



***CP* Violation in the *B* Meson System**

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Outline

- Refresher (hadrons, C , P , and T)
- Historical background
- Why is it interesting to study CP violation?
- How CPV arises in the Standard Model
 - B meson decays and B -Factories

Review of Basic Principles

Particle Zoo 101

- For each fundamental particle x there is an antiparticle \bar{x}
- Observed particles are the **leptons** and bound states of **quarks** (hadrons) \longrightarrow two types:

| Mesons (bosons) $q\bar{q}'$ | Baryons (fermions) $q_1q_2q_3$ |
|--|--------------------------------|
| $u\bar{d} = \pi^+$ $u\bar{s} = K^+$ $d\bar{s} = K^0$ | $uud = p$ $udd = n$ |

- **Strong force** keeps quarks bound into hadrons
- **Weak force** responsible for radioactive decay \Rightarrow lepton and quark flavor changes

Discrete Operations

- The field equations (*Lagrangians*) for particle interactions are symmetric under certain discrete operations or transformations.
- Invariance of these equations under such transformations imply existence of conserved, multiplicative quantum numbers.
- There are 3 particularly important such operations in particle physics...

C: Charge Conjugation

Particle \longrightarrow Anti-particle



Charged particle wavefunctions not eigenstates

$$C|e^{-}\rangle = |e^{+}\rangle \neq \pm|e^{-}\rangle$$

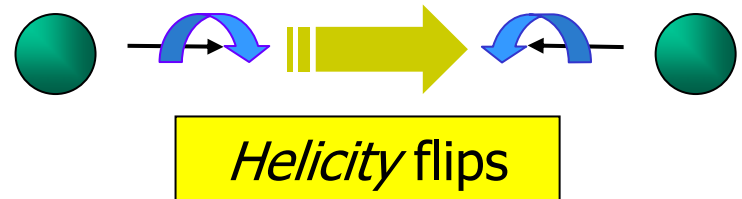
Many neutral particles are (eigenvalue ± 1)

$$C|\gamma\rangle = -|\gamma\rangle \quad C|\pi^0\rangle = +|\pi^0\rangle$$

P: Parity

Reflects a system through the origin

- $\mathbf{x} \rightarrow -\mathbf{x}$ and $\mathbf{p} \rightarrow -\mathbf{p}$
- but $\mathbf{L} \rightarrow \mathbf{L}$



Particles have intrinsic parity:

$$P|\gamma\rangle = -|\gamma\rangle \quad P|\pi^0\rangle = -|\pi^0\rangle$$

Fermions: opposite parity for particle and antiparticle

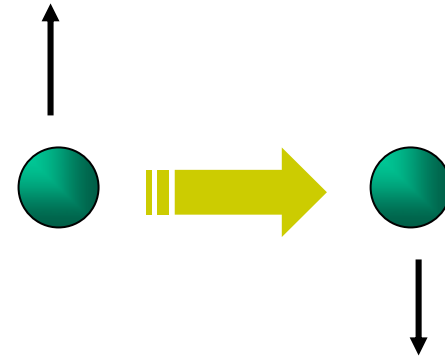
Bosons: same parity for particle and antiparticle

T: Time Reversal

Reverses direction of time

$$- t \longrightarrow -t$$

$$- \mathbf{p} \longrightarrow -\mathbf{p}$$



The *CPT* Theorem

- These 3 operations are connected through invariance of combined *CPT* for **all** forces
- *CPT* Theorem: all field theories are invariant under this combo of operations (any order)
 - Consequences:
 - particles and antiparticles have same mass and lifetime
 - particles obey spin statistics (Fermi or Bose)

Historical Background

Conservation of C , P , and T ?

Strong, electromagnetic and gravitational interactions are observed to be invariant under C , P , and T , separately.

Weak Interaction...

- It conserves *neither* C *nor* P .
- First postulated by Lee and Yang in 1956 and verified in studies of β decay of Cobalt.
- Later observed in many other systems (neutrinos, etc.).

Violation of C and P in Weak Decays

Neutrino system:

$$\begin{array}{l} \nu_L \xrightarrow{C} \bar{\nu}_L \\ \nu_L \xrightarrow{P} \nu_R \end{array} \left. \vphantom{\begin{array}{l} \nu_L \\ \nu_L \end{array}} \right\}$$

Neither of these states are observed in nature

Example \Rightarrow Pion decay:

$$\Gamma(\pi^+ \rightarrow \mu^+ \nu_L) \neq \Gamma(\pi^- \rightarrow \mu^- \bar{\nu}_L) = 0 \quad C \text{ violation}$$

$$\Gamma(\pi^+ \rightarrow \mu^+ \nu_L) \neq \Gamma(\pi^+ \rightarrow \mu^+ \nu_R) = 0 \quad P \text{ violation}$$

Conservation of CP ?

- For a long time it was thought that CP was conserved in weak interactions:

$$\Gamma(\pi^+ \rightarrow \mu^+ \nu_L) = \Gamma(\pi^- \rightarrow \mu^- \bar{\nu}_R)$$

⇒ CP invariance

But in 1964, an expt by Christenson, Cronin, Fitch and Turlay first demonstrated CP violation in the weak decays of K^0 mesons

CPV in Kaon Decays

- Two distinct neutral kaon states had been observed:
 $K_1^0 \rightarrow$ short lifetime, *CP* even (eigenvalue +1)

$K_2^0 \rightarrow$ long lifetime, *CP* odd (eigenvalue -1)

$$\tau(K_1^0 \rightarrow 2\pi) = 0.9 \times 10^{-10} \text{ sec}$$

$$\tau(K_2^0 \rightarrow 3\pi) = 0.5 \times 10^{-7} \text{ sec}$$

- The 1964 expt discovered the longer-lived kaon decaying, very rarely ($\sim 10^{-3}$) to the 2π , *CP* = +1 state

$$\left. \begin{aligned} |K_L^0\rangle &= |K_2\rangle + \varepsilon |K_1\rangle \\ |K_S^0\rangle &= |K_1\rangle - \varepsilon |K_2\rangle \end{aligned} \right\} |\varepsilon| \approx 2 \times 10^{-3}$$

Why Such Interest in *CP* Violation?

Interest in CP Violation

- What is it about the weak interaction that generates CP violation?
 - It is naturally present in the **Standard Model** of particle physics
- Can we observe it in decays of other particles besides the kaon?
 - Compare measurements with predictions of the Standard Model
- Can we observe the effects of **New Physics**?
 - Super Symmetry, String Theory → sources of more CPV
 - Amount of CPV from SM alone does not explain large matter-antimatter asymmetry of present universe

***CP* Violation in the Standard Model: *B* Meson Decays**

$$B^0 = \bar{b}d$$

$$\bar{B}^0 = b\bar{d}$$

CPV in the Decays of *B* Mesons

- As we shall see, *CP* violation expected to be relatively large (hopefully experimentally observable!) in the decays of *B* mesons to certain final states.
- “*B*-Factories” built in US (*BaBar*) and Japan (*Belle*) to produce hundreds of millions of *B* mesons, with goal of looking for *CP* violation \Rightarrow differences in *B* and \bar{B} decay rates
 - Colliders of e^+ and e^- beams \rightarrow production of $B\bar{B}$ pairs
 - Began running in 1999 and plan to continue until ~ 2009
- Looking for *CP* asymmetries...

CP Asymmetries

- Example: Look for *CPV* in the *B* meson decay to final state *X* (system of final state particles)

$$\mathcal{A}_{CP} = \frac{\Gamma(\bar{B} \rightarrow \bar{X}) - \Gamma(B \rightarrow X)}{\Gamma(\bar{B} \rightarrow \bar{X}) + \Gamma(B \rightarrow X)}$$

$$\Gamma(B \rightarrow X) \propto |A_X|^2$$

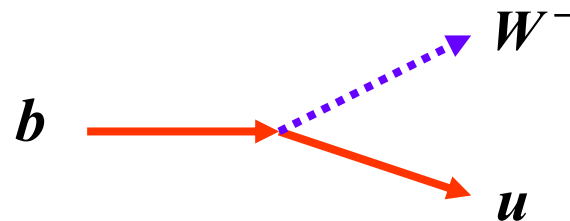
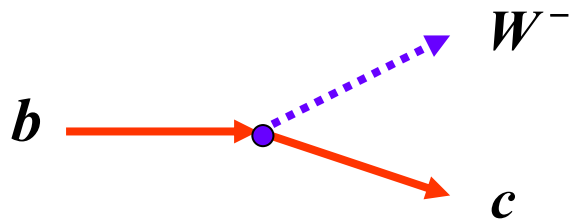
$$\Gamma(\bar{B} \rightarrow \bar{X}) \propto |\bar{A}_{\bar{X}}|^2$$

- $\Gamma(B \rightarrow X)$ is the decay rate for *B* to decay to *X*
- $A_{B \rightarrow X}$ is the “transition amplitude” for this decay (complex #)

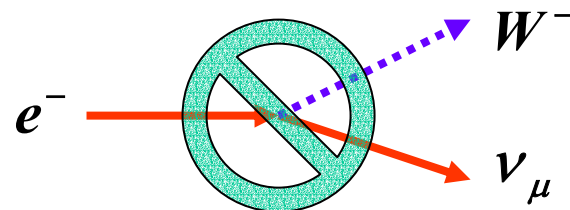
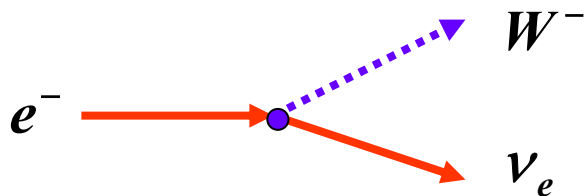
- $\mathcal{A}_{CP} \neq 0$ is violation of *CP* conservation

The SM Weak Decays

Quark "generation" can change in weak decays
(quark mixing):

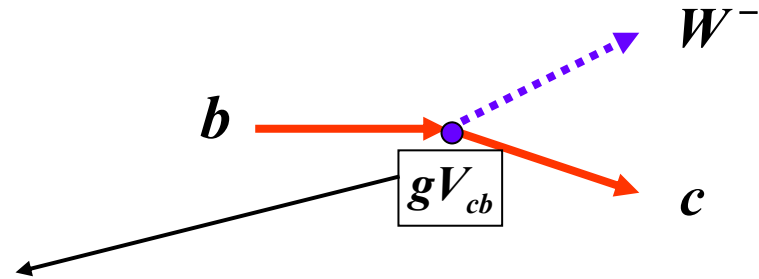


Not so for leptons:



The Weak Couplings of Quarks

- The coupling strength at the vertex is given by
 - g is a *universal* weak coupling
 - gV_{ij} depends on the initial and final state quark
 - For leptons, only g (?)



- The V_{ij} can be written as a matrix (CKM matrix)
- $V_{ij} \Rightarrow V_{ij}^*$ For antiquarks

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

The transition amplitude, A , is proportional to the product of the couplings for each vertex in the given weak decay

Properties of the CKM Matrix

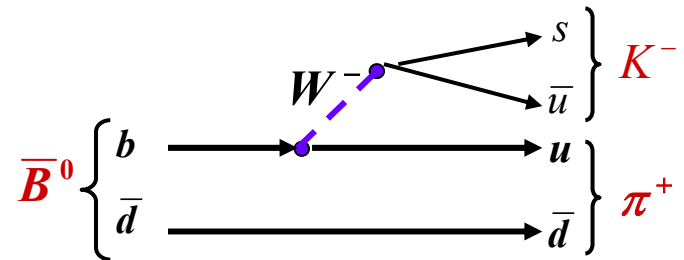
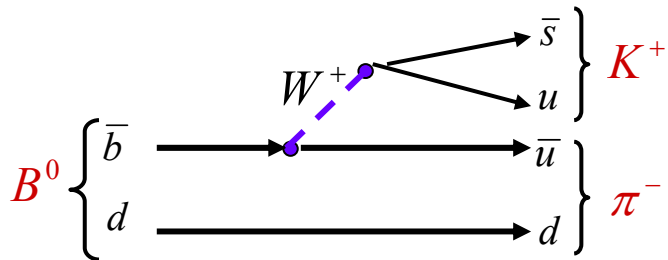
- The CKM matrix is a 3x3 complex, unitary matrix ($V^\dagger V = 1$)
- This means 4 independent parameters describe it:
 - 3 real numbers
 - **1 complex phase** → possibility of CP violation

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + O(\lambda^4)$$

All elements other than V_{td} and V_{ub} are real

CPV in B Decays: Example

- Example: $B^0 \rightarrow K^+ \pi^-$ and $\bar{B}^0 \rightarrow K^- \pi^+$



$$A_{K^+ \pi^-} = |A_{K^+ \pi^-}| e^{-i\gamma} e^{i\delta}$$

$$\bar{A}_{K^- \pi^+} = |\bar{A}_{K^- \pi^+}| e^{+i\gamma} e^{i\delta}$$

$$= |A_{K^+ \pi^-}| e^{+i\gamma} e^{i\delta}$$

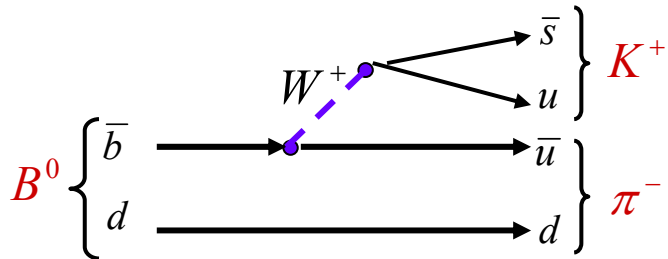
γ is the phase from V_{ub}

δ is any phase from "strong interactions"

$$\mathcal{A}_{CP} = 0 \text{ since } |\bar{A}_{K^- \pi^+}|^2 = |A_{K^+ \pi^-}|^2$$

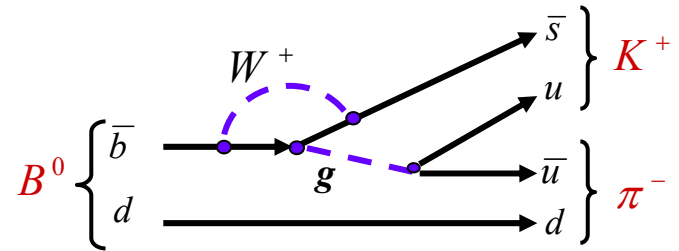
CPV in B Decays: Example

- But what if a second diagram exists...?



$$A_{K^+\pi^-}^T = \left| A_{K^+\pi^-}^T \right| e^{i(-\gamma+\delta_T)}$$

Tree



$$A_{K^+\pi^-}^P = \left| A_{K^+\pi^-}^P \right| e^{i\delta_P}$$

Penguin

$$A_{K^+\pi^-} = A_{K^+\pi^-}^T + A_{K^+\pi^-}^P = \left| A_{K^+\pi^-}^T \right| e^{i(-\gamma+\delta_T)} + \left| A_{K^+\pi^-}^P \right| e^{i\delta_P}$$

$$\bar{A}_{K^-\pi^+} = \bar{A}_{K^-\pi^+}^T + \bar{A}_{K^-\pi^+}^P = \left| A_{K^+\pi^-}^T \right| e^{i(\gamma+\delta_T)} + \left| A_{K^+\pi^-}^P \right| e^{i\delta_P}$$

CPV in B Decays: Example

- Now a non-zero CP asymmetry can be possible in SM!

$$\mathcal{A}_{CP} = \frac{\Gamma(\bar{B}^0 \rightarrow K^- \pi^+) - \Gamma(B^0 \rightarrow K^+ \pi^-)}{\Gamma(\bar{B}^0 \rightarrow K^- \pi^+) + \Gamma(B^0 \rightarrow K^+ \pi^-)}$$

$$\equiv \frac{|A_{K^- \pi^+}|^2 - |A_{K^+ \pi^-}|^2}{|A_{K^- \pi^+}|^2 + |A_{K^+ \pi^-}|^2}$$

$\neq 0$ if:
 $\gamma \neq 0, \pi/2$
 $\delta_T - \delta_P \neq 0, \pi/2$

$$= \frac{2|A_T||A_P|\sin\gamma\sin(\delta_T - \delta_P)}{|A_T|^2 + |A_P|^2 + 2|A_T||A_P|\cos\gamma\cos(\delta_T - \delta_P)}$$

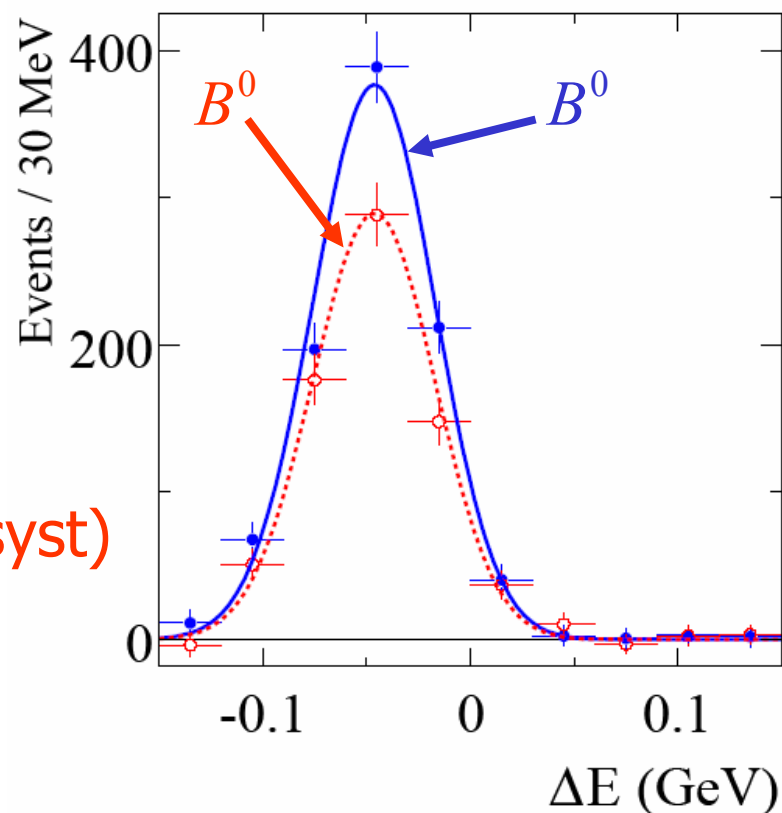
CP in *B* Decays: Example

- This *CP* asymmetry has just been observed for first time at the *BaBar* experiment!

In sample of ~ 550 million *B* mesons:

1606 ± 51 $B^0 \rightarrow K^+ \pi^-$
decays observed

$$\mathcal{A}_{CP} = -0.133 \pm 0.030(\text{stat}) \pm 0.009(\text{syst})$$



CPV in *B* Decays: Example

- Very interesting and important discovery of *direct CP* violation in *B* meson decays
 - But real goal is to try and make a measurement of the Standard Model parameters β and γ
- ➔ Not easy because we need theoretical predictions for values of $|A_T|$, $|A_P|$ and $\delta_T - \delta_P$
- A “cleaner” way involves measurements of *indirect CP* violation \Rightarrow see talk by Morii

Summary

- Study of CP violation in Weak decays of particles at forefront of particle physics research:
 - Crucial ingredient in cosmology → need to explain how the universe can exist as we observe it today!
 - Arises in the Standard Model (SM) via the single imaginary quantity in the quark-mixing (CKM) matrix, and nowhere else.
 - Until recently (2000), no reliable comparison of experimental measurements and SM predictions → effects had been predicted to be largest in decays of B mesons

Advent of B -Factories in 1999 to study this phenomenon
⇒ Very successful so far! CP asymmetries being observed

Do expt. measurements agree with SM...or New Physics?