

# High-Temperature Superconductors

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Superconductivity is a phenomenon of (a) exactly zero electrical resistance and (b) expulsion of magnetic flux fields occurring in certain materials, called superconductors, when cooled below a characteristic critical temperature  $T_c$ .

# Theory of superconductivity Continuous phase transition

Superconducting phenomenon is a **continuous phase transition**.

Bardeen–Cooper–Schrieffer (BCS) theory

- The "attractive" interaction between electrons allows the formation of "Cooper pairs" Ι. which do not follow the Pauli exclusion principle.
- **II**. The superconducting system is equivalent to an XY-lattice model. The dimension of order parameter is 2 (the amplitude & phase of wave function).

### Classification

- Type-I (e.g., mercury): the "attractive" interaction is s-wave and is symmetric. Ι.
- Type-II (e.g., bismuth strontium calcium copper oxide (BSCCO)): high-temperature, II. d-wave, penetration of magnetic field.

## Characterization



Conductor vs. Semiconductor vs. Superconductor



#### **Electrical resistance**



The critical temperature of the BSCCO sample is  $T_c \approx 103$  K, with a transition width of 6 K.

#### **Scaling behavior**

Given  $\varepsilon = (T - T_c)/T_c$ , we know that the correlation length and the correlation time should scale as

 $\xi \sim \varepsilon^{-\nu}$ ,  $\tau \sim \xi^{z} \sim \varepsilon^{-z\nu}$ .

The London's equation and Maxwell's equation suggest

 $B \sim \xi^{-2}, E/\xi \sim B/\tau.$ 

So, the voltage V (or electric field E) scales like

 $E \sim \varepsilon^{\nu(1+z)}$ .

### **Electrical resistance**



## Zoom-in of the critical transition region.

We find the slope  $v(1 + z) \approx 0.9$ . (Mean-field theory predicts v = 0.5 and z = 2.)

# **Meissner effect**

**Meissner effect** 

### Method of mirror images



The length dimension of  $F_{dipole-dipole}$  must be  $[L^{-2}]$ .

So,  $F_{\rm dipole-dipole} \propto m^2/d^4$ , with dipole moment m.





We find  $F_{\text{dipole-dipole}} \propto d^{-\gamma}$ , where  $\gamma = 3.09 \pm 0.39$  is smaller than what we expected.



## Systematic error:

□ (Electrical resistance) Impurity of the sample lowers the critical temperature.

□ (Meissner effect) The superconducting surface is not infinitely large.

□ (Meissner effect) The scale is made of "iron".

The next group could work on...

□ Characteristics of yttrium barium copper oxide (YBCO) material.

□ Measurement of critical magnetic field.

# References

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