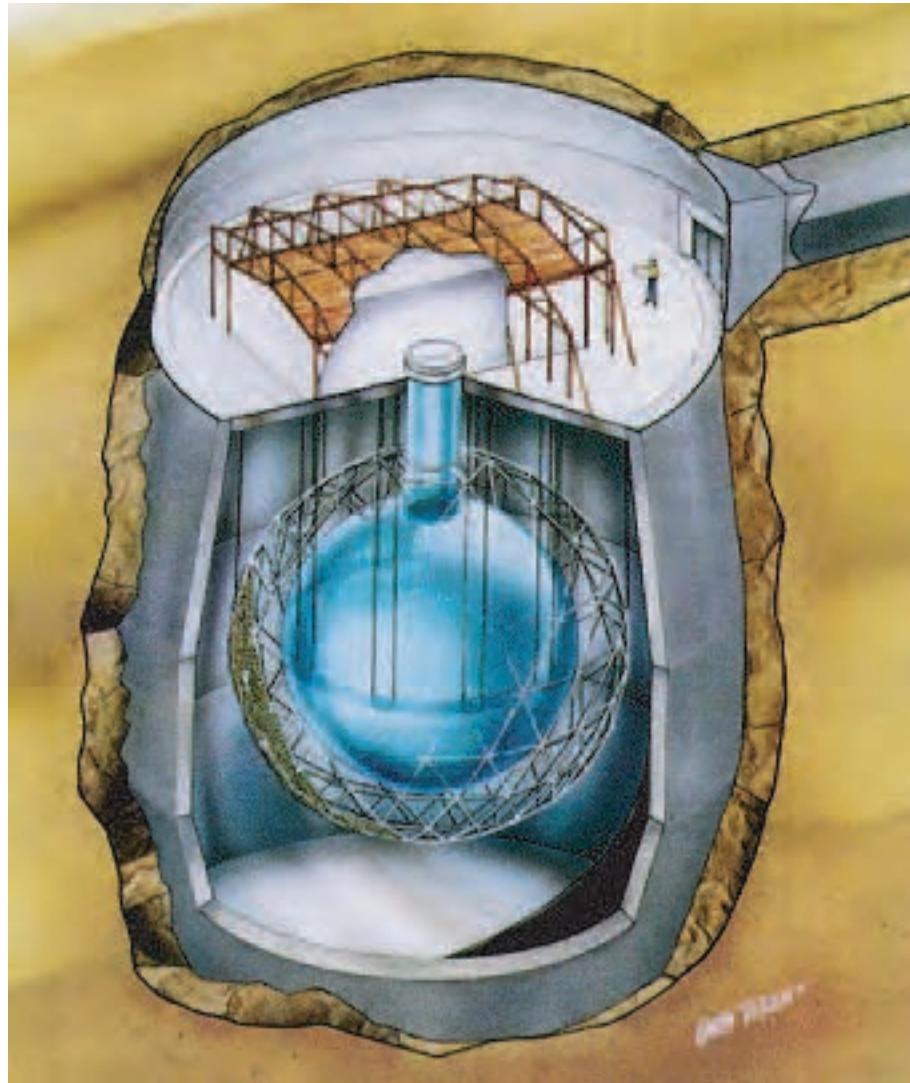
# Solar Neutrinos



Beryllium-7

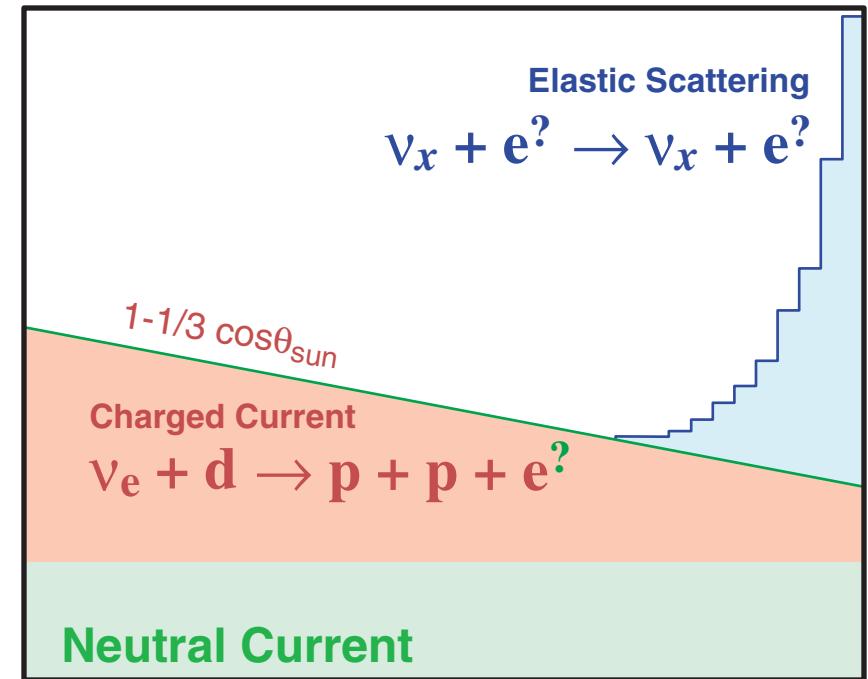


# SNO: Sudbury Neutrino Observatory



- 2073 m underground (~70 cosmic rays/day)
- 1 kton heavy water ( $D_2O$ )
- 9500 20-cm photomultiplier tubes
- separately measure  $\nu_e$  from  $\neq \nu_e$

Angle between  $\nu$  and sun



n-capture on d

n-capture on Cl  
(add MgCl)

n-capture on  $^3He$   
(add  $^3He$  counters)

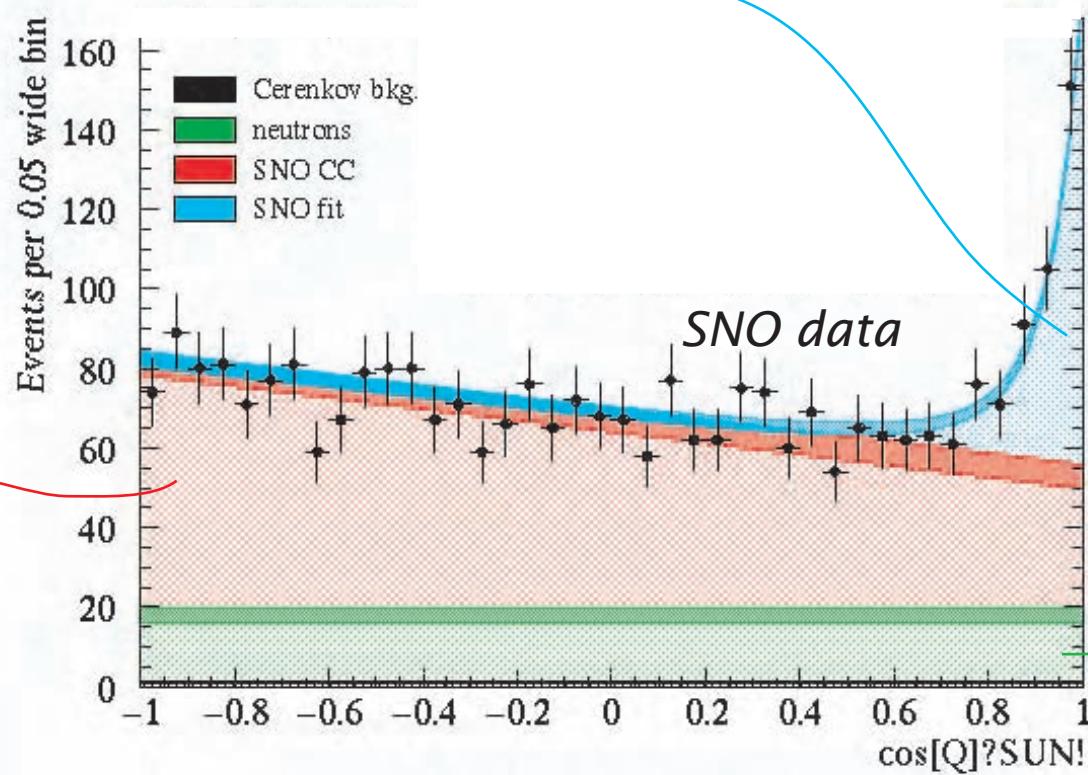
$x = e \text{ or } \mu \text{ or } \tau$

Note!:  
 so deep underground  
 and clean  
 that there is  
 nearly no  
 radioactive  
 background

# SNO Results

*elastic scattering:*  
*mostly  $\nu_e$  + some  $\nu_\mu$  +  $\nu_\tau$*

*charged current:*  
*all  $\nu_e$*



*neutral current:*  
 $\nu_e + \nu_\mu + \nu_\tau$

$$\nu_e \text{ only: } \Phi_{CC} = 1.68^{+0.06}_{-0.06} (\text{stat.})^{+0.08}_{-0.09} (\text{sys.}) \times 10^6 \text{ cm}^{-2} \text{ s}^{-1}$$

$$\Phi_{ES} = 2.35^{+0.22}_{-0.22} (\text{stat.})^{+0.15}_{-0.15} (\text{sys.}) \times 10^6 \text{ cm}^{-2} \text{ s}^{-1}$$

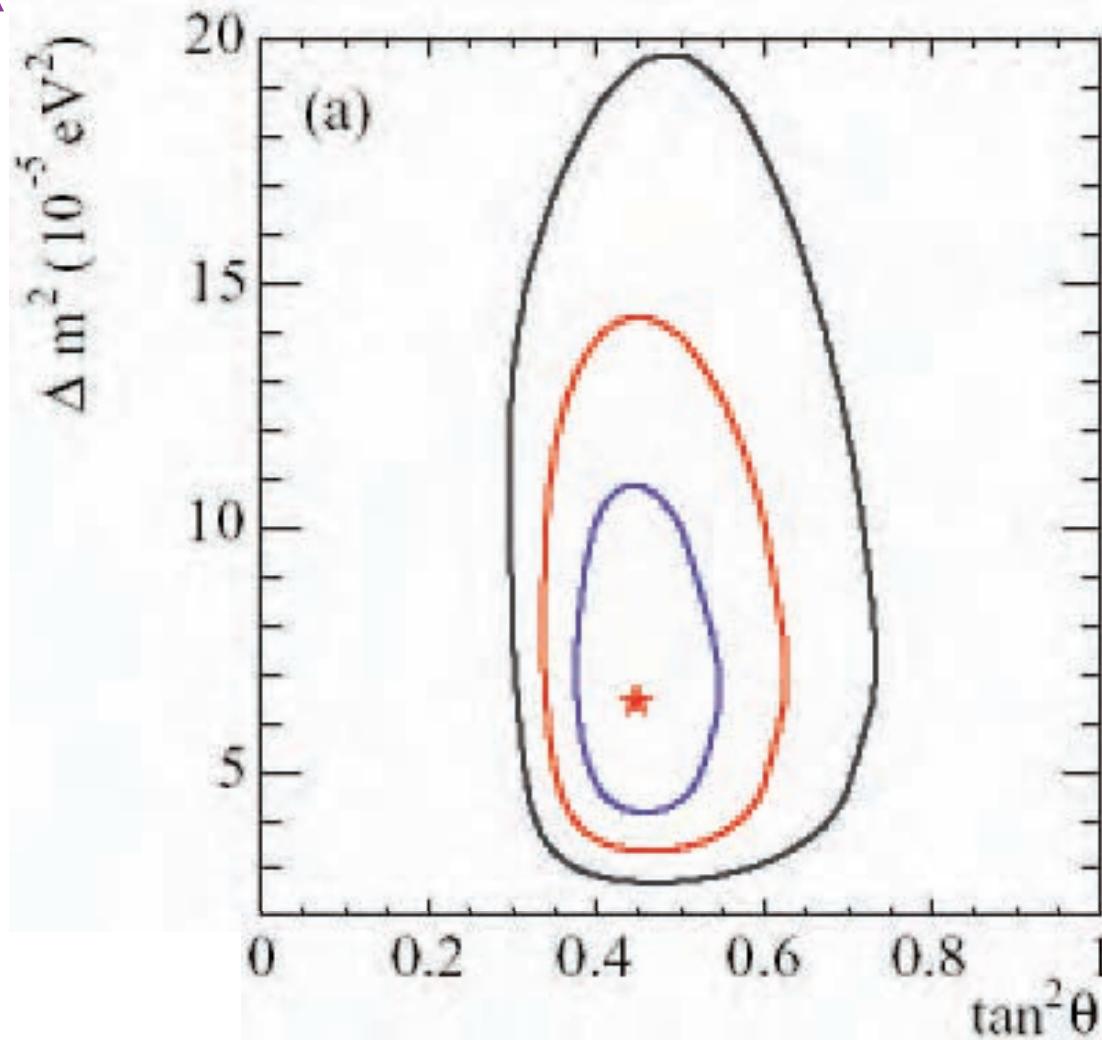
}

$\neq$

$$\nu_e + \nu_\mu + \nu_\tau: \Phi_{NC} = 4.94^{+0.21}_{-0.21} (\text{stat.})^{+0.38}_{-0.34} (\text{sys.}) \times 10^6 \text{ cm}^{-2} \text{ s}^{-1}$$

$$\Phi_{BP04} = 5.82 \pm 1.34 \times 10^6 \text{ cm}^{-2} \text{ s}^{-1}$$

# Solar Result (SNO+SK+Homestake+GNO+GALLEX+SAGE)



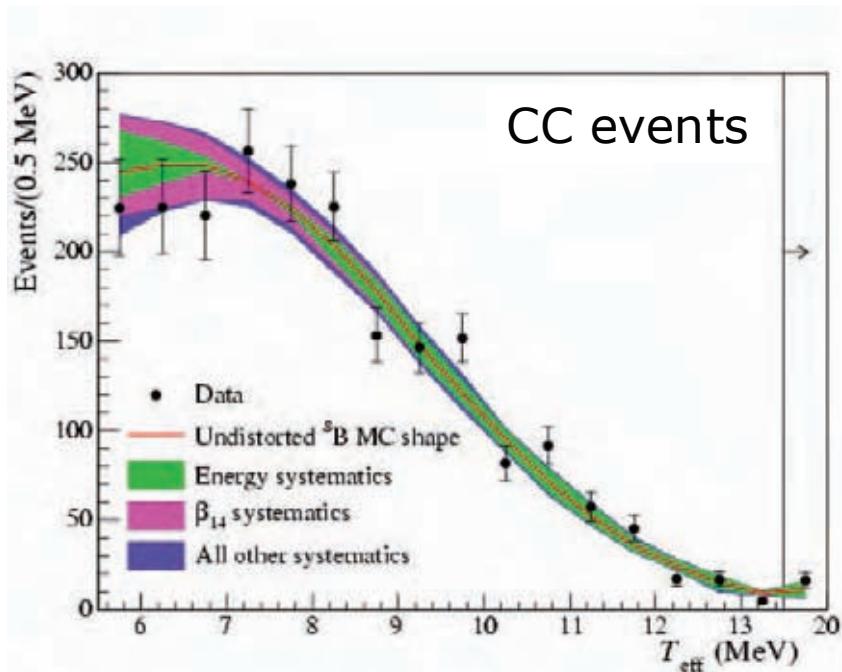
$$\Delta m_{12}^2 = 6.5^{+4.4}_{-2.3} \times 10^{-5} \text{ eV}^2$$

$$\tan^2 \theta_{12} = 0.45^{+0.09}_{-0.08}$$

large mixing  
(but not maximal)

# Where's the Smoking MSW Gun?

(besides SNO's NC/CC of course)

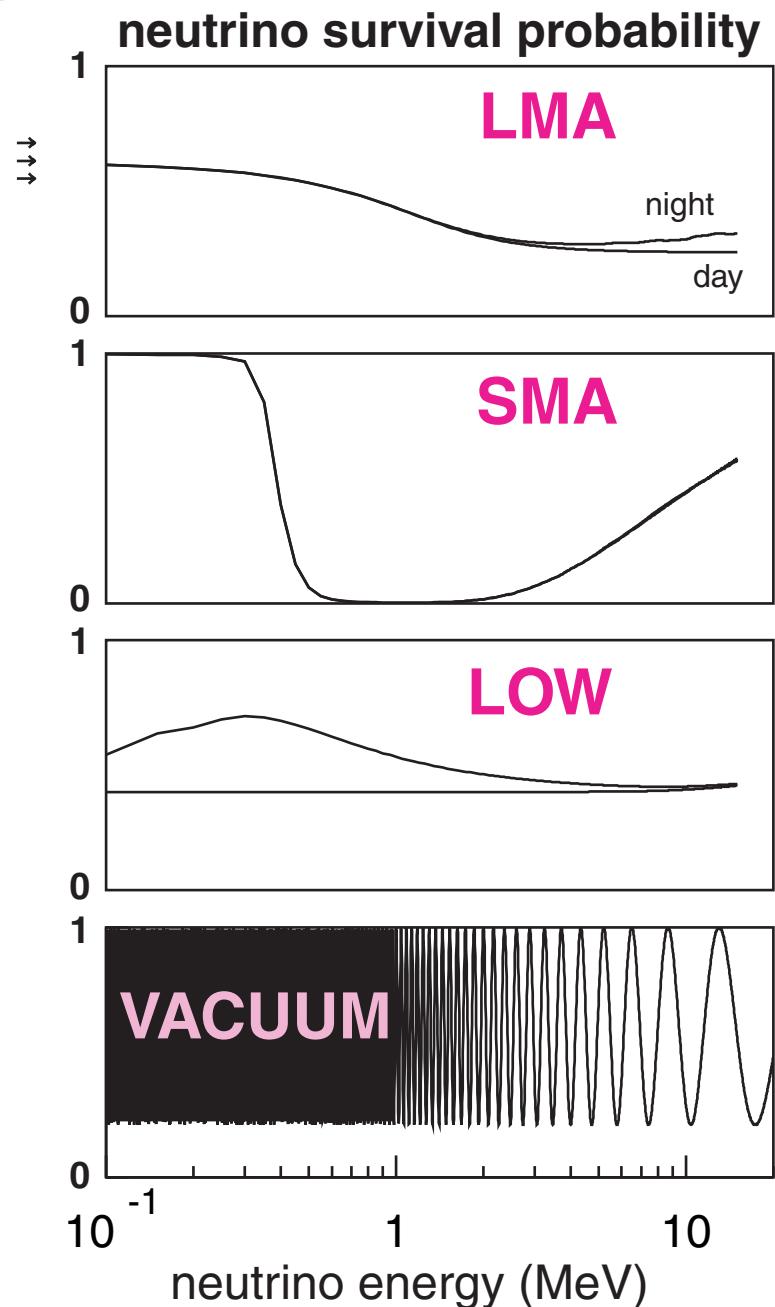


SK also sees no significant spectral distortion

$$\text{SK day/night asymmetry} = 0.021 \pm 0.020$$

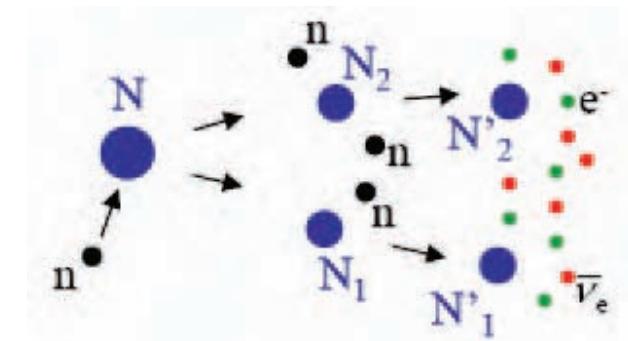
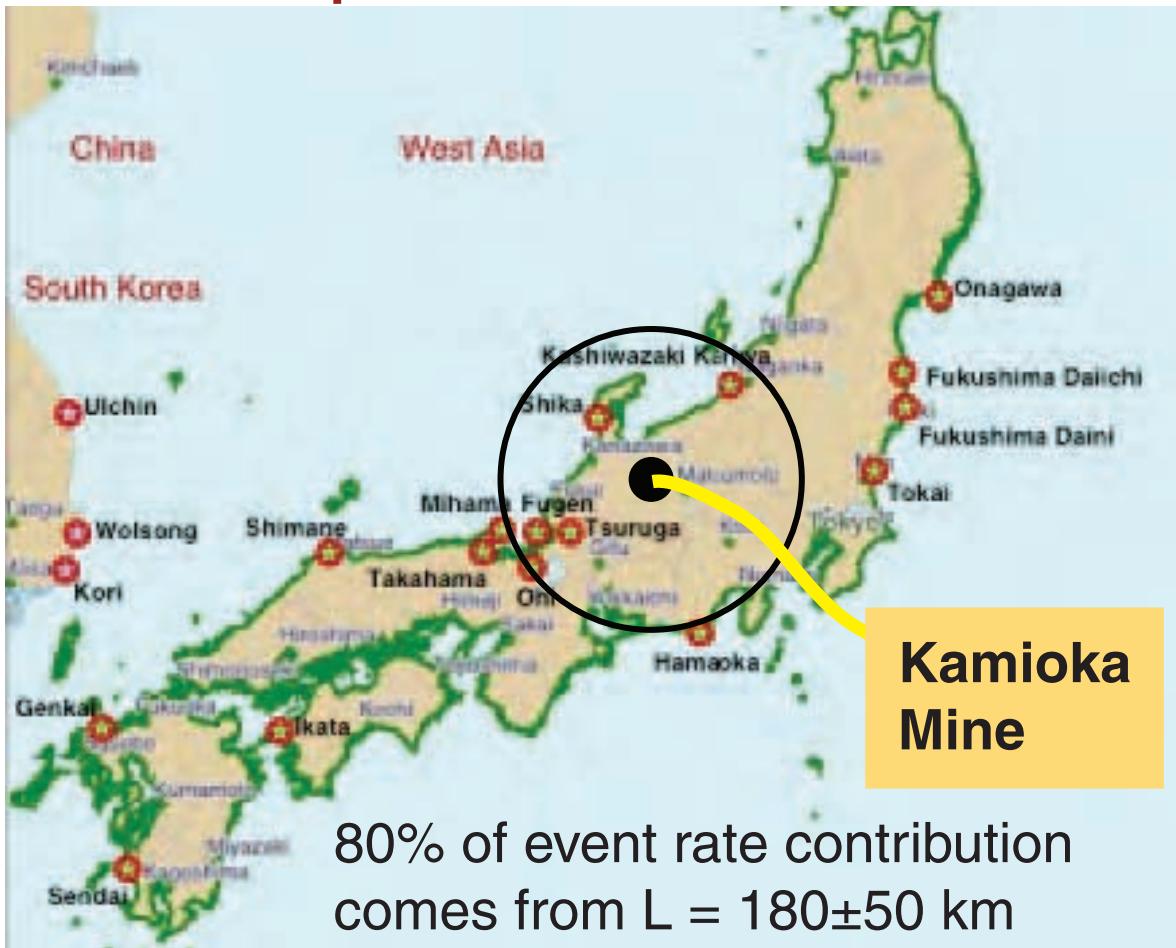
$$\text{SNO day/night asymmetry} = 0.037 \pm 0.040$$

no seasonal variation except  $1/r^2$

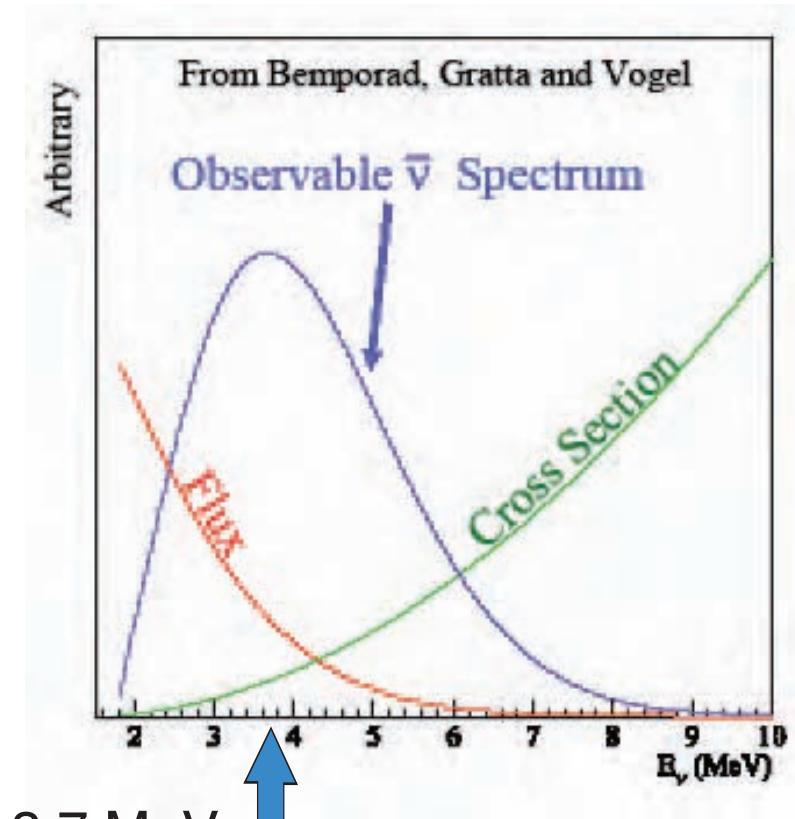


# KamLAND Reactor Experiment

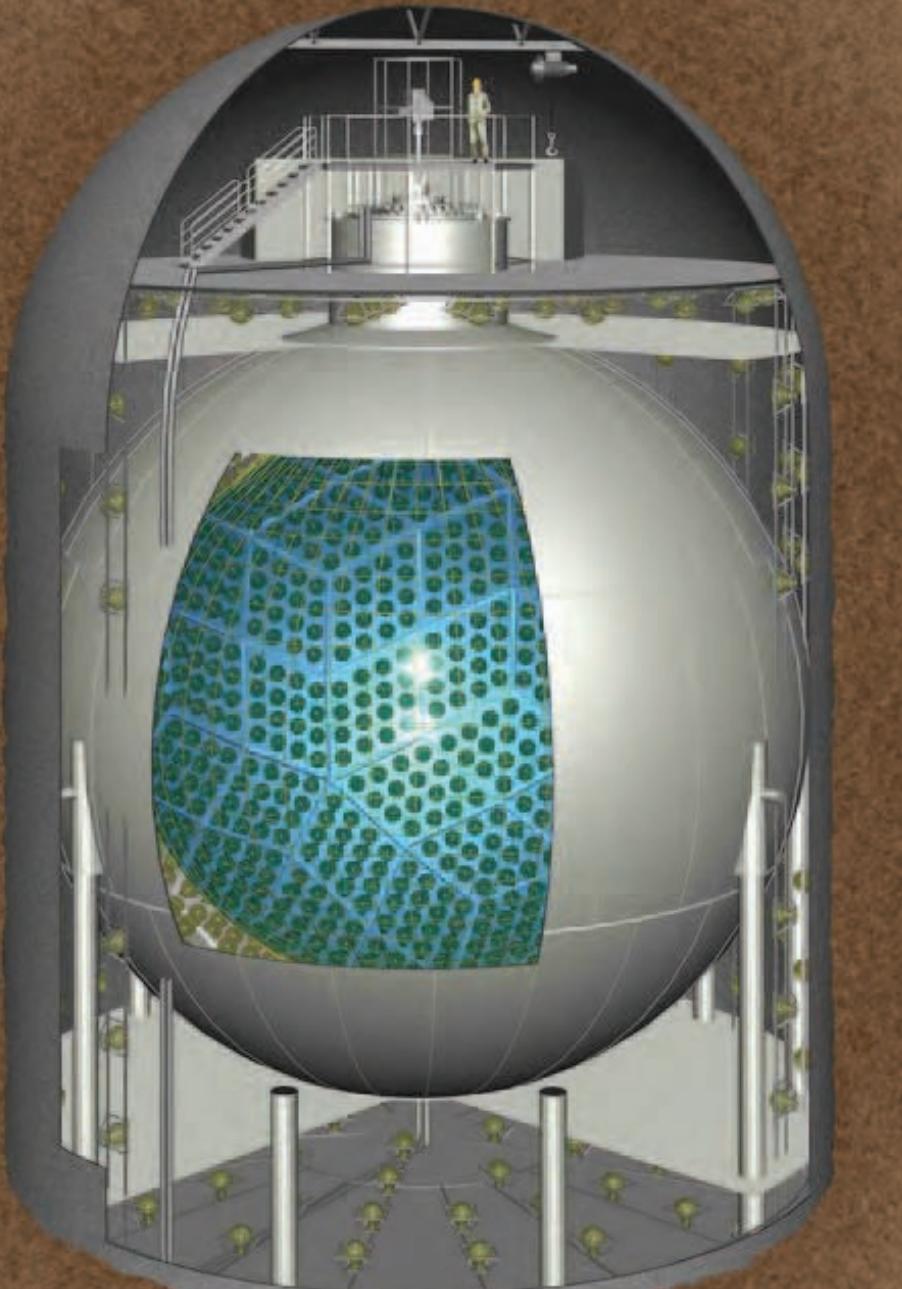
## Japanese Power Reactors



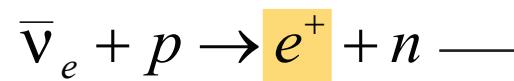
$\sim 6 \bar{\nu}_e / \text{fission}$



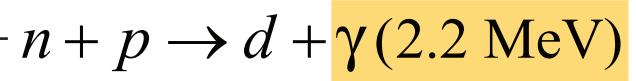
# KamLAND Detector



1000 ton liquid scintillator  
in plastic balloon  
surrounded by mineral oil  
viewed by 1879 PMTs  
in stainless steel sphere  
shielded by active water Cherenkov



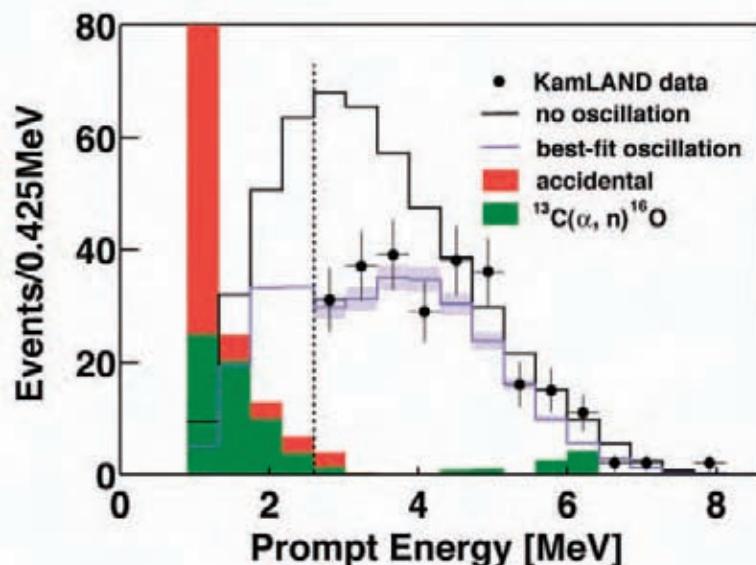
$E_{thresh} = 1.8 \text{ MeV}$



$\tau \sim 210 \mu\text{sec}$

~1000 events/yr

# KamLAND Results

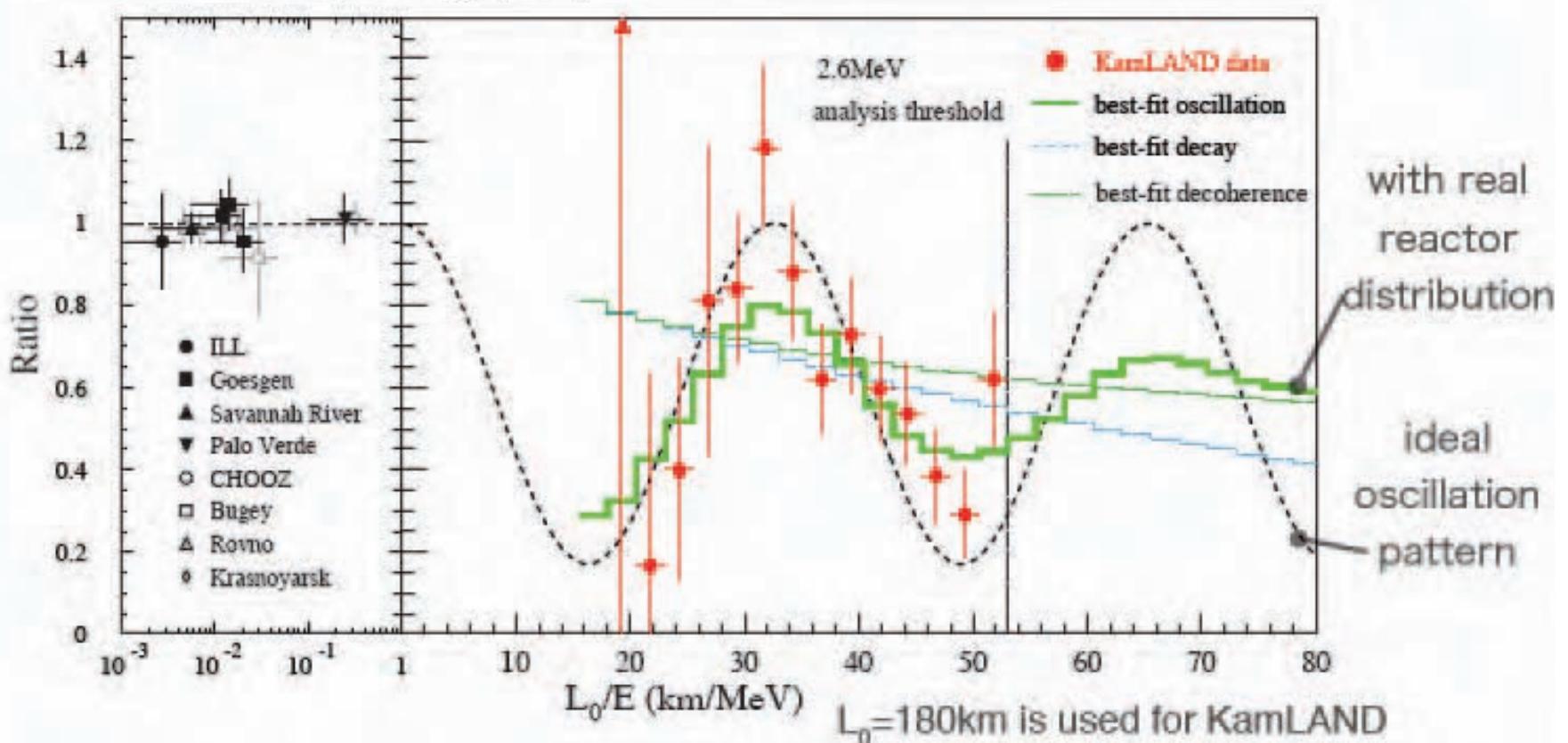


expected =  $365.2 \pm 23.7$  events  
observed = 258 events  
background =  $17.8 \pm 7.3$  events

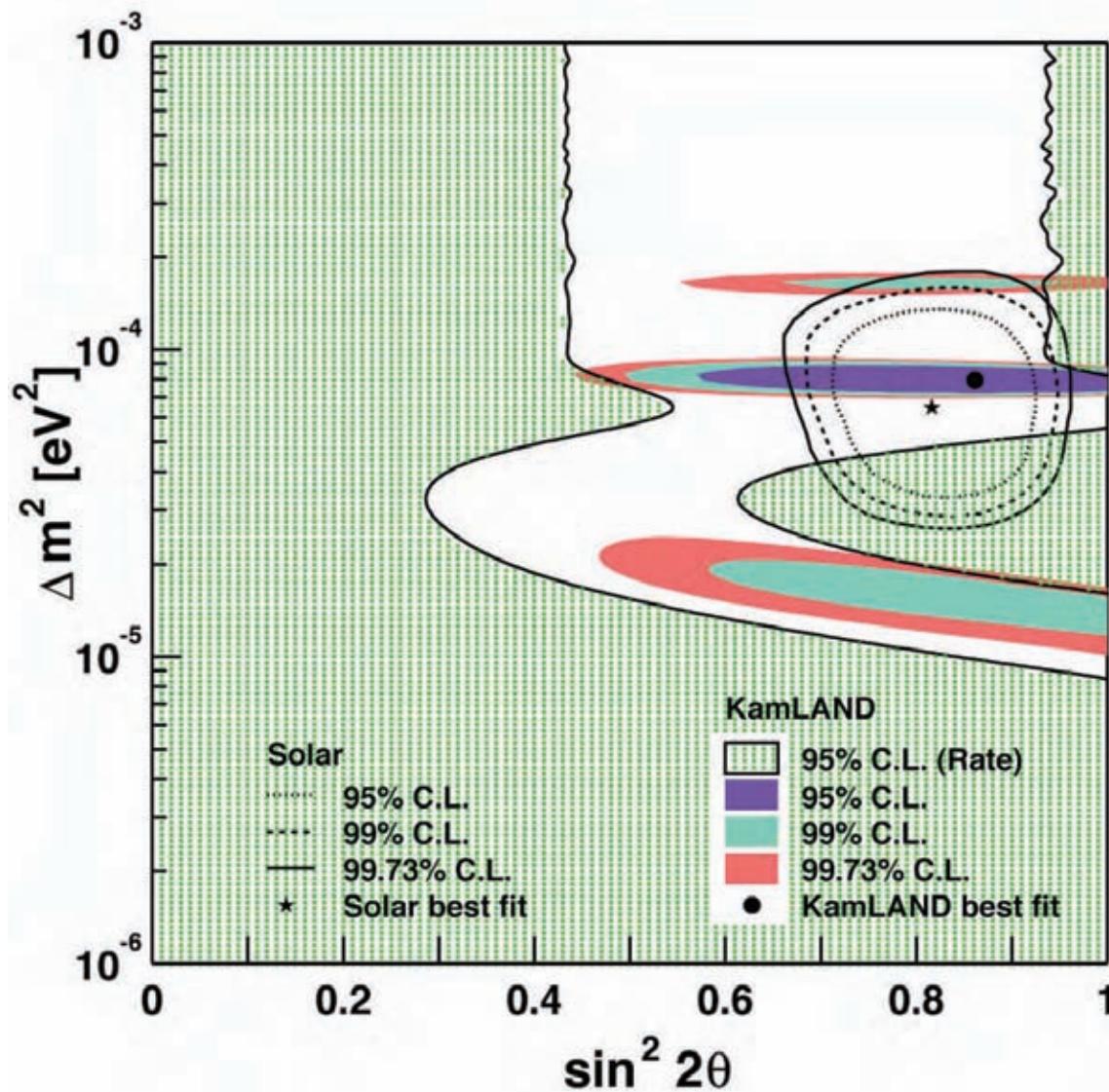
best fit:

$$\Delta m^2 = 7.9 \times 10^{-5} \text{ eV}^2$$

$$\sin^2 2\theta = 0.863$$

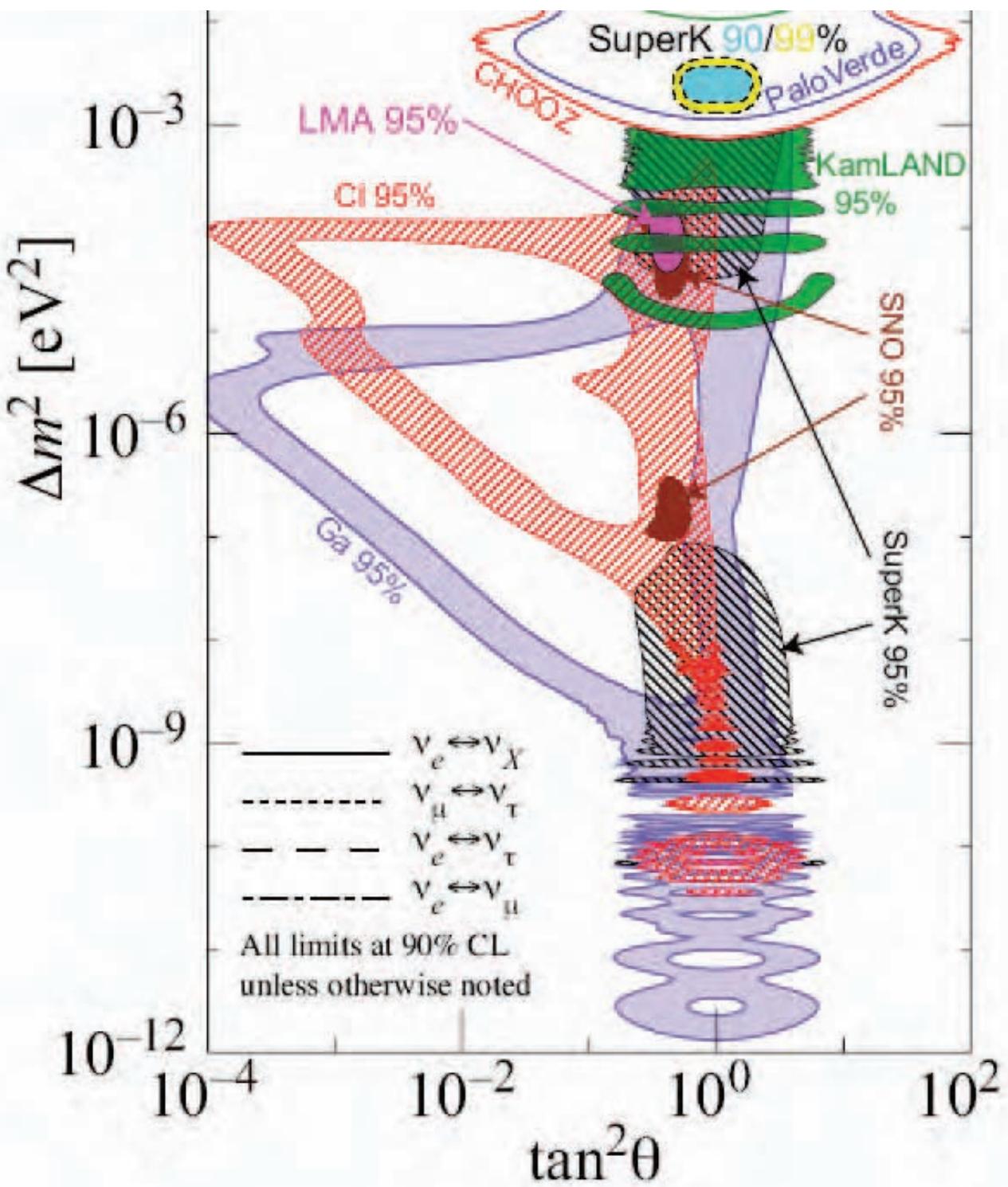


# KamLAND compared with Solar

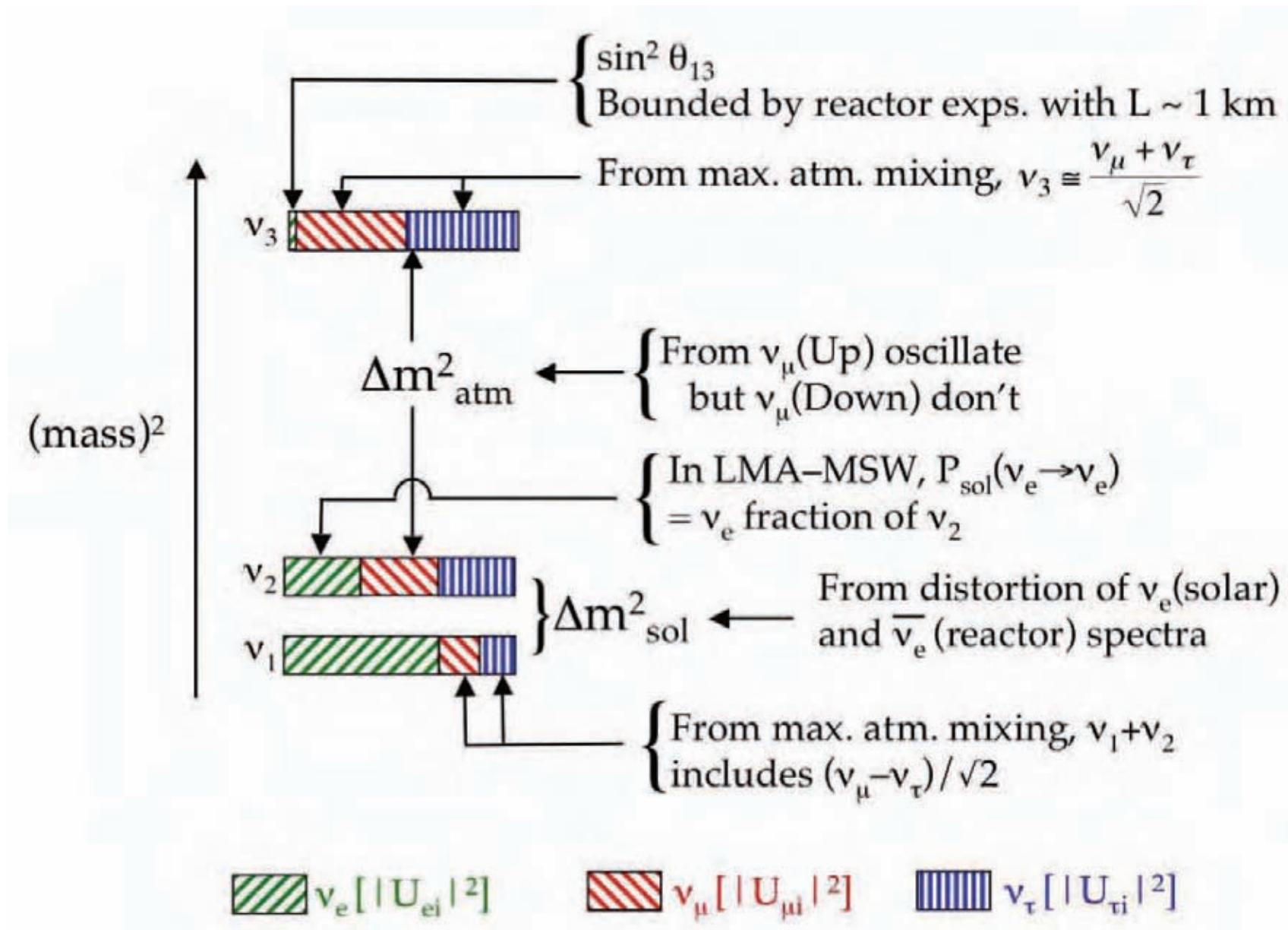


*KamLAND measurement is based on vacuum oscillation;  
solar survival probability relies on matter effect. Important comparison!*

IF YOU  
CAN  
UNDERSTAND  
THIS PLOT  
YOU ARE  
STANDING  
TOO  
CLOSE



# Current Picture of Neutrino Mass and Mixing



# A Useful Parametrization of the PMNS Matrix

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \times \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \times \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$\theta_{23} \sim \theta_{atm.} \approx 45^\circ$$

$$\theta_{13} < 12^\circ$$

$$\theta_{12} \sim \theta_{solar} \approx 32^\circ$$

$\delta$  is totally unknown

**why is it like this ???**

$$U_{CKM} = \begin{pmatrix} 1 & 0.2 & 0.005 \\ 0.2 & 1 & 0.04 \\ 0.005 & 0.04 & 1 \end{pmatrix}$$

**quarks**

$$U_{PMNS} = \begin{pmatrix} 0.8 & 0.5 & ? \\ 0.4 & 0.6 & 0.7 \\ 0.4 & 0.6 & 0.7 \end{pmatrix}$$

**neutrinos**

# What We Do Not Yet Know

- Are there only three neutrino states? (LSND)
- Can we really make an appearance experiment?
- What is the absolute mass scale?
- Are neutrinos their own antiparticle? (Majorana)
- What is the sign of the large  $\Delta m^2$ ? (heirarchy  $\overline{\overline{m}}$  or  $\overline{\overline{m}}$ )
- What is the value of  $\theta_{23}$ ? Is it truly maximal?
- What is the value of  $\theta_{13}$ ? Is it really zero?
- What is the value of  $\delta$ ?

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GUTs like this!
- What is the sign of the large  $\Delta m^2$ ? (heirarchy  $\underline{\underline{=}}$  or  $\underline{\underline{\equiv}}$ )  
0v $\beta\beta$  expts wish for this.
- What is the value of  $\theta_{23}$ ? Is it truly maximal?
- What is the value of  $\theta_{13}$ ? Is it really zero?  
must be > 0 to see CP violation
- What is the value of  $\delta$ ? **CP violation!**

$$P(\nu_\mu \rightarrow \nu_e) \neq P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$$

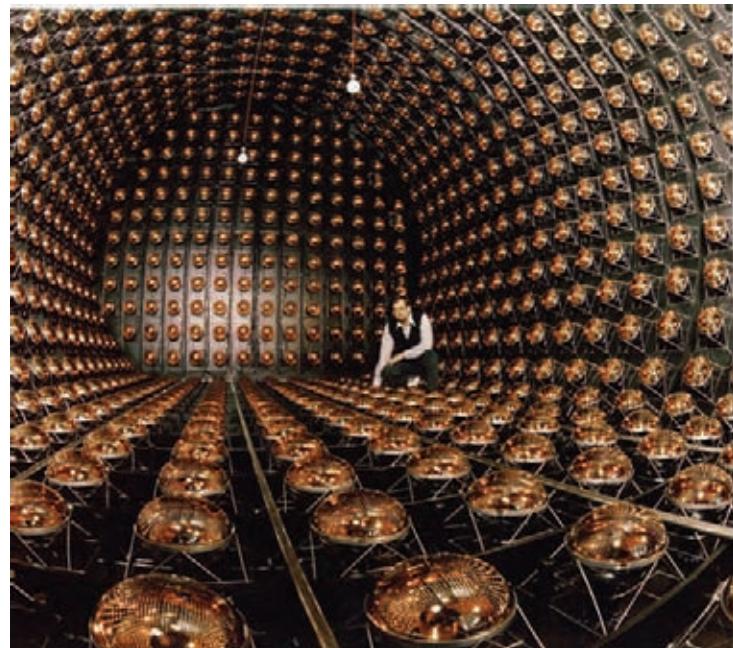
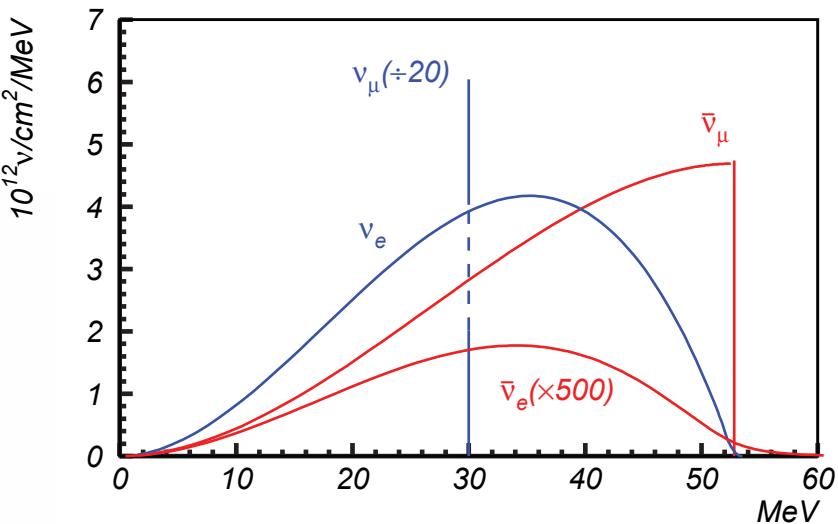
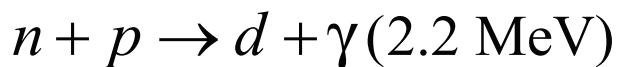
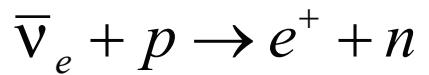
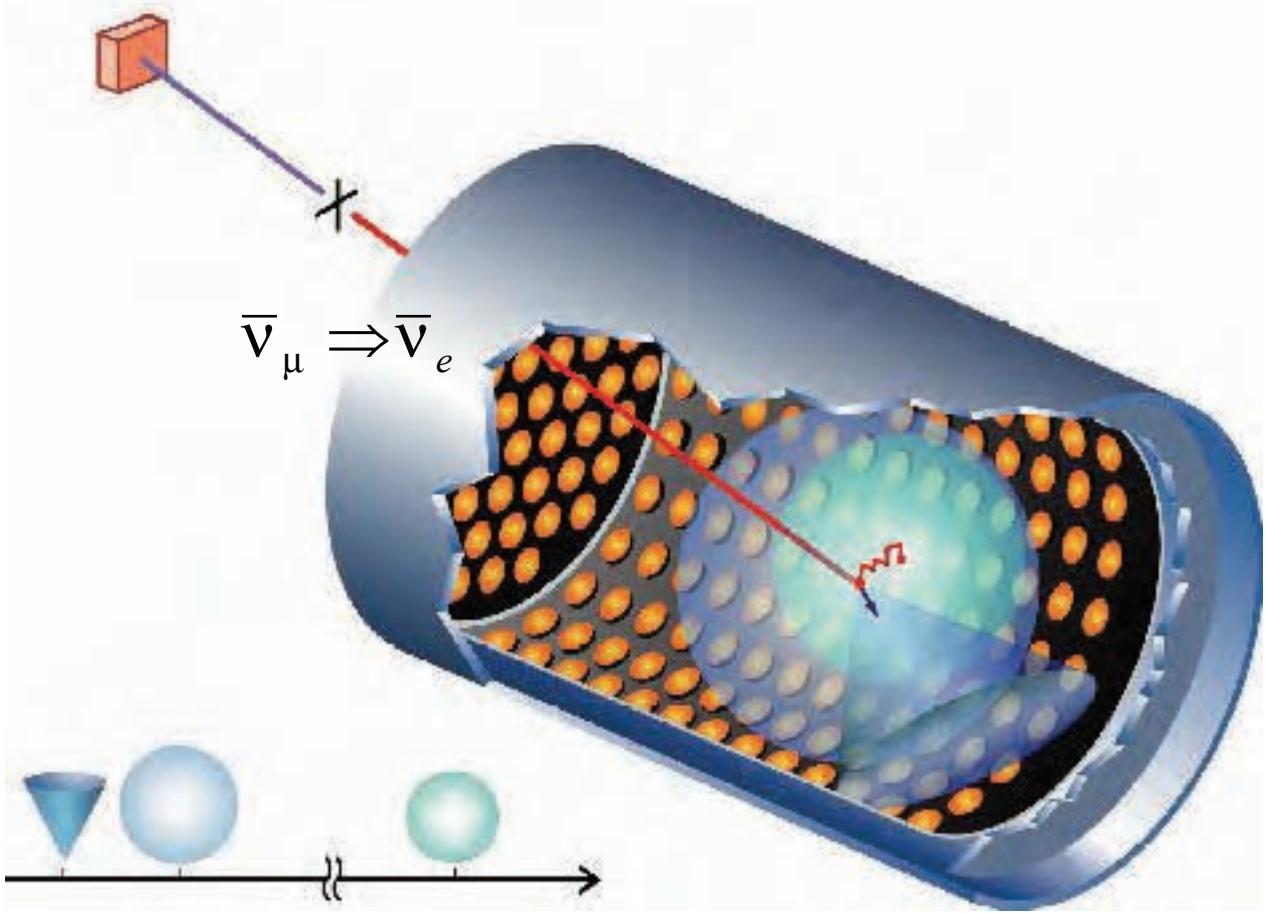
GUTs  
want to  
know!

# LSND Experiment

$$\pi^+ \rightarrow \mu^+ + \nu_\mu$$

$$\mu^+ \rightarrow e^+ + \nu_e + \bar{\nu}_\mu$$

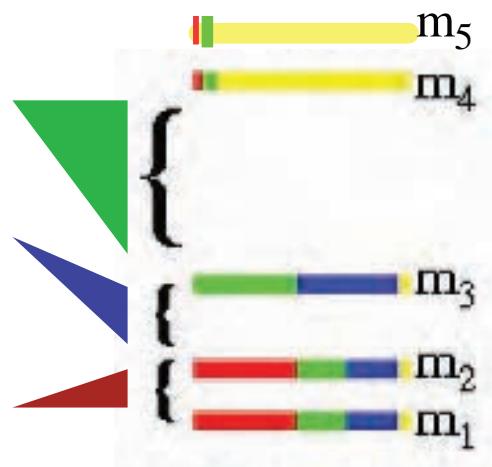
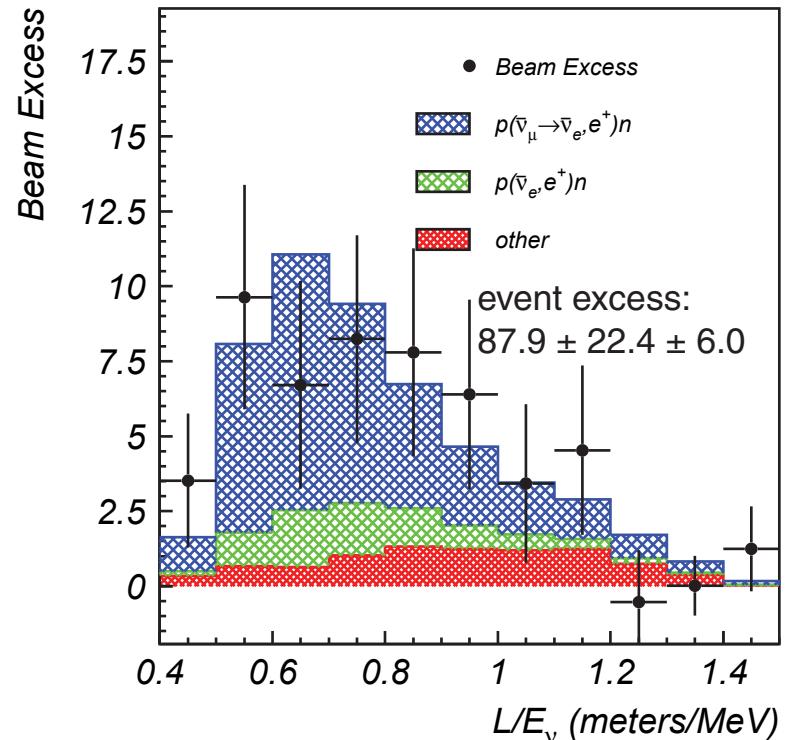
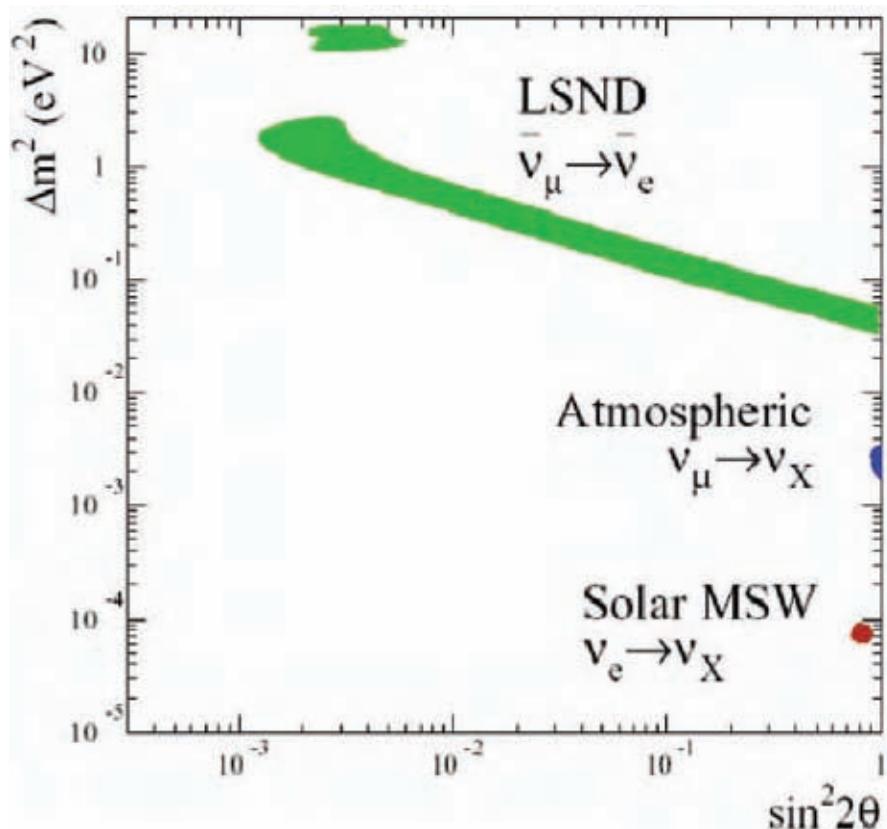
stopped pion beam  $\Rightarrow$   
decay-at-rest spectra:



# LSND Result

a fourth oscillation  
signature (with  
active neutrinos!)  
is a problem

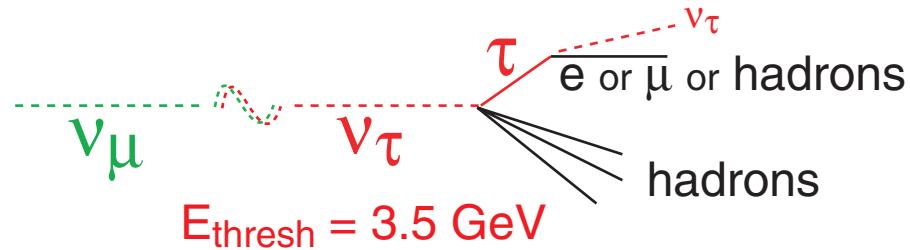
will be tested by mini-BooNE this year



$$\Delta m_{ij}^2 \equiv m_j^2 - m_i^2$$

$$\Delta m_{13}^2 = m_{12}^2 + m_{23}^2$$

# Tau Appearance



expect ~100 events

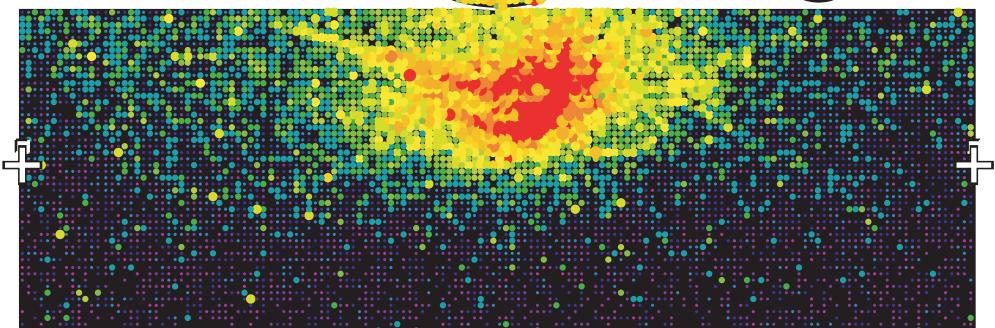
events have large visible energy (> 2 GeV)

multiple rings  
(not all may be reconstructed)

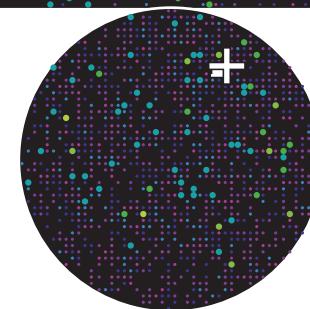
over threshold,  
only upward-going neutrinos  
have sufficient oscillation length

Charge (pe)

●	>60.0
●	52.5-60.0
●	45.5-52.5
●	39.0-45.5
●	33.0-39.0
●	27.5-33.0
●	22.5-27.5
●	18.0-22.5
●	14.0-18.0
●	10.5-14.0
●	7.5-10.5
●	5.0- 7.5
●	3.0- 5.0
●	1.5- 3.0
●	0.5- 1.5
●	< 0.5



try it  
at SK

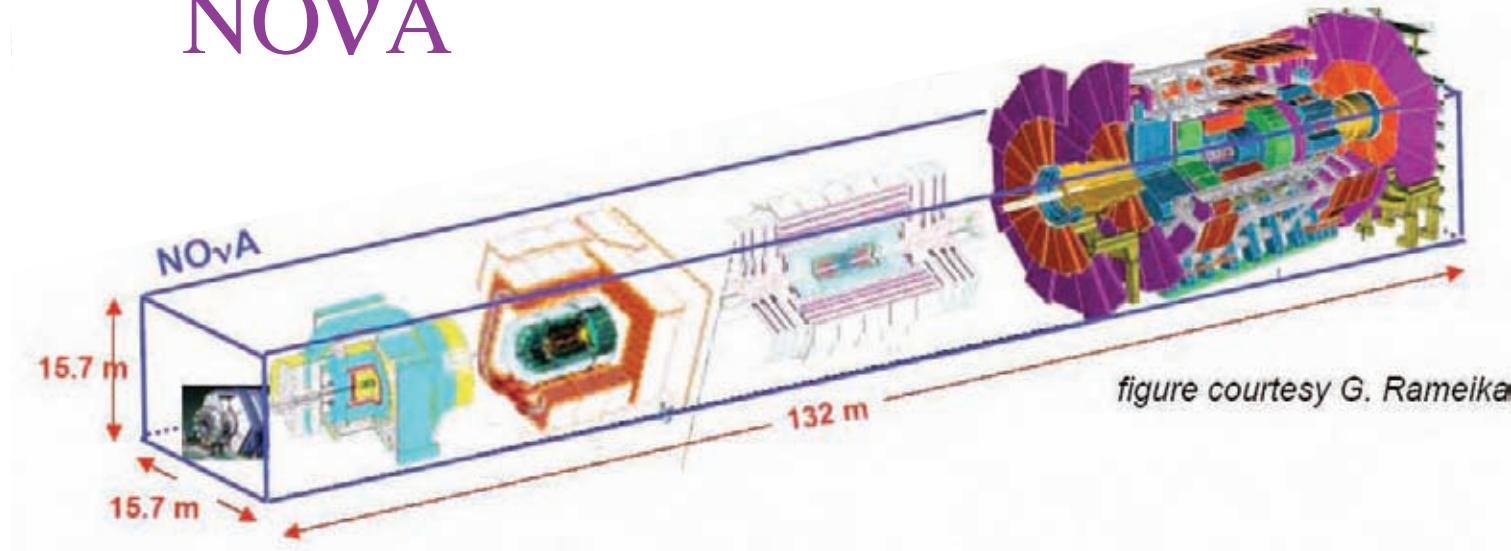


Tau appearance is special emphasis for CNGS (CERN-Gran Sasso) experiment OPERA  
~ only a handful of events, but with emulsion tracdker to identify kink of tau decay

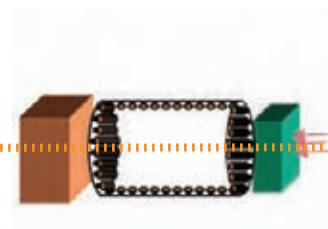
# Off-Axis Experiments

*Let's build a new detector off-axis from the existing NuMI beam!*

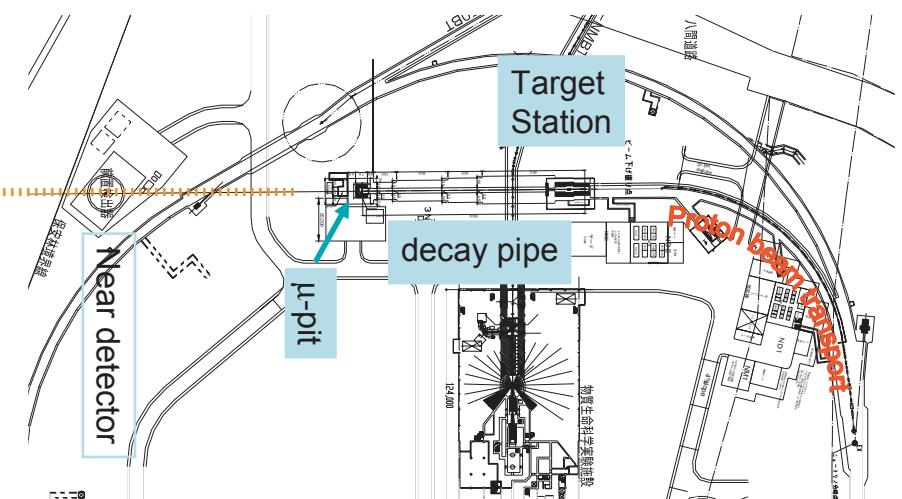
NOVA



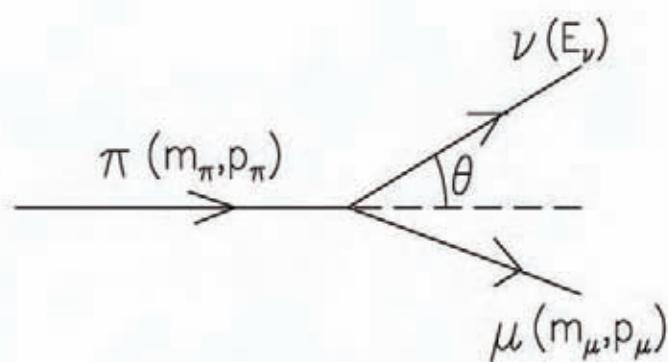
*Let's build a new beam off-axis to the existing Super-K detector!*



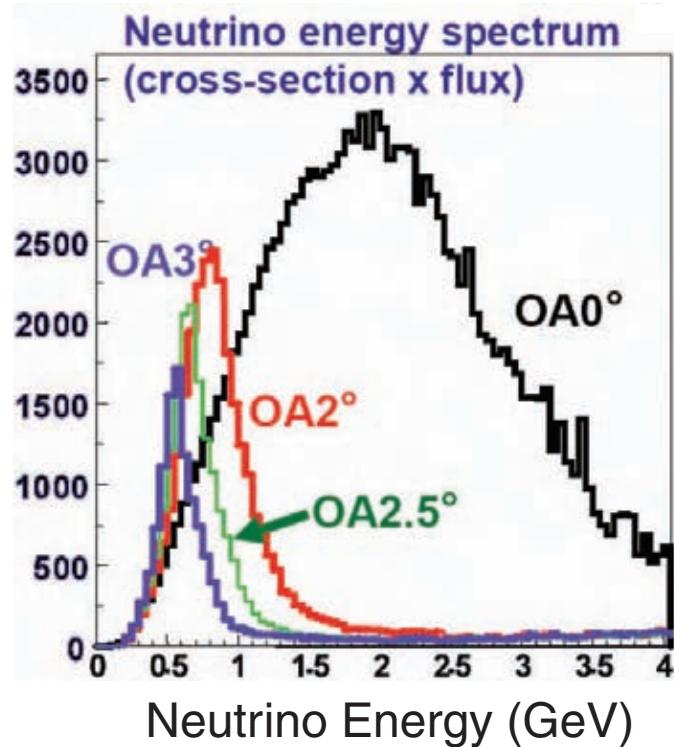
T2K



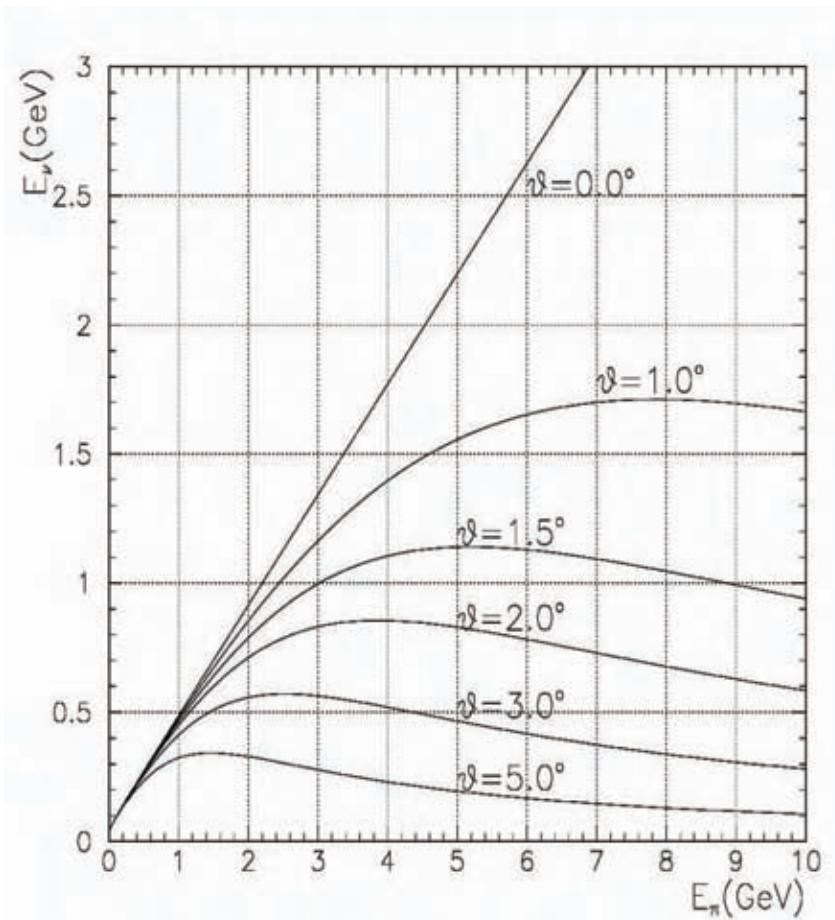
# Off-axis kinematics



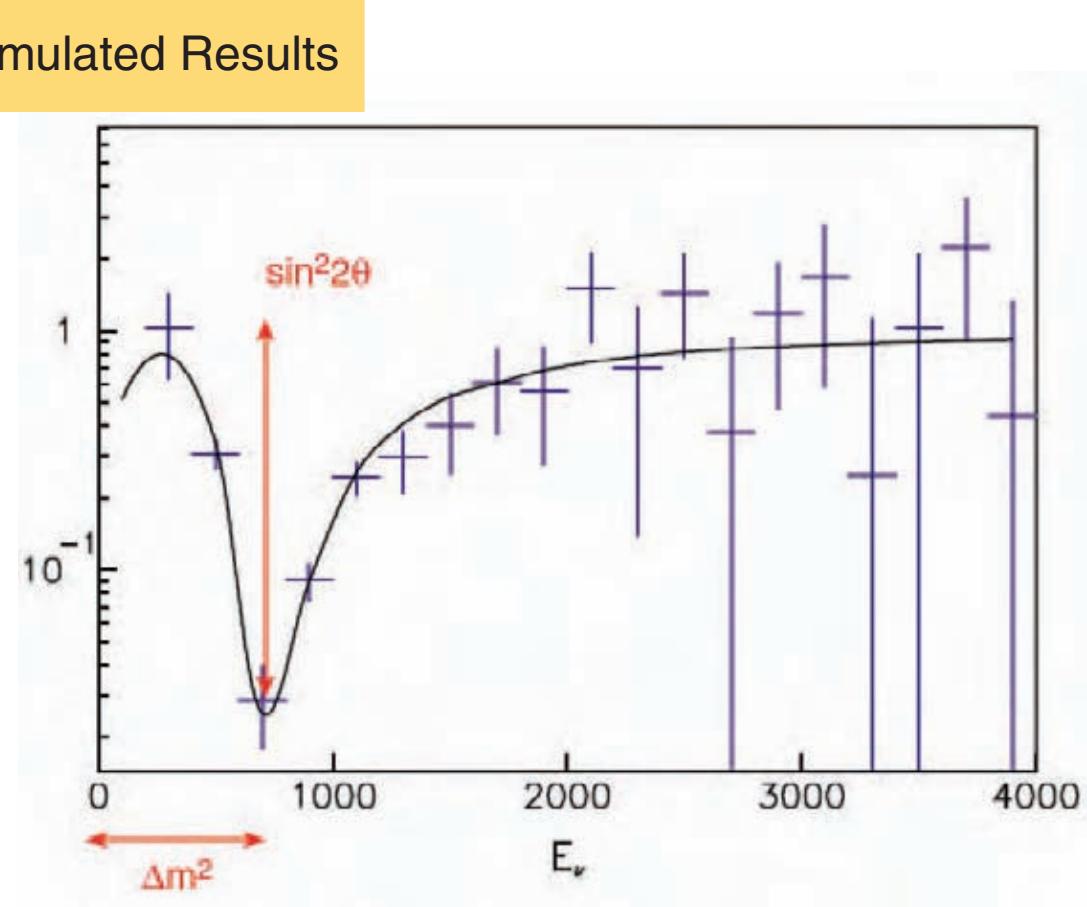
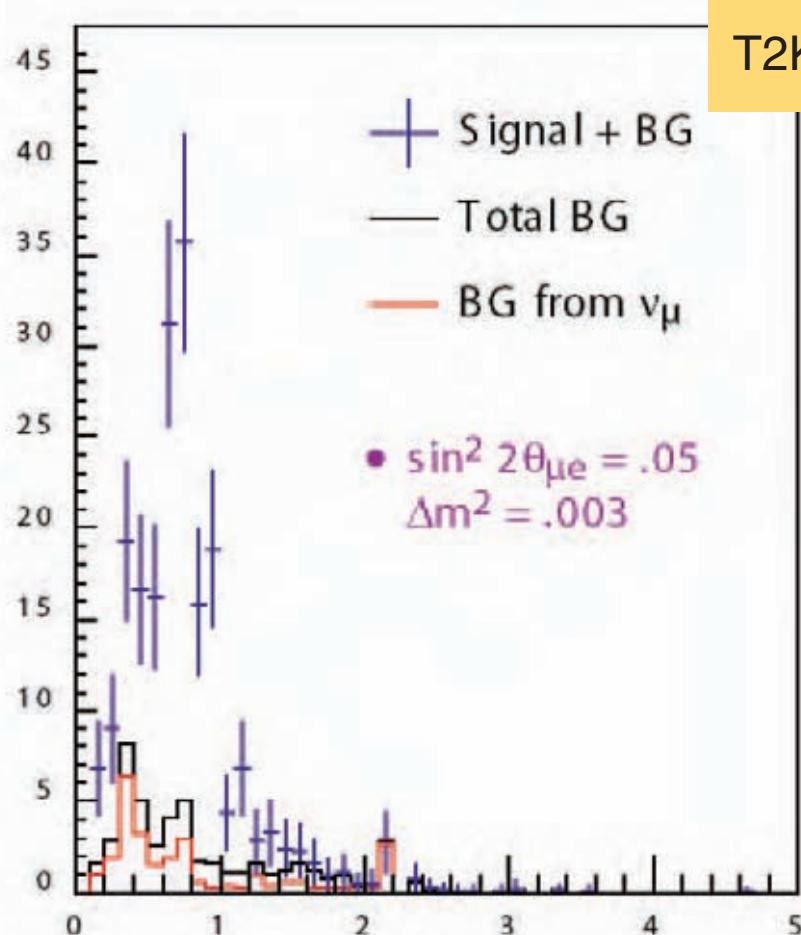
$$E_\nu = \frac{m_\pi^2 - m_\mu^2}{2(E_\pi - p_\pi \cos\theta)}$$



Angle chooses peak energy

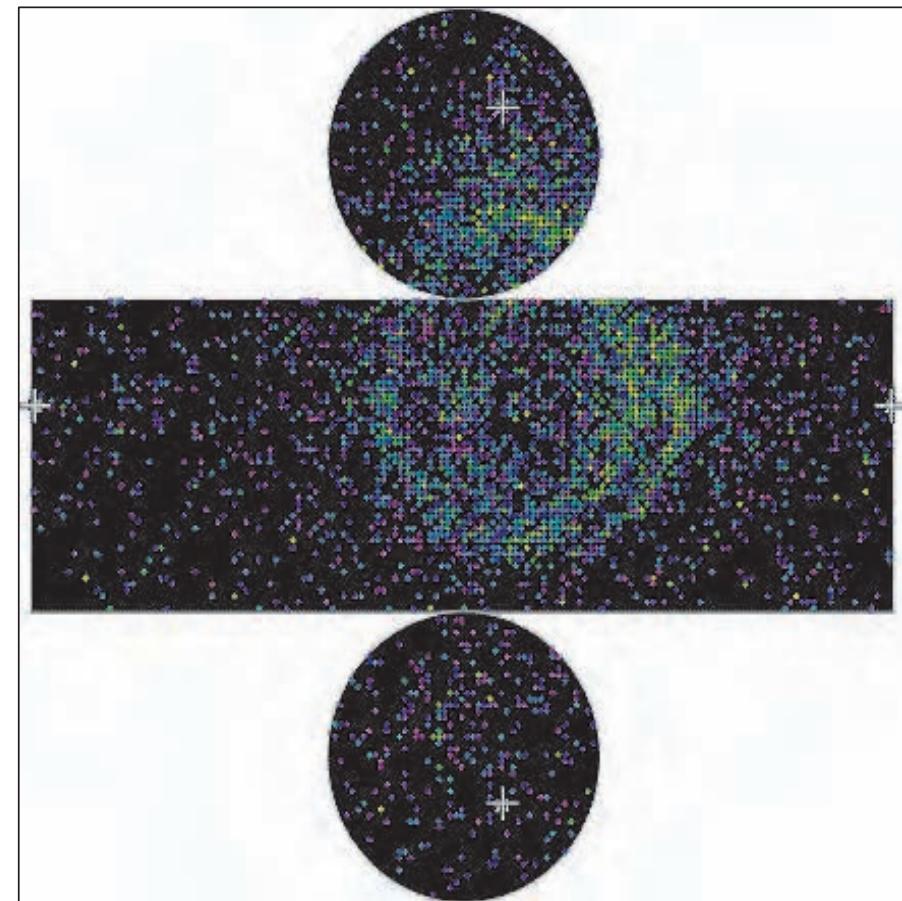
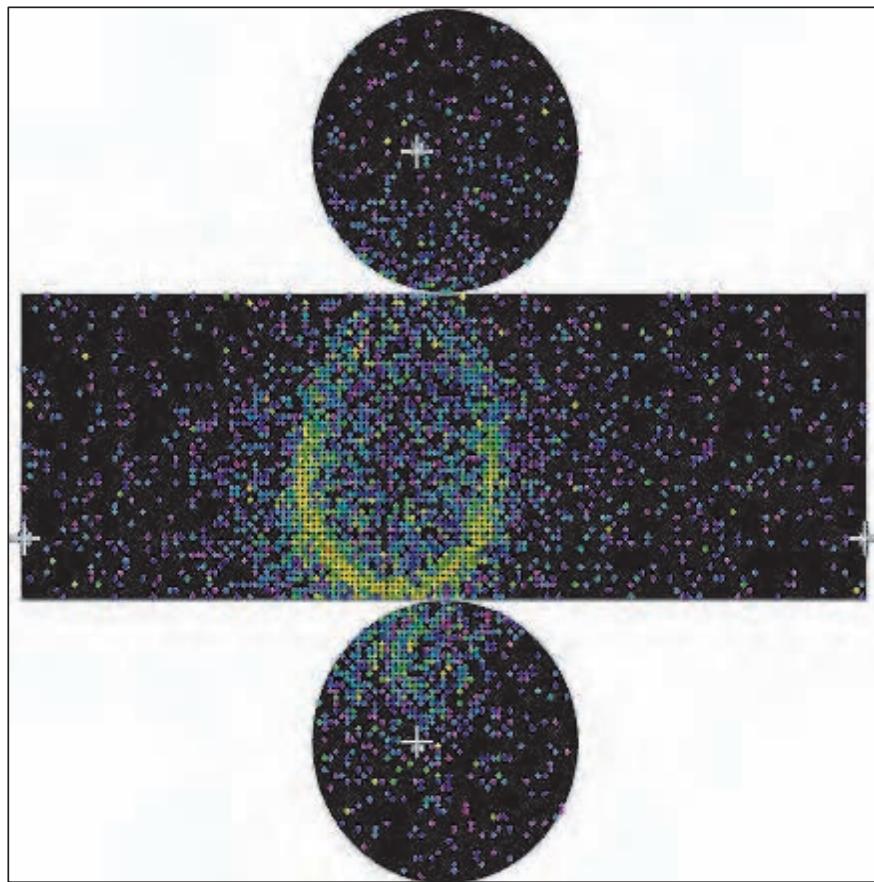


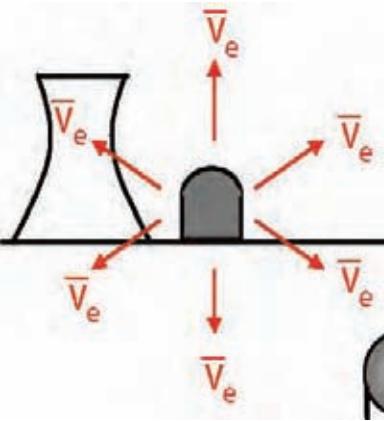
# Electron Neutrino Appearance and Muon Neutrino Disappearance



NOVA has comparable goals

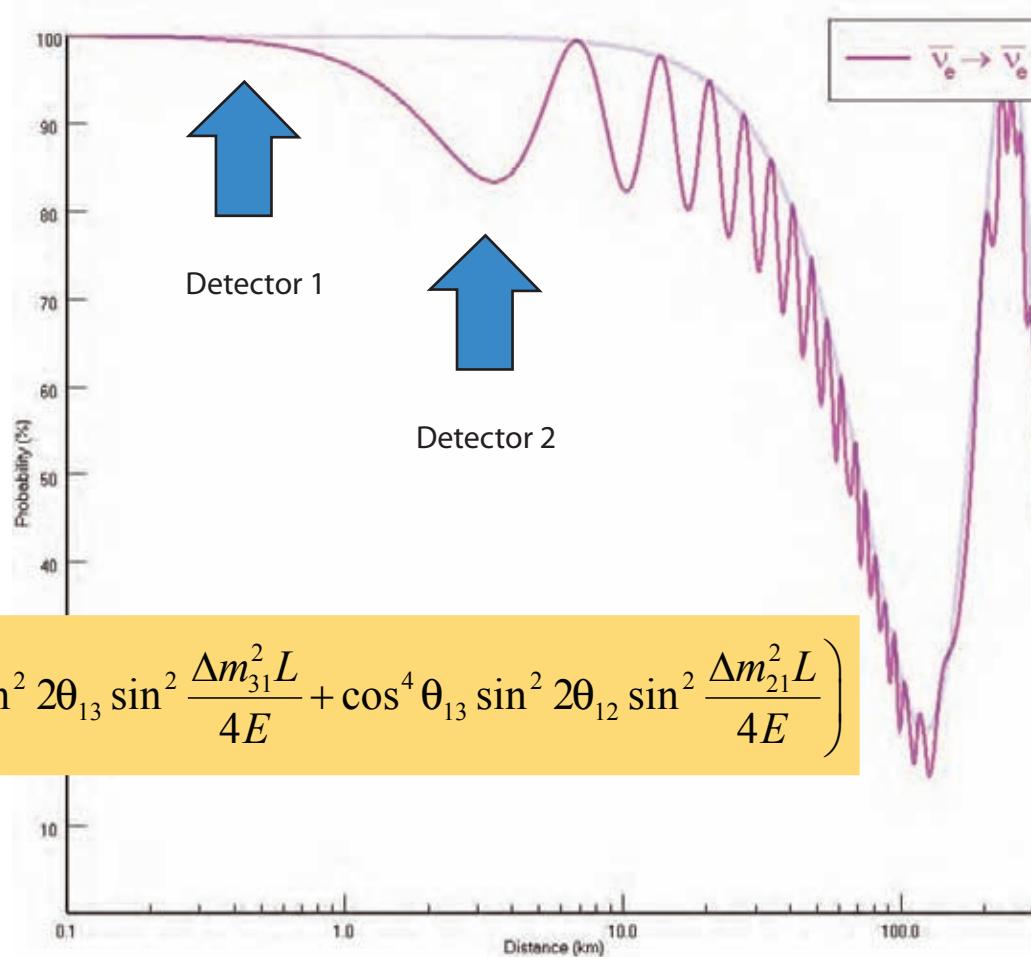
# Background is Single Pizero Events





# Two Detector Reactor Experiment

*requires very careful control of systematic effects*



**Best case scenario:**  
small wiggles assume  
 $\theta_{13}$  as large as allowed by  
CHOOZ limit

**smaller values  $\theta_{13}$ :**  
 $P_{\text{surv}}$  recedes to  
the faint blue curve

must believably measure  
small difference in event rates

**Several sites  
being considered:**

**Braidwood (IL)**  
**Daya Bay (HK)**  
**Chooz (France)**

# How We Might Know What We Do Not Yet Know

- Are there only three neutrino states? (LSND)
  - mini-BooNE (2005)
- Can we really make an appearance experiment?
  - CNGS, SK? ( $\tau$ ); T2K, NOvA ( $e$ )
- What is the absolute mass scale?
  - KATRIN,  $0\nu\beta\beta$ , precision cosmology?
- Are neutrinos their own antiparticle? (Majorana)
  - Numerous  $0\nu\beta\beta$  experiments being proposed
- What is the sign of the large  $\Delta m^2$ ? (hierarchy  $\stackrel{+}{=}$  or  $\stackrel{-}{=}$ )
  - NOvA + T2K
- What is the value of  $\theta_{23}$ ? Is it truly maximal?
  - NOvA, T2K
- What is the value of  $\theta_{13}$ ? Is it really zero?
  - NOvA, T2K, new reactor experiment
- What is the value of  $\delta$ ?
  - upgraded off-axis experiments (eg. Hyper-K+4MW beam)

plus challenging proposed accelerators like  $\beta$ -beams and muon storage rings